

**Parent-preferred dispersal promotes cooperation in
structured populations**

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1 **Parent-preferred dispersal promotes cooperation in structured**
2 **populations**

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31 **Abstract**

32 Dispersal is a key process for the emergence of social and biological behaviours. Yet
33 far less attention has been paid to the dispersal effects on the evolution of cooperative
34 behaviour in structured populations. To address this issue, we propose two dispersal
35 modes, parent-preferred and offspring-preferred dispersal, into the birth-death update
36 rule, and then consider the update rule with parent-preferred and offspring-preferred
37 dispersal into evolutionary prisoner's dilemma on random-regular, small-world, and
38 scale-free networks, respectively. We find that parent-preferred dispersal favours the
39 evolution of cooperation in these different types of population structures and
40 offspring-preferred dispersal inhibits the evolution of cooperation in homogeneous
41 populations. But in scale-free networks when the parent-preferred dispersal strength is
42 weak, cooperation is greatly enhanced for intermediate offspring-preferred dispersal
43 strength, and cooperators can coexist with defectors for strong offspring-preferred
44 dispersal strength. Moreover, our theoretical analysis precisely predicts the
45 evolutionary outcomes in random-regular networks. We also incorporate these two
46 dispersal modes into other three update rules, that is, death-birth, imitation, and
47 pairwise comparison update rules, respectively, and find that similar results about
48 effects of parent-preferred and offspring-preferred dispersal can be observed in
49 different types of population structures. Our work, thus, unveil robust effects of
50 individual preferential dispersal on the evolution of cooperation in different
51 interactive environments.

52 **Keywords**

53 prisoner's dilemma, cooperation, population structures, dispersal, update rule

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55 **1. Introduction**

56 How to understand the emergence of cooperation among rational individuals is a
57 central challenge in evolutionary biology as well as social sciences. Evolutionary
58 game theory provides a common mathematical framework to interpret the evolution
59 of cooperation [1-3]. In particular, the prisoner's dilemma game, as a typical example,
60 has attracted considerable attention [4,5]. The prisoner's dilemma is traditionally
61 studied in an infinite, well-mixed population, where all individuals are equally likely
62 to interact with each other. However, the well-mixed population typically opposes the
63 evolution of cooperation [6].

64 In the past few years, it has been increasingly realized that real populations are
65 not well-mixed, but structured, which can be well described by some network models,
66 e.g., small-world [7] and scale-free networks [8]. Many studies show that population
67 structures can promote cooperation via network reciprocity [9-18]. In particular,
68 network heterogeneity is identified as the main driving force behind the flourishing
69 cooperative behavior in scale-free networks [11,12]. However, such positive effects
70 from network reciprocity do not always hold well for the evolution of cooperation,
71 even in heterogeneous networks. For example, the advantage of heterogeneous
72 networks in the evolution of cooperation can be greatly weakened by participation
73 costs [19] or normalizing the accumulative payoff [20]. The update rule also plays an
74 important role in the evolution of cooperation in social networks [9,21-23].
75 Remarkably, it is found that death-birth update in social networks allows the
76 evolution of cooperation if the benefit-to-cost ratio in the prisoner's dilemma exceeds
77 the average degree of the graph [13]. But surprisingly, under the birth-death update
78 rule [24] cooperation can be never favoured in different types of network structures
79 [13]. These findings show that the birth-death update rule can strongly suppress the
80 favouring factors of network reciprocity for the evolution of cooperation.

81 Under the original birth-death update rule, a player is chosen for reproduction
82 from the entire population proportional to fitness, and then the offspring replaces a
83 random neighbour of the parental player. Such dispersal behaviour of offspring for the
84 new site will influence the parent's fitness in the game framework, even if the dispersal
85 model is random and local. Thus how to replace the neighbour site of parental player
86 may cause the competition between the offspring and the parent when only local
87 interaction is allowed [25]. Under this competitive scheme, when an individual is

88 selected from the entire population proportional to fitness and then engenders an
89 offspring, the offspring may replace a site of the neighbours according to some
90 preferential dispersal modes, rather than the random dispersal mode. In this work, we
91 thereby consider two different local dispersal modes driven by the parent and
92 offspring respectively [26], that is, parent-preferred dispersal and offspring-preferred
93 dispersal, and assume that the new location for the offspring under the birth-death
94 update rule is determined by parent-preferred dispersal and offspring-preferred
95 dispersal together. On the one hand, under the offspring-preferred dispersal the
96 offspring prefers to have a favourable interactive environment after leaving for the
97 new site [27]. Whereas, on the other hand, under the parent-preferred dispersal the
98 parent prefers to improve or maintain its own interactive environment through the
99 offspring's replacing. This may correspond to the phenomenon that, for example, in
100 the animal world young and male lions are abandoned or ostracized from the group, in
101 order to hold the predominance and reduce the competition from future generations
102 [28].

