

Dynamic Forecasting of Travel Demand, Residential Location and Land Development

Anas, A. and Duann, L.S.

**IIASA Collaborative Paper
September 1983**



Anas, A. and Duann, L.S. (1983) Dynamic Forecasting of Travel Demand, Residential Location and Land Development. IIASA Collaborative Paper. IIASA, Laxenburg, Austria, CP-83-045 Copyright © September 1983 by the author(s). <http://pure.iiasa.ac.at/2337/> All rights reserved. Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage. All copies must bear this notice and the full citation on the first page. For other purposes, to republish, to post on servers or to redistribute to lists, permission must be sought by contacting repository@iiasa.ac.at

NOT FOR QUOTATION
WITHOUT PERMISSION
OF THE AUTHOR

DYNAMIC FORECASTING OF TRAVEL
DEMAND, RESIDENTIAL LOCATION
AND LAND DEVELOPMENT

Alex Anas*
Liang Shyong Duann**

September, 1983
CP-83-45

* Northwestern University,
Evanston, Illinois, U.S.A. 60201

** National Cheng Kung University,
Tainan, Taiwan, R.O.C.

Contributions to the Metropolitan Study: 1

This paper was presented at an IIASA Seminar on July 20, 1983 and was prepared for the Eighth Pacific Regional Science Conference, August 17-19, 1983 in Tokyo, Japan.

Collaborative Papers report work which has not been performed solely at the International Institute for Applied Systems Analysis and which has received only limited review. Views or opinions expressed herein do not necessarily represent those of the Institute, its National Member Organizations, or other organizations supporting the work.

INTERNATIONAL INSTITUTE FOR APPLIED SYSTEMS ANALYSIS
A-2361 Laxenburg, Austria

FOREWORD

The project "Nested Dynamics of Metropolitan Processes and Policies" was initiated by the Regional & Urban Development Group in 1982, and the work on this collaborative study started in 1983.

The series "Contributions to the Metropolitan Study" is a means of conveying information between the collaborators in the network of the project.

This paper is the first of these contributions and presents the CATLAS-model (The Chicago Area Transportation-Land Use Analysis System) which is a dynamic large-scale urban simulation model for forecasting the effect of transportation system changes on travel mode choices, residential location, housing values and housing stock adjustment.

CATLAS has been applied to cost-benefit analysis of several subway projects proposed for the southwest side of Chicago. Currently, the model is being implemented to analyze the transportation system in Stockholm, and plans exist to extend this type of cross-city implementation to several other regions in the project.

Börje Johansson
Acting Leader
Regional & Urban Development Group

September, 1983

CONTENTS

1.	INTRODUCTION AND SUMMARY	1
2.	THE STRUCTURE AND PROPERTIES OF CATLAS	6
2.1.	Overall Recursive-Dynamic Structure	6
2.2.	The Demand Submodel	10
2.3.	The Occupancy or Existing Housing Supply Submodel	13
2.4.	The Housing Stock Adjustment Submodels	14
2.5.	Market Clearing Equilibrium at Each Year	16
2.6.	Steady State Behavior of CATLAS	17
3.	EMPIRICAL ESTIMATION	18
3.1.	Data Sampling and Estimation	18
3.2.	Estimation of Demand Submodels	18
3.3.	Estimation of Occupancy and Stock Adjustment Submodels	19
4.	SIMULATIONS AND POLICY IMPLICATIONS	20
4.1.	Simulation Data and Assumptions	20
4.2.	Simulation Results and Transit Finance Implications	21
4.2.1.	Static Simulations	22
4.2.2.	Dynamic Simulations	23
4.3.	Caveats and Conclusions	26
	REFERENCES	28
	FIGURES 1-5	30-34
	TABLES 1-11	35-45

1. INTRODUCTION AND SUMMARY

It is well known that following a transportation improvement (or more generally any infrastructure investment), the prices of real estate near the improvement will increase due to the increase in accessibility and the quality of service and the decrease in travel time.

