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5	Optimizing functional groups in ecosystem models: Case study of the Great
6	Barrier Reef
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# 34 Abstract:

35	Uncertainty is inherent in ecosystem modelling, however its effects on modelling results are often
36	poorly understood or ignored. This study addresses the issue of structural uncertainty or, more
37	specifically, model resolution and its impact on the analysis of ecosystem vulnerability to threats.
38	While guidelines for node assignments exist, they are not always underlined with quantitative
39	analysis. Different resolutions of a coral reef network are investigated by comparing the simulated
40	network dynamics over time in various threat scenarios. We demonstrate that the error between a
41	higher-resolution and a lower-resolution models increases, first slowly then rapidly with increased
42	degree of node aggregation. This informs the choice of an optimal model resolution whereby a finer
43	level of a food web representation yields only minimal additional accuracy, while increasing
44	computational cost substantially. Furthermore, our analysis shows that species biomass ratio and the
45	consumption ratio are important parameters to guide node aggregation to minimize the error.
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47	Keywords: structural uncertainty, resolution, node aggregation, ecosystem models, foodweb model,
48	coral reefs
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51	1 Introduction
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53	Simplification of reality and related uncertainty is unavoidable in any applied research aiming to
54	support decision making; what influences the quality of analysis is how that uncertainty is
55	incorporated into management decision processes. This issue was highlighted by Ludwig et al. (1993),
56	who said: "effective policies are possible under conditions of uncertainty, but they must take
57	uncertainty into account". Walker et al. (2003) defines uncertainty as "any deviation from the
58	unachievable idea of completely deterministic knowledge of the relevant system". Another way of
59	thinking about uncertainty is that "uncertainty reflects the probability that a particular estimate, piece
60	of advice, or management action may be incorrect" (Lek, 2007). According to Menditto et al. (2007)

uncertainty is the quantitative expression of the performance characteristic accuracy with accuracy
being defined as "Closeness of agreement between a quantity value obtained by measurement and the
true value of the measureand". While these definitions describe uncertainty well, they do not
differentiate between different types of uncertainty.

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Uncertainty can arise at different instances in a modelling process. For the purpose of this paper, we 66 will concentrate on two types of uncertainty. Parameter uncertainty is defined as the difference 67 between the true value of a parameter and the mean value estimated using the data available and 68 statistical techniques (Skinner et al., 2014). Structural uncertainty refers to a mismatch between the 69 70 simplified mathematical equations of a model and the true complex ecological relationship observed 71 in situ (Refsgaard et al., 2006). One type of structural uncertainty, which is the one we focus on in this 72 study, is model resolution. In an ecological network, given a true number of species in the network, 73 the resolution refers to the level of aggregation within each node which is reflected in the total number 74 of nodes in the network. A node within the network represents an ecological unit that can be at 75 different aggregation levels incorporating one or more species. Generally, it is believed that low-76 complexity models reduce parameter uncertainty by reducing the number of parameters, while more 77 complex models reduce structural uncertainty since they more closely describe the natural system 78 (Iwasa et al., 1987). This leads to a hump shape between the level of complexity and the accuracy, 79 with medium complexity models often performing best (Håkanson, 1995, Costanza and Sklar, 1985, 80 Jester, 1977).

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Even though it has been acknowledged for a long time that different types of uncertainties are crucial,
their role is often not thoroughly understood, especially in complex models (Milner-Gulland and
Shea, 2017, Link et al., 2012). Previous attempts at addressing node aggregation in ecosystem models
(Fulton, 2001, Iwasa et al., 1987) have not been taken up by the average user of these kind of models.
As shown by Weijerman et al. (2015) who completed an extensive review of ecosystem models and of

the 27 ecosystem models reviewed only one addressed structural uncertainty as well as parameter
uncertainty. Instead, general guidelines are used to aggregate species (Heymans et al., 2016).

89

90 Ecosystems are complex due to the combination of multifaceted species interactions, which are often 91 nonlinear, which may result in multiple equilibria (Gordon, 2007, McClanahan et al., 2009). 92 Furthermore, ecosystem models are often faced with many threats which when included add to the 93 model complexity. Informing the management of systems under threat is often one of the main 94 modelling goals. Ecosystem models always involve high uncertainties, especially when attempting to 95 predict the effects of interventions and management actions (Costanza et al., 1993, Hill et al., 2007). If uncertainty is larger than believed, the results are more likely to be misleading, and are therefore 96 97 more likely to generate an inefficient or incorrect management decision (Weijerman et al., 2015). Lek 98 (2007)'s definition of uncertainty emphasizes this possibility of decision-makers being misled by 99 models.

100

Ecosystem models are usually created at a functional group level to reduce the number of nodes and 101 102 therefore parameters (Fulton et al., 2003). A functional group refers to a group of species that are 103 assumed to be so similar in a defined set of characteristics that they can be investigated as one unit. In 104 the literature, species are commonly grouped according to their trophic status and diet (e.g., herbivore, 105 or detritivore) (Stoddart, 1969). In ecosystem modelling a functional group is often used as the basis 106 of one node: Instead of treating each species as different and assigning a different dynamic equation 107 and parameters to each species, the functional group is assumed to be homogenous enough to be 108 represented by a single equation. Reducing resolution by considering functional groups only of course 109 reduces the total number of nodes in the system, which consequently, reduces the complexity and the 110 number of parameters that needs to be estimated. Guidelines about which species to group together 111 have existed for a long time (Gardner and Ashby, 1970, Wiegert, 1975, O'Neill, 1975, Cale Jr and 112 Odell, 1980), however, they never used to have any quantitative foundations and were based purely 113 on experience. In the more recent time, there have been a few, but not always thorough studies

114	(Fulton, 2001, Fulton et al., 2003, Pinnegar et al., 2005) that explore the uncertainty that is caused by
115	the introduction of functional groups as suggested in the literature. Thus, we lack an understanding of
116	the magnitude and even distribution of structural uncertainty in the threat response of ecosystems
117	(Bellwood and Fulton, 2008).