103 In this paper, we incorporate such two preferential dispersal modes
104 simultaneously into the birth-death update rule in structured populations, where
105 individuals can have some information about their surrounding environments. We
106 assume that individuals can not only easily observe the information about their nearest
107 neighbours, but also obtain the information about other individuals through their close
108 friends in a social manner since most of individuals can only have local information
109 about others in realistic networked systems [29,30]. Based on the local information
110 the parent and identical offspring can inspect the environments around the new
111 locations. And the potential gains of the parent and offspring after the offspring's
112 replacing could thus be set as two quantities for parent-preferred and
113 offspring-preferred dispersal, which can characterize the surrounding interaction
114 environments for the parent and offspring, respectively. Accordingly, the new
115 location for the offspring can be determined in combination with these quantities.

116 In this work, we then study how the dispersal rule based on parent-preferred
117 and offspring-preferred dispersal affects the evolution of cooperation in different
118 types of population structures including random-regular [31], small-world, and
119 scale-free networks. Also, we develop the pair-approximation method for some
120 theoretical analysis on regular networks. We find that parent-preferred dispersal can
121 always favour the evolution of cooperation in different types of social networks. In

122 addition, offspring-preferred dispersal inhibits the evolution of cooperation in
 123 homogeneous networks, whereas in heterogeneous networks there exists an
 124 intermediate offspring-preferred dispersal strength at which cooperators can be
 125 promoted for weak parent-preferred dispersal strength. We also explicitly incorporate
 126 parent-preferred and offspring-preferred dispersal modes into other three strategy
 127 update rules including death-birth, imitation, and pairwise comparison update rules
 128 [32-37], and find that our main results about effects of parent-preferred and
 129 offspring-preferred dispersal hold against the changes of the update rules.

130 **2. Model**

131 We consider the evolutionary prisoner's dilemma game in structured populations.
 132 Following previous study [5], we adopt the game's payoff matrix as

$$M = \begin{bmatrix} b - c & -c \\ b & 0 \end{bmatrix},$$

133 where b represents the benefit of cooperation, and c ($0 < c < b$) represents the cost
 134 of cooperation.

135 Initially, each player x is designated to play either as a cooperator (C) or as
 136 defector (D), and occupies one node of the network. At each time step, each player x
 137 engages in pairwise interactions with all its adjacent neighbours, and then collects its
 138 payoff P_x based on the payoff matrix parameters. Furthermore, player x obtains its
 139 fitness associated with the payoff information, given as [38]

$$f_x = e^{wP_x},$$

140 where $w > 0$ is the intensity of selection. In our present study, we adopt the
 141 exponential function of fitness so that each individual's fitness is always positive. In
 142 order to avoid amplifying the fitness difference among the population under this
 143 exponential function, in the main context we simply set $w = 0.01$.

144 After playing the games, individual x is chosen for reproduction proportional
 145 to its fitness. In other words, individual x is selected with probability f_x/T for
 146 reproduction, where $T = \sum_j f_j$ denotes the total amount of fitness in the population.
 147 We assume that individual x reproduces an identical offspring x_o , and only has
 148 local information about its nearest and next-nearest neighbours. Hence, parent x can
 149 obtain its expected fitness and its offspring's expected fitness when one site in its
 150 neighbourhood is chosen for its offspring x_o . In combination with these expected
 151 fitness information, the selection probability of offspring x_o replacing one of the

152 neighbours y is set as

$$153 \quad P_{x_o \rightarrow y} = \frac{(f_{x_o x_o \rightarrow y})^\alpha (f_{x x_o \rightarrow y})^\beta}{\sum_{z \in \Omega_x} (f_{x_o x_o \rightarrow z})^\alpha (f_{x x_o \rightarrow z})^\beta},$$

154 where the sum is over all the neighbours of x , $f_{x_o x_o \rightarrow y}$ denotes the expected fitness of
 155 offspring x_o when x_o occupies the site of player y , $f_{x x_o \rightarrow y}$ denotes the expected
 156 fitness of parent x when x_o occupies the site of player y , $\alpha > 0$ denotes the
 157 offspring-preferred dispersal strength, and $\beta > 0$ denotes the parent-preferred
 158 dispersal strength. In particular, for $\alpha = 0$ and $\beta = 0$ the offspring will replace a
 159 random neighbour of player x , and in this case the original birth-death rule is
 160 considered [13].