However, there is a gap in our knowledge of how to estimate property value increases caused by a public investment. Urban economists have developed simplified mathematical models of long run equilibrium in the urban land and real estate markets. These models provide a sound theoretical basis for policy analysis but are not detailed enough for actual empirical application. On the other hand, transportation planners place a strong emphasis on empirically estimable models, but these models focus only on the travel-related attributes and the demand for travel without properly taking into account the interactions between transportation, land use and property values through the markets for land and buildings.

There is a need for a theoretically sound and empirically estimable dynamic model which can satisfy the transportation planner's travel demand forecasting requirements while at the same time predicting the operation of real estate markets and the adjustment in property values due to new or improved transportation systems.

The Chicago Area Transportation/Land Use Analysis System (CATLAS) is such a model which synthesizes our knowledge of "location rent analysis" from urban economics with our knowledge of "travel demand analysis" from transportation planning. It is a dynamic model which simulates the market in recursive periods of one year in length, and for a geographic grid system of 1690 zones covering the Chicago metropolitan area. The distribution of jobs among the zones and the

characteristics of the transportation system are assumed to be known in every year. CATLAS generates people's choices of travel mode (automobile, commuter rail, rail rapid transit, bus, and "other") and their choice of residential location. Transportation improvements or changes in parking fees, gas prices, transit fares, etc. change people's decisions of where they will live and how they will commute there, given where they work. This is a demand side process and it is assumed that people make their decisions rationally by choosing the most attractive (or utility maximizing) of the travel-location options available. Because people are different, their choices differ as well. On the supply side CATLAS simulates profit-maximizing behavior on the part of housing owners. Three decisions are simulated. For the owner of an existing dwelling unit the decision (which recurs every year) is whether to withdraw the dwelling from the market and keep it vacant or whether to supply it to the market by selling it or renting it out. For the owner of vacant land, the decision is whether to build new housing on that land or whether to postpone that decision to the next year. The owner of an old dwelling or building faces a similar decision. If he perceives that demolishing the building and selling the land is more profitable than continuing to rent it out he will demolish and sell. Otherwise the decision will be postponed to the next year. Building new dwellings and demolishing old ones are major decisions that take time to implement. In CATLAS it is assumed that there is a one year lag: the number of new dwellings constructed and old ones demolished in a given year depend on decisions based on last year's conditions. The demand and supply side of a real estate market must be in some sort of balance. This balance comes about as prices and rents adjust in each geographic zone. In CATLAS it is assumed that the demand for occupancy in a zone in a given year equals the number of dwellings supplied for occupancy in that year. Prices and rents adjust within

every year to make this possible. Such a clearing of the market is a "temporary equilibrium". Changes in outside influences such as travel characteristics or job locations will shift the system to a new "temporary equilibrium" next year.

A precise list of the simulation output of the current version of CATLAS is as follows:

- (1) the average housing rent in each geographic zone in each year,
- (2) the number of vacant dwellings in each geographic zone in each year,
- (3) the number of commuters choosing each travel mode by geographic zone of residence and employment,
- (4) the number of new dwellings built by zone in each year,
- (5) the number of old dwellings demolished by zone in each year,
- (6) the price of the vacant land in each zone in each year,
- (7) the amount of vacant land in each zone in each year,
- (8) the number of dwellings in each zone in each year,
- (9) the change in aggregate housing and land rent (or producer surplus) by year and zone.

There are five lines of literature that are relevant to the subject matter of CATLAS. These are: (a) the theoretical literature on location and land use in urban economics; (b) empirical studies of the impact of transportation improvements on property values; (c) travel mode and location choice models, (d) economic urban simulation models and (e) noneconomic urban simulation models. The main developments and bibliographic references in each of these areas are briefly reviewed.

The theoretical literature in urban economics is based on the early works of Mohring and Harwitz (1962), Alonso (1964), Mills (1967), Muth (1969), Beckmann (1969). The basic argument of this literature is that part of consumers' savings in travel cost (and travel time) are capitalized into land

and property values. Although travel costs are explicitly treated in this literature, travel time savings are not considered explicitly, but it is understood that the same results apply to travel times as well. In theoretical urban economic models such as those by Wheaton (1974) and Arnott and Stiglitz (1981) the interest is in the relationship between uniform improvements in unit transportation costs and the aggregate value of land. Even in such cases the relationship between aggregate rents and travel costs is complicated and does not yield any simple quantitative rules of thumb.