118

119 One ecosystem under threat that benefits from a whole ecosystem analysis is the marine environment, 120 specifically coral reefs. Coral reefs (here we will consider the Great Barrier Reef) are often made up 121 of thousands of species, making this system a great example for high level aggregation. A common 122 tool for ecosystem modelling in the marine environment, especially for the evaluation of fisheries 123 management, is Ecopath with Ecosim (Colléter et al., 2015). Ecopath is based on the estimation of 124 biomasses and food consumption to create a mass-balanced food web. It has been reviewed and 125 extended on over the past 40 years to enable dynamic simulations (Ecosim) and spatial analysis 126 (Ecospace) (Christensen and Walters, 2004). Since its inception, over 800 studies have used it to 127 investigate questions related to fisheries management. However, even though used extensively it does 128 not include a formal strategy to include structural uncertainty in its outputs or management 129 recommendations. In terms of designing the structure, specifically the resolution, of an Ecopath the 130 only guidance available to a new user are a few published guidelines (Heymans et al., 2016). These 131 guidelines are mostly based on experience and only underlined by a few selected and non-132 comprehensive analysis (Fulton, 2001).

133

In this study, we develop and apply a new approach of varying the resolution of an ecological network
while simulating the food web response to a species degradation. This will enable a comparison with
some of the guidelines and give them a quantitative foundation. The aim of this study is threefold:

We want to show that uncertainty introduced due to lowering the system resolution even
 slightly can be substantial and should not be neglected.

139 2) We want to propose a basis for choosing an optimal resolution to balance parameter and140 structural uncertainty.

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ecosystem models while also generalising these techniques for other types of networks.
These objectives are achieved by extensive simulations of a reef within the Great Barrier reef,
considering different levels of aggregation and threat scenarios. Followed by the evaluation of these
using visual examination, basic statistics as well as a machine learning algorithm.

3) We want to suggest ways to improve the guidelines and techniques used to group species in

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147 2 Methods

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The goal of this study is to understand how the ecosystem resolution affects the model's predictive 149 150 power in what concerns the effects of species degradation onto the entire ecosystem. To do so, we will 151 examine a number of "threat" scenarios, in which a fraction of a biomass of a focal species is removed 152 giving rise to changes in biomasses of other species because of feeding relationships. We will 153 evaluate the variation between threat impacts modelled based on a network at species level versus a network at a functional group level, which has a coarser resolution. For a single simulation we 154 calculate the error to reflect the accuracy of the simulation in relation to the reference model with full 155 156 resolution. Then we look at the distributions of the error over several simulations as a measurement of 157 uncertainty. To calculate errors, it is assumed that the high-resolution model reflects nature closely 158 and thus the error between the high- and low- resolution models can be used as an estimate of the 159 accuracy of a model structure. As the resolution of a model is a discrete characteristic, in this study, 160 nodes within a chosen functional group are being merged, one by one, to "imitate" a step-by-step 161 formation of the functional group. This enables a comparison of the response dynamics under the 162 same input (a particular threat scenario) and an estimation of the difference that each particular 163 merger entails. On this basis, a thorough understanding of the changes in the error and, consequently, 164 the uncertainty with a reduction in resolution can be obtained.

165

166 Naturally, one expects that a model should become more accurate with a finer resolution. However, it167 comes at a cost. This cost is made up of two components. First, a finer scale could result in more

parameter uncertainty, because the data underlying the parameters is not known well enough to
support this scale. Second, there is a cost of computing power that is required. In this study, we refer
to an "optimum" in terms of good overall accuracy (including both, parameter and structural
uncertainty) without an explosion of computational power.

- 172
- 173 2.1 Ecosystem simulation model and calibration

The dynamic ecosystem model used in this study is based on a network of interacting nodes that represent a single or a group of species. The interactions considered between the nodes resemble predation, i.e., the consumption of biomass of one node by another. This means that the connection between two nodes indicates organic matter being transported from one node to the other and travelling generally up the food chain. Organic matter can be lost from the living nodes to the external environment through energy spent in respiration. Egestion and other mortality that add to the detritus close the loop from high to low trophic levels of the food chain.

181

The network model used for this study is based on the Ecopath with Ecosim toolbox. We use Ecopath to calibrate our ecosystem network model and then we adopt Ecosim equations to simulate the ecosystem dynamics in response to a shock. We re-code the model in MATLAB for convenience of running simulations. In what follows, we present a general approach towards achieving the goal of this study as discussed above, and then we apply it to Great Barrier Reef as a case study.
First, we describe the modelling framework. Ecopath is a static mass-balanced ecosystem model describing the network through linear equations that connect biomasses, diet preferences, mortalities

and productions in an ecosystem. The static equations of Ecopath can then be extended to differential(difference) equations to allow for dynamic manipulations of the system (Ecosim extension).