161 In this study, we focus on the effects of α and β on the evolution of
 162 cooperation in three different types of population structures, including random-regular,
 163 small-world, and scale-free networks. Instead of the fixation probability of
 164 cooperation, the key quantity for characterizing the cooperative behaviour of the
 165 population is the density of cooperators, which is defined as the fraction of
 166 cooperators in the population. We use individual-based simulations as well as the
 167 pair-approximation method to perform this study.

168 Simulations are carried out in a population with the size $N = 1000$. The
 169 average number of neighbours in each network model (including random-regular,
 170 small-world, and scale-free networks) is set to 4. We implement the simulation with
 171 asynchronous update [14,39]. Initially, the two strategies of C and D are randomly
 172 distributed among the population with an equal probability 0.5. Under stochastic
 173 dynamics, the population will converge to one of the two possible absorbing states:
 174 full cooperation or full defection [29]. We run 10^2 independent realizations for each
 175 set of parameter values, and compute the fraction of times that the system evolves to
 176 full cooperation as the density of cooperators [27,32]. However, if the population does
 177 not converge to an absorbing state after 5×10^6 generations, the cooperation level is
 178 determined by the average fraction of cooperators in the population over the last
 179 2×10^4 generations.

180 **3. Results**

181 First, we incorporate the proposed offspring-preferred and parent-preferred dispersal
 182 modes into the birth-death update rule, and respectively show the fraction of

183 cooperators depending on α and β together in random-regular, small-world, and
184 scale-free networks, as plotted in figure 1. We see that in random-regular and
185 small-world networks the cooperation level dramatically decreases as the
186 offspring-preferred dispersal α increases, whereas intensively increases as the
187 parent-preferred dispersal β increases (figure 1*a* and 1*b*). Moreover, full defection
188 can be easily achieved for strong offspring-preferred dispersal strength and weak
189 parent-preferred dispersal strength, whereas full cooperation can be easily achieved
190 for weak offspring-preferred dispersal strength and strong parent-preferred dispersal
191 strength. However, in scale-free networks, the cooperation level monotonically
192 increases with increasing the parent-preferred dispersal strength β for fixed α
193 (figure 1*c*). For larger fixed values of β , the cooperation level gradually decreases
194 with increasing the offspring-preferred dispersal α . Surprisingly, for smaller fixed
195 values of β (e.g., $\beta = 1$), the cooperation level first increases from zero until
196 reaching the maximum value, and then decreases with increasing α . It means that for
197 small values of β , there exists an intermediate value of α , which can results in the
198 optimal cooperation level in scale-free networks. In addition, the cooperation level is
199 not very low when the value of α becomes large, indicating that cooperators can
200 coexist with defectors.

201 In figure 2, we provide the theoretical results by pair-approximation method in
202 regular networks (for details see electronic supplementary material). By comparison,
203 we find that theoretical analysis agrees well with numerical simulations in
204 random-regular networks, as shown in figure 1*a*. However, this theoretical method
205 cannot well predict simulation results in other types of networks, especially in
206 scale-free networks. Here, we do not provide the theoretical results by the extended
207 pair-approximation method considering the clustering effect and degree fluctuation
208 [13,40]. Despite this point, our present theoretical analysis qualitatively reflects the
209 roles of parent-preferred dispersal and offspring-preferred dispersal in the evolution of
210 cooperation in structured populations.