In the empirical literature the focus is not on whether aggregate rent will increase or fall, or on how to measure benefits, but rather on how to measure the magnitude of changes in land or other real estate values following the transportation improvement. These studies generally agree that the improvement would increase values nearby. The earlier studies are descriptive. These include the impacts of rapid transit (Spengler, 1930; Davis, 1965), expressways (Adkins, 1959; Lemly, 1959; Golden, 1968), interchange development (Ashley, 1965) and interstate highways (Wootan and Haning, 1960) on property values. The more recent work uses statistical analysis. Examples of these are the study of the Lindenwold-Camden-Philadelphia line by Mudge (1972) and Boyce et al. (1972), of a rapid transit line in Toronto by Dewees (1976) and of the Washington, D.C. METRO by Lerman et al. (1977). The findings of these studies hinge on the judicious application of multivariate regression analysis making substantial improvement on the descriptive studies.

A major shortcoming of all these studies is that they are exclusively focused on specific transportation facilities. Each tends to deal with a single or several selected facilities rather than attempt a region-wide or city-wide cross-sectional study of the effects of multimodal transportation systems. As a result, their findings are difficult to generalize and are biased by the

peculiar conditions that may surround the studied facilities.

The power of mode choice analyse has increased since the contributions of (McFadden (1973) and Domencich and McFadden (1975)). Transportation planners can now analyze mode choices by drawing on the standard techniques of multinomial logit, nested logit and multinomial probit models. Logit and nested logit models have also been applied to the choice of residential location and the joint choice of travel mode and residential location by Quigley (1976), Lerman (1977), McFadden (1978) and Anas (1981). The resulting models predict choices of location and travel mode but not the aggregate behavior of housing prices in response to travel improvements.

There are two economic urban simulation models which have been empirically applied to policy questions concerning the housing market. These are the Urban Institute Model (UIM) (de Leeuw and Struyk, 1975) and the National Bureau of Economic Research (NBER) (Ingram et al., 1973) model. The former model is based on a well developed theory of housing market behavior and includes a number of innovative ideas. Weaknesses of the model are (1) its highly aggregated form which makes it inapplicable to situations requiring detail, (2) the fact that it can be statistically estimated only with rather crude aggregated data and (3) that the numerical algorithm it uses may not always be able to find a solution.

The NBER model is the most comprehensive urban simulation model developed. Unfortunately, it is not a very workable model because it cannot be consistently estimated since all of the data it requires is not available for the same metropolitan area. Some of its submodels are descriptive in nature and are not rooted in theory. The assignment of households to housing units follows a disequilibrium process rather than being rooted in well established market clearing procedures.

CATLAS is an economic urban simulation model primarily intended for testing

the effects of transportation policies on housing and land values, on residential land development and on mode choice patterns. It can deal with any transportation policy which changes travel times and costs in any of several travel modes. CATLAS can be estimated in its entirety using widely available data and rigorous econometric procedures. CATLAS has well behaved solution properties and computes equilibrium allocations of households to dwellings.

CATLAS can be viewed as a synthesis of the land rent and land use models developed by urban economists following Alonso (1964) with the travel and location choice models developed by transportation planners following McFadden (1973). Thus, it is a tool for simultaneously doing travel demand and land rent analysis. Using CATLAS one can evaluate the direct benefits to the users of the transportation system, the indirect benefits to nonusers, and the fiscal benefits due to changes in rent. Thus, CATLAS provides an alternative to the noneconomic urban simulation models which do not have such capabilities and which are not estimated using rigorous econometric techniques, but by means of ad hoc and sometimes partly subjective goodness-of-fit procedures.