196 
$$P_i = Q_i - R_i - U_i,$$
 (1)

197 where  $P_i$  represents the total biomass production of node i ( $t \ km^{-2} y ear^{-1}$ ) and  $Q_i$  represents the 198 total biomass consumption of node i ( $t \ km^{-2} y ear^{-1}$ ),  $R_i$  represents the respiration of node i199 ( $t \ km^{-2} y ear^{-1}$ ), which is a loss of a part of biomass to the environment and  $U_i$  represents the 200 amount of unassimilated food for each node i ( $t \ km^{-2} y ear^{-1}$ ) for all i = 1, ..., n with n being the 201 number of nodes in the ecosystem network. Unassimilated food refers to the amount of biomass lost 202 through excretion, i.e., the amount of biomass input into the lowest trophic level node called detritus. 203

The second master equation unfolds the node production of all nodes (besides detritus) that consists of the amount of its biomass consumed by other nodes plus the amount of biomass that emigrates and the amount of biomass that is lost due to natural mortality, here called other mortality or excretion. The flow from one node to another is assumed to be proportional to the total consumption of the noderecipient, which is sometimes called top-down or recipient control:

209

$$P_{i} = \sum_{i} Q_{i} D C_{ii} + E_{i} + P_{i} (1 - E E_{i}),$$
<sup>(2)</sup>

where  $DC_{ij}$  = proportion of the consumption by predator *j* that is made up of prey *i* (unitless),  $E_i$  = net emigration (emigration – immigration;  $t \ km^{-2}year^{-1}$ ); and  $EE_i$  = ecotrophic efficiency (unitless). The ecotrophic efficiency is the proportion of production that is passed onto the next trophic level. This parameter is smaller than one due to natural mortality.

214

Compared to the standard form of the second master equation found in many publications (Christensen et al., 2005, Heymans et al., 2016),this formulation of the second master equation has been modified already to assume that there is no biomass accumulation (in Ecopath notations  $BA_i =$ 0) to ensure a steady state and as a baseline it also assumes that there was no fishing ( $Y_i = 0$ ).

220 Combining (1) and (2) one obtains

221 
$$EE_i(Q_i - R_i - U_i) = \sum_i Q_i DC_{ii} + E_i$$
 (3)

which means that the surviving production of one group (the left-hand side of this equation) is equal to
the consumption of that group by all predators and the biomass that is leaving through emigration and
other forms of losses not otherwise explicitly represented in the model (see Figure 1).

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Figure 1. Visualisation of Equation (3), the mass-balance of a single node within the network

The data requirements for Ecopath encompass at a minimum the input of parameters  $DC_{ij}$  and  $E_i$ , as well as any three out of four variables  $P_i$ ,  $Q_i$ ,  $B_i$  and  $EE_i$  for each node in the model. The missing parameters are then estimated using the mass-balance Equations (1) and (2). This process is called balancing the Ecopath model.

233

234 For some nodes we might have information on all four parameters. However, since they have often 235 been estimated during different studies and any such parameters contain uncertainty, we often cannot 236 reach a mass-balance directly by just calculating the remaining unknown parameters (which are fewer 237 than n). In this case, we conduct another step called the model calibration. For the model calibration, 238 i.e. to find "free" parameters that ensure mass-balance, all parameters are varied according to the 239 parameter uncertainty underlying their estimates until a mass-balance is reached. For example, the 240 production of a species might have been investigated and confirmed by several studies, so the 241 parameter uncertainty is low and the bound in which it is varied for calibration might be set at 10%. On the other hand, a production estimate of a different species might not be available for the study 242

region and needs to be inferred from a different region. This would result in a higher parameter
uncertainty and hence a variation bound of 20% would be used. Rules to identify these uncertainty
bounds have been established and are called pedigrees within the Ecopath software (Christensen et al.,
2005). In practice this means that we can often find several possible parameterizations that ensure

247 mass-balance. To identify robust conclusions for a study utilising these models several/ all of these

248 parameterizations should be evaluated. We elaborate more on how we used them in this study in

section 2.5.

250

251 Equation (2) motivates a differential equation in which species biomass evolves over time as a

response to external shocks and pressures, such as harvesting. Let  $B_i$  be the biomass of a group *i*.

253 From here on out we no longer consider the total production  $(P_i)$  or consumption  $(Q_i)$ , but rather the

production  $(p_i)$  and consumption  $(q_i)$  per unit of biomass. Since (2) has the assumption of a steady

state, we can rearrange it to refer to the population change of zero as follows

256 
$$0 = -\sum_{j} q_{j} B_{j} D C_{ij} + p_{i} B_{i} - E_{i} - p_{i} B_{i} (1 - E E_{i});$$
(4)

257 or generally as change in population size over time

258 
$$\frac{dB_i}{dt} = -\sum_j q_j B_j DC_{ij} + p_i B_i - E_i - p_i B_i (1 - EE_i).$$
(5)

Furthermore, we consider that immigration  $I_i$  into the group is independent of the population sizes within the system, while emigration  $e_i$  out from the group depends on the population size of group

261 *i*, due to the effect of crowding, which means

$$E_i = e_i B_i - I_i \tag{6}$$

We denote

264 
$$M_i = p_i (1 - EE_i)$$
. (7)

which refers to the non-predation mortality. So, all together we obtain

266 
$$\frac{dB_i}{dt} = -\sum_j q_j B_j DC_{ij} + p_i B_i + I_i - (e_i + M_i) B_i .$$
(8)

267

268 In the literature, Equation (8) is often described in a more general form

269 
$$\frac{dB_i}{dt} = -\sum_j c_{ij} (B_i, B_j) + g_i \sum_j c_{ji} (B_i, B_j) + I_i - (e_i + M_i) B_i.$$
(9)

Equation (9) has the advantage that  $c_{ij}(B_i, B_j)$  can be chosen to represent bottom-up, top-down or mixed control. In this study, we investigate bottom-up control due to its inherent stability (Hearon, 1963) and consequently, assign

$$273 c_{ij}(B_i, B_j) = \beta_{ij}B_i. (10)$$

274 Since each flow from i to j needs to be consistent between the static and the dynamic approach we 275 define

$$\beta_{ij}B_i = Qb_jB_jDC_{ij}.$$
(11)

277 Consequently,  $\beta_{ij}$  is defined as

$$\beta_{ij} = \frac{B_j}{B_i} Q b_j D C_{ij}, \tag{12}$$

where all entries in formula (12) are to be taken from the model calibration results.