211 What is the origin of such a boost of cooperation by the parent-preferred
212 dispersal mode in different types of networks? In fact, when a defector is chosen for
213 reproduction, it implies that this defector has a higher fitness and is surrounded by
214 some cooperators. Under the parent-preferred dispersal, the defective parent prefers to
215 let the offspring replace a defective neighbour's site, rather than a cooperative

216 neighbour's. In this situation, although the parent can keep having a higher fitness, the
217 spreading of defective behaviour is inhibited in the population (figure 3a). Moreover,
218 in the initial conditions of 50% cooperators and for weak selection, cooperators can
219 also have the opportunity to be chosen for reproduction in these types of population
220 structures, especially in scale-free networks. When a cooperator is chosen for
221 reproduction, it implies that the cooperator should directly connect more cooperative
222 neighbours than others. Under the parent-preferred dispersal, if the cooperative parent
223 also directly connects some defectors, the offspring prefers to replace the defective
224 site so that the parent can have a higher fitness. On the one hand, such replacement
225 can expand the cooperators' clusters, and the cooperative behaviour is spreading
226 (figure 3a). On the other hand, it leads to a positive feedback mechanism, so that
227 cooperators in the population can have more opportunities to be chosen for
228 reproduction. Consequently, cooperative behaviour can evolve and prevail in
229 structured populations.

230 Why does the offspring-preferred dispersal inhibit the evolution of
231 cooperation in random-regular and small-world networks? In fact, under the
232 offspring-preferred dispersal, when a defector is chosen for reproduction, the
233 offspring prefers to choose a neighbour who is connecting more cooperators.
234 Accordingly, this defective offspring replaces a cooperative neighbour of the parent.
235 This is because that the cooperative neighbour often connects other cooperators under
236 the birth-death rule without mutation, and it has the same (similar) number of
237 interacting neighbours to others' in random-regular (small-world) networks.
238 Correspondingly, the defective offspring can have a higher fitness, but the defective
239 behaviour is spreading in the population (figure 3b). On the other hand, when a
240 cooperator is chosen for reproduction, the offspring prefers to take over a cooperative
241 neighbour of its parent so that the offspring can have a higher fitness in
242 random-regular and small-world networks. However, such replacing for its offspring
243 is unfavourable to the expansion of cooperators' cluster, and hence the spreading of
244 the cooperative behaviour in the population is slow and stagnated (figure 3b).

245 It still remains to explain why cooperators can survive in scale-free networks
246 under the strong offspring-preferred dispersal. To do this, we investigate the time
247 evolution of bias in distribution of cooperators across degree number in scale-free
248 networks. as shown in figure 4. We define the distribution bias for each time step t

249 as $\text{sign}[b_k(t)]1/(1 + 1/|b_k(t)|)$, where $b_k(t) = [\rho_{ck}(t) - \rho_c(t)]/\rho_c(t)$. Here,
250 $\rho_c(t)$ represents the total fraction of cooperation at time t , and $\rho_{ck}(t)$ represents the
251 fraction of cooperators on nodes with degree k at time t .

252 We find that for weak offspring-preferred strength, as time increases the
253 fractions of cooperators on high-degree and middle-degree nodes first becomes
254 smaller than the total fraction of cooperation in the whole population (figure 4a). Thus,
255 cooperation cannot evolve in this situation. For moderate offspring-preferred dispersal
256 strength, as time increases the fractions of cooperators on high-degree and
257 middle-degree nodes becomes higher than the total fraction of cooperation in the
258 whole population, which induces a positive feedback mechanism for the evolution of
259 cooperation (figure 4b). For strong offspring-preferred dispersal strength, as time
260 increases there are always some fluctuations of distribution bias of cooperators on
261 high-degree and middle-degree nodes (figure 4c). Hence, cooperators cannot stably
262 dominate the high-degree nodes, which indeed play a crucial role in the emergence of
263 cooperation in scale-free networks [11]. However, in this situation cooperators can
264 coexist with defectors for a long time. This is because that in scale-free networks
265 individuals occupying high-degree nodes can be easily chosen for reproduction. When
266 a D-hub is chosen, its offspring prefers to move the site of one nearest neighbour with
267 high-degree number for strong offspring-preferred dispersal strength. This induces a
268 negative feedback mechanism that reduces their fitness and the opportunity of being
269 chosen for reproduction. When a C-hub is chosen, its offspring prefers to move the
270 site of one nearest neighbour with high-degree number for strong offspring-preferred
271 dispersal strength. Moreover, for strong offspring-preferred dispersal strength the
272 cooperative offspring always prefers to choose the high-degree nodes for replacing.
273 This does not facilitate the expanding of cooperator clusters in the networks. However,
274 cooperators can still coexist with defectors in this situation. On the contrary, under
275 relatively weaker offspring-preferred dispersal strength the cooperative offspring may
276 prefer to choose the site with other degree classes for replacing, which is helpful to
277 the spreading of cooperative strategy. Consequently, cooperative behaviour can
278 dominate the whole population.

279 Finally, it is of interest to elaborate on the generality of the effectiveness of
280 offspring-preferred and parent-preferred dispersal for the evolution of cooperation. To
281 do so, we further incorporate explicitly the offspring-preferred and parent-preferred

282 dispersal modes into other three update rules, that is, death-birth, imitation, and
283 pairwise comparison update rules, respectively (for detailed description see electronic
284 supplementary material). We still find that under these three different update rules the
285 parent-preferred dispersal approach can promote the evolution of cooperation in
286 different types of population structures, and in scale-free networks cooperation can be
287 still enhanced by an intermediate value of offspring-preferred dispersal strength when
288 the parent-preferred dispersal strength is not high (electronic supplementary material,
289 figure S2). However, together with figure 1, we can further find that under the
290 birth-death update rule a favourable cooperation level can be achieved in a wider
291 parameter range in comparison with the results for other three update rules.
292 Noticeably, full cooperation can only be realized in a relatively narrow parameter
293 range under the pairwise comparison update rule, since the intensity of selection also
294 influences the evolutionary outcome of cooperation [14].

295 **4. Discussion**

296 In this work, we have proposed two dispersal modes simultaneously into the
297 birth-death update rule, and shown that parent-preferred dispersal favours cooperation
298 to evolve in different types of population structures. Thus, our results indicate that
299 when some competition exists between the parent and its offspring in structured
300 populations, cooperative behaviour can thrive if the parent is more self-interested.
301 Moreover, we have found that offspring-preferred dispersal often inhibits the
302 evolution of cooperation in homogeneous networks. While for strong
303 offspring-preferred dispersal cooperators can coexist with defectors for a long time in
304 a heterogeneous population. And, compared with the case without offspring-preferred
305 dispersal or parent-preferred dispersal in scale-free networks cooperation is still
306 promoted by the introduction of offspring-preferred dispersal in scale-free networks
307 (electronic supplementary material, figure S1). Our work highlights the importance of
308 dispersal rule to the evolution of cooperation in structured populations.

309 Our dispersal rule is one mode of local migration or mobility for individuals,
310 but is different from the ones often studied on a square lattice [41-46]. In the
311 traditional framework of migration, only the focal individual moves into an empty site
312 from an occupied one if needed, so that the spatial interactions and the number of
313 interactive individuals are both influenced, and even individuals can become isolated.

314 Such spatial dispersal has been considered into evolutionary games for studying the
315 evolution of cooperation [41-44] and the evolving biodiversity [45,46]. Whereas in
316 our study we propose two different dispersal modes and simultaneously incorporate
317 them into different types of population structures. Under our dispersal rule, only the
318 offspring individual replaces the site of the neighbouring individual who is chosen to
319 be dead. Hence the empty site in our study is temporary. Moreover, previous study
320 found that when individuals move into a favourable environment for cooperation,
321 cooperation can prevail even in a noise condition [44]. However, in our framework
322 we find that when an offspring individual moves into a favourable interactive
323 environment for itself, cooperation cannot evolve in homogeneous populations.
324 Instead, when the offspring individual moves into a favourable interaction
325 environment for its parent, cooperation can flourish in structured populations. In fact,
326 under the birth-death update rule with random dispersal, cooperation can be never
327 favoured in structured populations [13]. Thus, in a sense our work extends the local
328 dispersal rule into different types of structured populations from the spatially
329 structured populations, and enriches the knowledge of local dispersal's effects on the
330 evolution of cooperation in structured populations.

331 Our dispersal approach is simultaneously driven by both the parent's and
332 offspring's preferences. And, dispersal competition exists between them, and such
333 kin-like competition works as the driver determining the final dispersal site of the
334 offspring. Here, we compare the relative contribution of parent-preferred and
335 offspring-preferred dispersal to the evolution of cooperation. Intuitively, cooperation
336 could be favourable under the strong offspring-preferred dispersal. This is because
337 that the parental individual may sacrifice its own interests for maximizing its
338 offspring's benefit in structured populations, leading to the emergence of kin selection
339 [6]. However, surprisingly we find that the parent-preferred dispersal can favour the
340 evolution of cooperation in different types of population structures, compared with the
341 offspring-preferred dispersal. Although cooperators can coexist with defectors in
342 scale-free networks for strong offspring-preferred dispersal strength, this result
343 depends on the topology features of scale-free networks.