280 Thus, we have

281 
$$\frac{dB_i}{dt} = -\sum_j \beta_{ij} B_i + g_i \sum_j \beta_{ji} B_j + I_i - (e_i + M_i) B_i - T_i B_i.$$
(13)

where  $g_i$  is the growth efficiency, which is a ratio between the production and consumption (unitless) and  $\beta_{ij}$  represent elements of the interaction matrix (Christensen et al., 2005). In (13), we also include threats (last term in the right-hand side) with  $T_i$  being the proportion of the total biomass removed by threat *i* in Ecopath usually only considered as fishing ( $t \, km^{-2} year^{-1}$ ). Most threats remove part of a population so  $0 < T_i < 1$ , however it could also be  $-1 < T_i < 0$  in case of a threat that increases an unwanted population, for example the increase of algae,

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In the dynamic simulations, we initiate system (13) using initial values  $B_{i,t=0}$  equal to the steady-state values  $B_i$  calculated using Ecopath. Emigration and immigration are also taken from Ecopath. As the dynamics is affected by a threat, the system is moving away from the initial steady state

292 corresponding to an equilibrium in the absence of external disturbance. Due to the donor-control

- assumption, the dynamics converges to a new steady state.
- 294

#### 295 2.2 Case study system and data

296 The Great Barrier Reef (GBR) is the biggest reef system in the world. It is currently under a severe 297 threat due to global warming and the resulting bleaching. One reef within this system is Rib reef (lat:-298 18.48, long:146.88). It is located on the mid-shelf in the central Great Barrier Reef. Due to its 299 location, Rib reef is a good template for other reefs within the system. Rib reef was previously 300 investigated in a fisheries management assessment study using Ecopath (Tudman, 2001). This study 301 used an Ecosim network with 25 nodes representing functional groups. However, data in this paper is 302 simply a collection of studies and as such it is available from the original published sources at the 303 species level for most fish species, allowing for a more complex network of n = 206 nodes. This 304 makes Rib reef an ideal case study for evaluating the consequences of merging species into functional 305 groups for modelling and management. Note that in this case only fish species are identified at a 306 species level, while other functional groups (total of 15) are kept at a functional group level to reduce 307 the data requirements and the model complexity and consequently to keep computational time feasible 308 (in the absence of these limitations the model resolution could be increase to a few thousand nodes). 309 When interpreting our results here, this limitation needs to be remembered, i.e., the actual error due to 310 coarse model resolution is likely to be larger than estimated here. 311 Following Tudman (2001), we adopt input parameters  $P_i$ ,  $Q_i$ ,  $B_i$  for all i = 1, ..., n and the net 312 emigration  $E_i$  as zero (this is a common assumption that immigration is roughly equal to emigration, it is also based on the original study the data is based on by Tudman (2001)). Parameters  $DC_{ij}$  for all 313 314  $i, j = 1, \dots, n$  are downloaded directly from Fishbase (Froese and Pauly, 2017), as these parameters 315 were only given at a functional group level in Tudman (2001). Assuming that the ecosystem is 316 initially in the steady state, using the available data for  $P_i$ ,  $Q_i$ ,  $B_i$  and  $DC_{ij}$  we derive the missing 317 parameters  $EE_i$ . This is possible if at least two parameters of each node are known. In this way, we 318 fully calibrate our dynamic model, the resulting parameters for the following simulations can be found 319 in the supplementary materials (S1).

320

#### 321 2.3 Threat implementation and threat scenarios

322 We model threats as a fixed proportional reduction of biomass of a node at each time step. This is a 323 common way to represent fishing pressures in ecosystem models, and it can also represent other 324 threats such as bleaching or nitrification via reducing or increasing the biomass of a lower trophic 325 level. 326 We implement a total of six threat scenarios in this study to prototype a range of alternatives from 327 fishing on a variety of target species to coral bleaching and increased nutrition loading, choosing 328 those scenarios which represent most typical and critical threats for coral reefs. Importantly, these 329 scenarios represent threats impacting a variety of trophic levels from top predators to primary 330 producers and consequently, enable a detection of potential differences in terms of uncertainty spread 331 unevenly across trophic levels. However, it is important to keep in mind that the selected scenarios are 332 theoretical and not directly based on data. The full list of scenarios is as follows: 333 1. A reduction of the biomass of pelagic fish (fishing on a high trophic level) 334 2. A reduction of the biomass of coral trout (fishing on a high trophic level) 335 3. A reduction of the biomass of herbivores (fishing on a medium trophic level) 336 4. A reduction of the biomass of sharks (fishing on a high trophic level) 337 5. A reduction of the biomass of coral (indicative of bleaching, threat on low trophic level) 338 6. An increase of the biomass of algae (indicative of increased nutrients, threat on low trophic 339 level). 340 All of these scenarios are introduced at different intensities ranging from 10 to 90% 341 removal/introduction rate, i.e.,  $T_{\text{impacted node}} = 0.1, 0.2, \dots, 0.9$  (per year). 342 343 2.4 Merging nodes and error calculation

Merging nodes refers to pooling of biomasses of two nodes (here species or functional groups) into one node and corresponding uniting/reassignment of incoming and outgoing flows. The following describes the routine of consecutive mergers we use to evaluate the error for each of the 54 scenarios (six different threats and nine intensities per threat). In the first instance, we focus on merging nodes within each functional group from the original model (Tudman, 2001) individually, meaning that all nodes outside the functional group in focus remain at species level. Then we merge the functionalgroups consecutively to fully recreate the original 25-node model.