344 We set that initially cooperators randomly occupy 50% of the sites of
345 individuals in the population, rather than only one cooperator like Ref. [13]. In fact, in
346 that harsh initial condition, the only one cooperator is chosen for reproduction with an
347 extremely small probability in scale-free network with large population size (e.g.,

348 $N = 1000$) in some simulation realizations. Conversely, the cooperator could be
349 replaced by the defective offspring with a higher probability even under strong
350 parent-preferred dispersal. Hence this initial condition can greatly diminish the
351 positive effects induced by strong parent-preferred dispersal. Correspondingly, we
352 consider that cooperators and defectors are equally distributed on the population
353 structure as the initial condition in our study as previous works did [11,12]. In
354 addition, we use the fraction of cooperators as the key quantity instead of the fixation
355 probability of cooperation. This is because that we find that cooperators can coexist
356 with defectors for a long time in scale-free network under some parameter settings
357 (figure 1c), even if initially half the players are cooperators. Furthermore, we only
358 provide the theoretical results by the pair-approximation method for regular graphs in
359 this work. In fact, there are some improved pair-approximation approaches by
360 considering the clustering effect and degree fluctuation [40,47], which can be used to
361 predict our evolutionary outcomes in scale-free networks. Thus, it is worth using these
362 approaches or further developing precise analytical tools to confirm our simulation
363 results in scale-free networks in the future [48].

364 In this work, we consider that the parent only has the local information of its
365 nearest and next-nearest neighbours, and the offspring can only replace one site of the
366 parent's nearest neighbours. That is to say, nearest-neighbour dispersal mode is used.
367 In fact, individuals may have the information of more neighbours in the population,
368 and they can move into distant sites in the population. If there are more placements
369 for dispersal, both the defective parent and offspring do not prefer that the offspring
370 moves to the nearest sites. And both cooperators and defectors prefer that they are
371 surrounded by more layers of cooperators when the distant dispersal mode is
372 considered. In this extended framework, it is worth studying how the non-local
373 parent-preferred and offspring-preferred dispersal modes are implemented in
374 structured populations and how they influence the evolution of cooperation in
375 structured populations. In addition, we do not include the effects of behavioural
376 mutation [37] or imitation errors [49] in the present study. For example, when an
377 individual is chosen for reproduction, mutation may occur on the offspring with a
378 probability. And stochastic effects arising from different sorts of errors may play an
379 important role in the cooperative behaviour at a population level. Thus, an interesting
380 extension is to examine the robustness of our results in the presence of mutation
381 errors.

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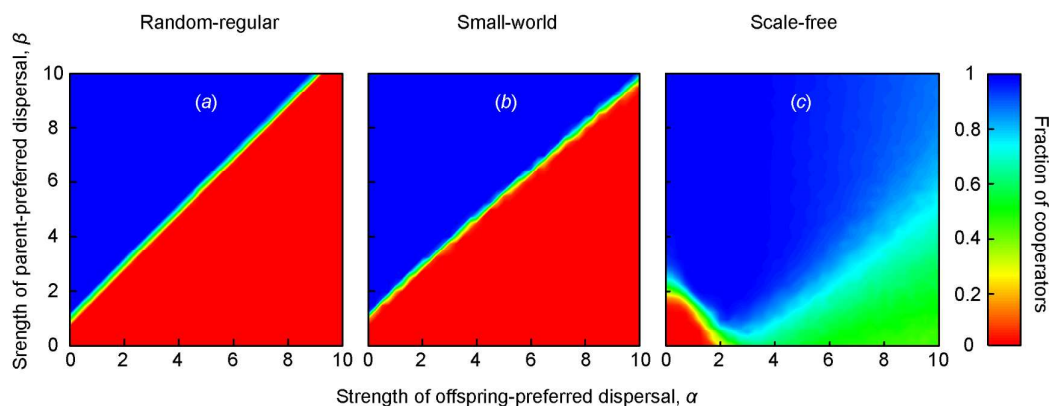
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547 **Figures and Captions**

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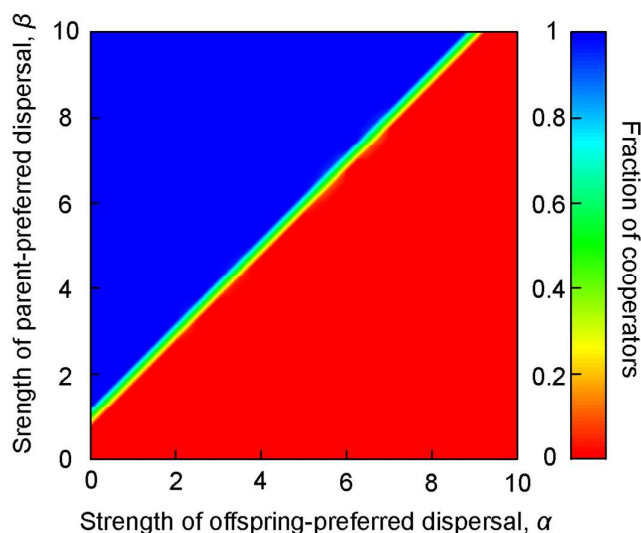
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551 **Figure 1:** Fraction of cooperators depending on offspring-preferred dispersal strength
 552 α and parent-preferred dispersal strength β in a contour plot form in random-regular
 553 (a), small-world (b), and scale-free (c) networks, respectively. Parent-preferred
 554 dispersal favours the evolution of cooperation in different types of population
 555 structures. In scale-free networks, cooperators can coexist with defectors under strong
 556 offspring-preferred dispersal strength. Here, $w = 0.01$ and $b/c = 4$.

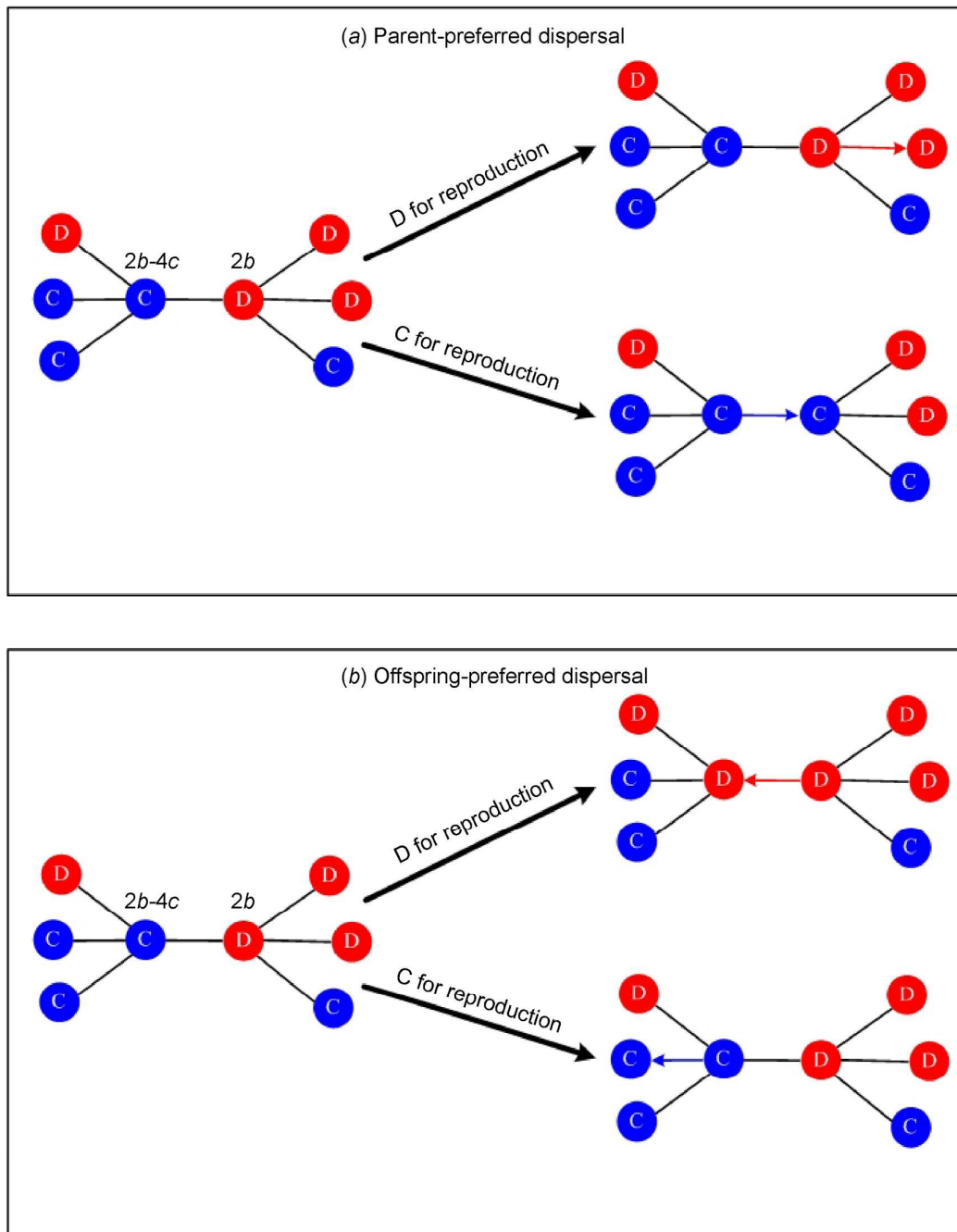
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559 **Figure 2:** Theoretical analysis by pair-approximation method in regular networks
 560 depending on the offspring-preferred dispersal strength α and parent-preferred
 561 dispersal strength β in a contour plot. The analysis precisely predicts the
 562 evolutionary outcomes in random-regular networks.