351 For each of the eight functional groups in the original model we run an "experiment". Each 352 experiment consists of a number of steps equal to the initial size of the functional group in terms of 353 the number of nodes. At each experiment step, we reduce the number of nodes from the functional 354 group by one from *j* to j - 1 (the calculations for all parameters after a merger can be found in S2). 355 To do so, we implement all possible mergers of two nodes within this functional group into one, total  $\frac{j!}{2!(j-2)!}$  mergers. For every merger at a given experiment step, we consecutively run all six threat 356 357 scenarios with nine intensity levels, total 54 scenarios. For each scenario, we simulate the ecosystem 358 dynamics using (13) and initial conditions from Ecopath for up to 500 time steps (which is equivalent 359 to 5 years) and compare it with the dynamics corresponding to the case without any mergers. To 360 quantify the comparison we use the total relative error as follows

361

$$\operatorname{Error} = \sqrt{\frac{\sum_{i} \frac{\sum_{t} (B_{i,t} - \hat{B}_{i,t})^{2}}{\sum_{t} B_{i,t}^{2}}}{n}},$$
(14)

363

362

where  $\hat{B}_{i,t}$  refers to the merged biomass of a node  $(B_{n-1} + B_n$  assuming that you merge the two last nodes *n* and *n* – 1) and  $B_{i,t}$  refers to the unmerged biomass of the two merged nodes added together after the simulations; *n* here is the size of the considered ecosystem model version. Threats are implemented in the merged simulations as

368 
$$\hat{T}_{n-1} = \frac{B_{n-1}T_{n-1} + B_n T_n}{B_{n-1} + B_n}$$
(15)

369 Where  $\hat{T}_{n-1}$  is the threat on the new node.

370

371 Since five years is a commonly used timeframe for management decision making, it is chosen as the372 length for the simulations.

373 Actually, due to the linearity of the model equations, for a given threat (including none) the initial (or

any given) steady state of the full system can be reproduced exactly by the reduced system (see

375 supplementary materials S2) by a choice of coefficients  $DC_{ij}$ , as well as  $B_i$ ,  $P_i$  and  $Q_i$  in the reduced 376 system. But modellers and decision makers are interested in models which are able to process a 377 variety of possible threats, hence we use a metric (14) to evaluate the "goodness" of a merger 378 averaging over all nodes in the system. Also (14) focuses on the transient path instead of just the 379 eventual steady state.

380 At each experiment step, we save the "best" merger and a corresponding network, resulting in the

381 lowest error (14). We use this "optimal" network configuration as a starting point for the next

382 experiment step. Experiments continue until the considered functional group becomes a single node.

383

#### 384 2.5 Parameter and structural uncertainty

385 In a study that would like to estimate the response of this coral reef to a given threat, the stepwise 386 aggregation that we have done so far is of not much use. Managers would be interested in the total 387 amount of uncertainty around the population size estimates that are provided with a given model. This 388 situation is what we are exploring in this section. The total amount of uncertainty in the estimates is 389 partly due to parameter uncertainty and party due to the structural uncertainty. Here, we are 390 comparing how much uncertainty we would assign depending on if we consider both the structural 391 and the parameter uncertainty or only one of them as it is often done in most previous studies 392 (Weijerman et al., 2013).

393 Parameter uncertainty can be easily estimated by simulating the system response with different 394 parameter sets. As described in the previous section 2.1 we calibrate the model with different 395 variations of the original parameters to create 10 separate parameter sets for the system. The 396 parameter sets are then each simulated over 500 time steps (5 years) for each scenario and intensity. 397 The resulting responses are compared to the response of original parameter set using the same error 398 estimates as for the structural uncertainty described in section 2.4. For these error estimates 399 (10 parameter sets \* 6 scenarios \* 9 intensities = 540 estimates) we then calculate the mean 400 and standard error.

401 Structural uncertainty here is based on errors that are calculated similar to the previous methods in 402 section 2.4. The only difference is that instead of calculating the error at each merger, we create three 403 resolutions and only compare the error between these. The three resolutions are as follows (S3): First, 404 we have the full resolution model (assumed to have no structural error) with 206 nodes. Second, we 405 have the medium resolution model identified as the optimum from the previous sections with 49 406 nodes. Third, we have the low resolution model based on the functional group in the original study by 407 Tudman. This results in 54 error estimates (6 scenarios \* 9 intensities) for each resolution which 408 are then averaged to calculate the structural uncertainty. 409 Now we can combine both of these uncertainties by creating 10 parameter sets for each resolution and 410 comparing the errors across all of them (10 parameter sets \* 6 scenarios \* 9 intensities = 411 540 estimates for each resolution). The parameter sets were identified using the pedigree 412 approach build into Ecopath and Ecoranger. In this approach each variable is assigned a level of 413 confidence (based on the data collection) followed by randomly selecting parameters within these 414 confidence intervals and rebalancing of the model (Christensen et al., 2005).

415

## 416 2.6 Regression tree analysis

417 The previous sections show that there is a large spread between the errors introduced even when 418 reducing the resolution by a single step. This spread of errors is caused by the differed species/ nodes 419 that are merged, i.e. some species represent a "good" merger others a "bad' merger. In order to make 420 better decisions on which species/ nodes to merge we need to know which characteristics of each 421 species/ node causes the error to increase. This is why we conduct this regression analysis. 422 Characteristics of interest are related to parameters of each node, i.e., biomass, production, or specific 423 to each combination of nodes in conjunction with the threat scenario, i.e., the difference in trophic 424 level between nodes merged and nodes experiencing a threat (Table 1). We use the bagged regression 425 tree analysis since input data, predictors and responses typically have different non-normal 426 distributions. A regression tree analysis is a supervised (ie. there is a response variable) machine 427 learning algorithm. At each step, the algorithm splits the samples according to one of the predictors to 428 form a more homogenous group of the response. This means that if we know the value for each 429 predictor we can follow all of the splits and predict the likely response. An extension of this is used in 430 this study by growing several trees (200) for more reliable results. In the bagged regression tree 431 analysis we grow each regression tree while utilising all predictors but subsampling data from the 432 initial sample (Prasad et al., 2006). Those trees are then combined in an ensemble to give more 433 reliable predictions. We performed an analysis with replacement i.e. each subsample is placed back 434 into the full sample after growing the tree and a new subsample is taken for the next tree. This 435 provides an opportunity for internal validation at each tree level using the mean squared error (MSE) of predictions. Compared to other methods of growing ensembles of trees, bagged trees largely 436 437 prevent overfitting. Another great feature about the bagged tree analysis is that it can calculate 438 surrogate splits. At each split, when the tree is grown, the algorithm determines the next best split 439 according to the MSE, this split is then known to be the surrogate split. Overall, this procedure 440 enables comparing the optimal split (the split chosen by the algorithm to grow the tree due to the lowest MSE) and the surrogate splits for all variables. The variable association is then measured 441 442 according to how different the MSE between the optimal and the surrogate split is. Variables that can 443 be easily replaced by their surrogate splits are less important and could be excluded. Additionally, we 444 also calculate the overall variable importance, which is the total reduction of the MSE that is due to 445 splits based on that variable (Prasad et al., 2006). This means that if the variable importance is high, 446 the splits based on that particular predictor have a large influence on the reduction of the MSE 447 achieved by the analysis. Variables with a low importance only reduce the MSE a little, so could 448 potentially be excluded from the analysis without much loss in overall performance. The variable 449 importance calculated here is relative within the analysis, i.e. the magnitude of the importance can 450 only be compared between variables of the same analysis not across different models.

451

Table 1: Predictors utilised in the bagged tress analysis

Variable name	Explanations

Threat distance	The difference in trophic level* between the threat and the average of the			
	merged groups $(TL_{\text{threat}} - \frac{TL_1 - TL_2}{2})$			
Node distance	The absolute difference in trophic (TL*) level between the two groups to be			
	merged $( TL_1 - TL_2 )$			
Predator overlap	The proportion of the outflows that are the same in nodes to be merged			
	(Outflows that are the same) Total number of outflows			
Food overlap	The proportion of the inflows that are the same in nodes to be merged			
	(Inflows that are the same) Total number of inflows			
Biomass ratio	Ratio of the node sizes between two merged nodes $\left(\frac{B_{1,0}}{B_{2,0}}\right)^{**}$			
Production ratio	Ratio of the total production between two merged nodes $(\frac{P_{1,0}}{P_{2,0}})^{**}$			
Consumption	Ratio of the total consumption between two merged nodes $\left(\frac{Q_{1,0}}{Q_{2,0}}\right)^{**}$			
ratio	~2,0			

452 \*Trophic levels in Ecopath are continuous variables and based directly on the trophic levels of the

453 species consumed. For more information Christensen et al. (2005) section 6.4.4

\*\*Considering that the designation of node 1 and 2 for these calculations is arbitrary, we allocate node
1 and 2 so that the ratios calculated are between zero and one. This is achieved by allocating the larger

456 value to node 1.

457

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458 3 Results
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459

460 *3.1* Error due to model coarse-graining

461 The error estimates after merging show a clear pattern, the error estimates start low then first slowly

then rapidly increase. However we are also interested in differentiating between the maximum and

463 minimum error at each merger. Since this represents the variation of errors that can occur depending

464 on if we merge two similar or two very different species or nodes. For most scenarios, the minimum

465 error is rather small when only few nodes are merged, however after a "tipping point" when a certain

466 "critical mass" of nodes is merged, it increases rapidly. The maximum error on the other hand starts 467 relatively high and remains mostly stable with just a small increase at the final mergers. This also 468 means that we can reduce the error when only merging a few species, however only if we are merging 469 the correct species. Finally, the spread of errors across the  $\frac{i!}{2!(i-2)!}$  possible networks at each merger is 470 not even, but rather clustered. This clustering can aid the identification of the nodes (here species) that 471 should or should not be merged to avoid large losses of accuracy.