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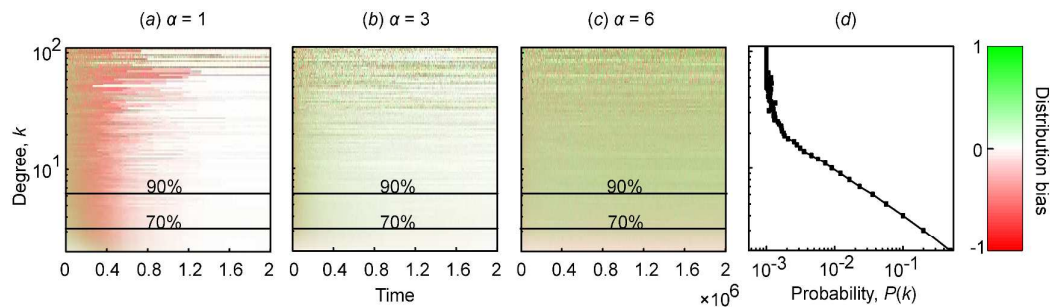


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565 **Figure 3:** Intuitive illustrations for microscopic evolution in homogeneous networks.
 566 We consider a cooperator-defector pair competing for the next reproduction event.
 567 The defector with payoff $2b$ has a great advantage to be chosen for reproduction.
 568 However, its left cooperative neighbour with payoff $2b - 4c$ can have the
 569 opportunity to be chosen for reproduction under the proportional birth rule and for
 570 weak selection. (a) Under the parent-preferred dispersal, the offspring of the focal
 571 defector prefers to replace a neighbouring defector; which induces a positive feedback

572 mechanism for the expanding of cooperator clusters. (b) Under the offspring-preferred
 573 dispersal, the offspring of the focal defector prefers to replace the site of the focal
 574 cooperator, leading to the expanding of defectors, whereas the offspring of the focal
 575 cooperator prefers to replace a cooperative neighbour.

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578 **Figure 4:** Time evolution of bias in distribution of cooperators across degree number
 579 in scale-free networks for weak parent-preferred dispersal strength $\beta = 1$ and
 580 different values of offspring-preferred dispersal strength: (a) $\alpha = 1$, (b) $\alpha = 3$, and (c)
 581 $\alpha = 6$. The distribution bias for each time step t is computed as $\text{sign}[b_k(t)]1/(1 +$
 582 $1/|b_k(t)|)$, where $b_k(t) = [\rho_{ck}(t) - \rho_c(t)]/\rho_c(t)$. Here, $\rho_c(t)$ represents the total
 583 fraction of cooperation at time t , and $\rho_{ck}(t)$ represents the fraction of cooperators on
 584 nodes with degree k at time t . (d) describes the degree distribution of scale-free with
 585 average degree number $k = 4$ and population size $N = 1000$. In the networks, there
 586 are 70% nodes whose degree number is not larger than 3, and 90% nodes whose
 587 degree number is not larger than 6. Here, $w = 0.01$ and $b = 4$.