472 Figures 2 and 3 illustrate the typical patterns we observed in these experiments. Figure 2 depicts

473 errors in one (of six) threat scenario with fixed intensity (0.5) for all eight functional groups. Figure 3

474 illustrates the effects of all six threat scenarios with fixed intensity (0.5) on one selected functional

475 group (lutjanids). Both figures represents the tendencies concerning the minimum and maximum

476 errors described above from two different perspectives. The graphs of all functional groups across all

477 six scenarios and intensities can be found in the supplementary materials (S4). One feature that can be

478 observed in both figures and all panels is that there are two separate "clouds" of points. One is worse

479 in terms of errors than the other. This cloud of bad mergers is made up of a few species that whenever

they are added to the remainder spike the error. The regression analysis later in this section will

481 outline characteristics that can help determine these species in the hope to avoid them.



483

Figure 2. Example of results: Error estimates for all eight functional groups under threat scenario 1)
in which the biomass of pelagic fish is reduced with intensity 0.5. Panel A compares functional
groups lutjanids, serranids, corallivores, lethrinids, small and large planktivores. Panel B shows
herbivores and panel C the functional group other demersals. Each point represents one possible
merger of two nodes originating from the model identified with the lowest error in the previous
mergers.



492 Figure 3. Error estimates for threat scenario 1) to 6) of intensity 0.5 for lutjanids. Each point
493 represents one possible merger of two nodes originating from the model identified with the lowest
494 error in the previous amount of mergers.

495

491

496 *3.2 Parameter versus structural uncertainty* 

497 To compare the balance of parameter and structural uncertainty we are looking at the combined 498 uncertainty (Fig.4). Since 205 nodes is the highest resolution considered here (reference point for the 499 structural uncertainty), it only includes parameter uncertainty with the structural uncertainty being 500 zero (according to our assumption). The 49 and the 22 node model both include structural and 501 parameter uncertainty. We found that the 49 node model was the optimal model in the sense that the 502 overall (structural and parameter) was the lowest. This supports the hypothesis that there is an optimal 503 resolution even when taking into account the parameter uncertainty.



505 Figure 4. Average error estimates with standard errors for the different resolutions.

506

504

#### 507 3.3 Variable Importance

508 The bagged trees analysis shows that we can explain most of the variation in the error of a particular merger when considering how similar in the predictor variables the two nodes are ( $R^2 = 0.89$ ). 509 510 The variable importance shows that the most effective predictors to determine a good merger are the 511 biomass ratio (~ node size) and the consumption ratio (~total amount of inflow into the node) of the species (Fig. 5). The more similar (i.e. ratio of 1) biomass and consumption of the nodes are the lower 512 513 the error, meaning the better the merger. Another variable of medium importance is the difference in 514 trophic level between the threat scenario and the merged groups (Fig.5). In this case, the smaller the 515 difference between the trophic level of both nodes the smaller the error, causing a better merger. It is 516 interesting that the similarities in parental or child nodes between nodes to be merged (i.e. similarities 517 in predators and food sources for the merged species) are of low value to determine the direction of 518 merging. In fact, predator overlap is largely associated with all the other predictors (Fig.6), and hence it could be removed from the analysis without any loss of predictive power ( $R^2 = 0.8$ ). 519 520







525



526

Surrogate predictor

527 Figure 6: Association between predictors in the tree

528

# 529 4 Conclusions and Discussion

531 This study provides insights into structural uncertainty and more specifically into what role the 532 resolution plays in complex network-based models. Overall, the study gives a good indication of how 533 structural uncertainty in form of the trophic resolution could be better integrated into the process of 534 constructing the models based on complex networks. Here we considered an Ecopath model as a 535 prominent example in ecological modelling. We found that different levels of model resolution can 536 change the error in estimating model outcomes in response to exogenous shocks. While higher 537 resolutions always reduce the structural uncertainty this might not be the best resolution overall. 538 Besides the computational capacity needed for high resolution models, the overall (parameter and 539 structural) uncertainty is lowest at a medium resolution. This resolution can be considered as an 540 optimal resolution and can be found by merging species with the most similar parameters for biomass 541 and total consumption. Note that there is no direct cut-off that can be applied here. The acceptable 542 ratio between biomasses of both nodes depends on species and total network resolution. The study 543 confirms that the distance in trophic level between the merged nodes and the threat can be of importance. Our results highlight that the common practice of putting high importance on the ratios of 544 545 the size of the merged nodes and their biomasses, rather than on the rest of the network the nodes are 546 connected to, and on the directions of in- and outflows may be warranted.

547

548 A result that holds true across all considered functional groups, independently from the number of 549 species or threats is that the minimum error grows with an increasing slope when the model resolution 550 becomes coarser (i.e., with increasing the number of mergers). This means that at a medium resolution 551 level the error is substantially lower than the error at the lowest resolution level (i.e., when a complete 552 merger of all species into one group is achieved). This is not surprising since some species have 553 common ecology, and hence they are even sometimes called "redundant species", while others differ 554 dramatically in size, food source or predator protection. Redundancy refers to different species full-555 filling similar ecological roles (Naeem, 1998), hence not much difference can be found if these 556 species are considered as one group in the analysis. While the existence of functional redundancy is still debated (Hoey and Bellwood, 2009), this analysis seems to support the hypothesis. Similar 557

analysis on different systems other than coral reefs might be useful to explore this concept further.
The shape of the relationship between the degree of model coarse-graining and the model accuracy
introduces a notion of an optimal grouping of species in terms of structural uncertainty and
computational requirements.

562

563 This study supports the previous assumption of an opposite hump shape or seesaw between structural 564 and parameter uncertainty (Costanza and Sklar, 1985, Håkanson, 1995, Jester, 1977). When the 565 structural uncertainty is reduced (according to our assumptions entirely removed) and only parameter uncertainty is considered (the 205 node resolution) then we have the highest overall uncertainty. The 566 567 medium resolution model produced here with 49 nodes shows the lowest overall uncertainty, i.e. while the structural uncertainty is increased the lower amount of parameters resulted in a much lower 568 569 parameter uncertainty. On the other hand, once the resolution is reduced too much (22 nodes), the 570 structural uncertainty is so high that even combined with the now low parameter uncertainty, the 571 overall uncertainty is increased again. This in conjunction with the shape of the uncertainty estimates 572 across different numbers of mergers supports the hypothesis that an optimal resolution exists. This is 573 not just the optimal across structural uncertainty and computing power required, but also parameter 574 uncertainty. It should be considered here that we only considered errors introduced through the 575 resolution, not other sources such as the formulation of equation. However, the introduction of such 576 variations and their errors would generally only increase the structural uncertainty, not decrease it, 577 consequently the hump shape would be more and not less pronounced. Another interesting finding 578 here is that the species grouped in this optimal resolution model (here 49 nodes) are consistent for all 579 of the threat scenarios and intensities. This is especially important when the management questions 580 underlying the model are concerned with multiple threats.

581

When it comes to the practical implementation of these results, we would like to caution that the
errors calculated in this study should not be taken as an accurate measure of the true error. The error
calculated here is only based on resolution and due to the reference system itself having a reduced

resolution (lower trophic levels are grouped substantially), it represents a minimum error that we would have to expect based on the merging of the fish species into functional groups. The error here is supposed to guide decisions in reducing the overall error and highlight the importance of getting this component "right". The next few paragraphs will outline how we could more practically use the results gathered in this study.

590

591 Common practice has often focused mainly on grouping together nodes with similar connections 592 (Cale Jr and Odell, 1980, Fulton, 2001, Gardner and Ashby, 1970, O'Neill, 1975, Wiegert, 1975). This 593 would be similar to the characteristic of predator and diet overlap in this study. However, this study 594 shows that the actual similarities of the predators is not very influential in terms of the aggregation of 595 species. Instead we found that similar abundances (here biomass) are the most important. One 596 example of considering connections over abundance, is Tudman (2001) who groups all herbivores 597 together irrespective of the large differences in their biomasses ranging from 0.01 to over 10  $t \, km^{-2} y ear^{-1}$ . On the other hand, it has been recognized that for some very rare species it is better 598 to exclude them from the model than to merge with a species with another group (Fulton, 2001). The 599 600 results presented here have to be taken with some caution, however, since the data the analysis is 601 based on already assumes some similarity between then species merged, i.e. due to limitations related 602 to computing time the method does not allow a shark and a goby to be merged purely because they 603 have a similar biomass in the system. This restriction here was due to technical reasons mainly, 604 however, it also represents another commonly applied guideline: "do not aggregate serially linked 605 groups" (Fulton et al., 2003), i.e., expert knowledge should be used to provide the initial coarse 606 groupings.

607

In the literature, it is often suggested that Ecopath models should have as high as possible resolution
of the foodweb nodes that are of special interest to the question asked (Heymans et al., 2016,
Hollowed et al., 2000, Christensen et al., 2005). For example, if we are investigating fishing, we
should differentiate fish groups more explicitly than other parts of the foodweb such as, for example,

612 algae. While this is common practice and might suit the manager's needs, it has been pointed out that 613 this method could cause biased results (Fulton et al., 2003). Our study found some support to this 614 guideline, i.e., as we obtained that the difference between the trophic level of the threat and the 615 merged group had some importance, however, it needs to be recognised that it was lower than that of 616 the biomass and production. Furthermore, the optimal resolution, and specific species to group in the 617 medium sized model did not change in all of our threat scenarios. Since the threats that were used here 618 can represent anything from bleaching to high trophic level fishing, the results seem to indicate that it 619 is not important which question we are trying to answer when deciding on the species grouped within 620 each node. This contradicts some previous advice (Heymans et al., 2016) and should be further 621 investigated, especially, since it is often used as a justification to represent lower trophic levels in 622 massive groups that can represent hundreds or even thousands of species (Tudman, 2001).

623

624 Overall, when constructing a new network to underlay a foodweb model we should first and foremost 625 consider the biomass of species being merged. If a large difference exist we should rather exclude 626 than merge that respective species. Second, we should consider the amount that each species 627 consumes. Similar to biomass, we need to only merge species that are very similar in the amount they 628 consume, per biomass unit and overall. Only after these characteristics are considered we should 629 evaluate if the purpose of the individual study justifies a higher resolution at certain points within the 630 network. Please not we would recommend to only increase resolution close to points of interest rather 631 than decrease the resolution in other parts of the foodweb.

632

The future use of this study is twofold. The study can have a direct use for coral reef models
constructed in the future. The optimal groupings found here as well as the total amount of uncertainty
found can be utilised for any model of this system. However, the results from this study can reach
further since it provides information on how to aggregate nodes in any network model independent of
its use. In conclusion, this study is a good foundation for further investigation and the better
integration of structural uncertainty in ecosystem models, but also other network based models. As

639	long as merging nodes that are not serially linked, the most important determinant of uncertainty is the
640	size ratio of the merged nodes and their total outflow. This can give guidance to future models to
641	manage uncertainty caused by a coarser resolution which modellers have to accept in return for
642	feasible computing resources.
643	
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645	
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