2. THE STRUCTURE AND PROPERTIES OF CATLAS

2.1 Overall Recursive-Dynamic Structure

CATLAS consists of a number of equations to be solved simultaneously for each year in a simulation, while some of the variables entering these equations are adjusted recursively by being linked to the solution of the previous time period. Using general functional notation, the model's equations can be written as follows, where $t = 1 \dots T$ denotes the simulation year, $i = 1 \dots I$ the residential zones covering the metropolitan area and $h = 1 \dots H$ the categories of employment location (or zones of employment) and $m = 1 \dots M_i$ the number of modes available in zone i :

$$\sum_{h=1}^H N_h^t \sum_{m=1}^{M_i} \delta_i p_{im}^h (\bar{R}^t, \bar{X}^{Dt}, \bar{Y}_h^t, \bar{\alpha}_h) = S_i^t Q_i^e(R_i^t, \bar{X}_i^{St}, \bar{\beta}); i = 1 \dots I, \quad (1)$$

$$S_i^t = S_i^{t-1} + C_i^{t-1} - D_i^{t-1}; i = 1 \dots I, \quad (2)$$

$$C_i^{t-1} = \left(\frac{L_i^{t-1}}{g_i} \right) Q_i^c(R_{is}^{t-1}, s = 1 \dots M; \bar{X}^{St-1}, r, \bar{\gamma}); i = 1 \dots I, \quad (3)$$

$$D_i^{t-1} = O_i^{t-1} Q_i^d(R_{is}^{t-1}, s = a_i^{t-1} \dots M; \bar{X}^{St-1}, r, \bar{\delta}); i = 1 \dots I, \quad (4)$$

$$L_i^{t-1} = L_i^{t-2} - g_i C_i^{t-2} + g_i D_i^{t-2}; i = 1 \dots I, \quad (5)$$

$$O_i^{t-1} = O_i^{t-2} - D_i^{t-2} + A_i^{t-2}; i = 1 \dots I, \quad (6)$$

$$R_{is}^{t-1} = R_i^{t-1} + \theta(s - \{X_{i1}^{Dt-1} = X_{i1}^{St-1}\}); i = 1 \dots I, \quad (7)$$

$$\bar{X}_i^{Dt} = f_1(\bar{X}_i^{Dt-1}); i = 1 \dots I, \quad (8)$$

$$\bar{X}_i^{St} = f_2(\bar{X}_i^{St-1}); i = 1 \dots I. \quad (9)$$

The equations in (1) are the crux of the model and are solved simultaneously for every simulation year t to obtain the values of the rent vector $\bar{R}^t = [R_1^t, R_2^t, \dots, R_I^t]$ where R_i^t is the average rent of the housing units in zone i during year t . This average zonal rent is defined as

$R_i^t = f_i^t r_i^t + (1 - f_i^t) V_i^t/10$, where f_i^t is the proportion of the zone's occupied dwellings which are renter occupied in year t , r_i^t the annual rental and V_i^t the

value of the owner occupied dwellings. Values are divided by ten to annualize them following a rule of thumb due to Shelton (1968) widely used by urban economists. N_h^t is the number of commuters employed in location h at time t , δ_i is zone i 's ratio of households to commuters and S_i^t the number of housing units in zone i at time t . The functions $P_{im}^h(\cdot)$ and $Q_i^e(\cdot)$ are the demand and supply side choice functions. $P_{im}^h(\cdot)$ represents a commuter's choice of residential zone i and travel mode m for the journey from work to home as a function of the rents, \bar{R}^t , of all the residential zones, a vector \bar{X}^{Dt} describing characteristics of the residential zones, another vector \bar{Y}_h^t describing travel related characteristics of the zones for travel mode m and employment location h and a vector $\bar{\alpha}_h$ of coefficients to be estimated. $P_{im}^h(\cdot)$ is the average probability with which a commuter employed at h will choose zone i and mode m , or the expected proportion of commuters employed in h choosing zone i and mode m . The function $Q_i^e(\cdot)$ is the probability that the average dwelling in zone i will be offered for rent by the owner given the ongoing average rent R_i^t , a vector of the zone's characteristics, \bar{X}_i^{St} , relevant to the supply side, and $\bar{\beta}$ a vector of coefficients to be estimated. $Q_i^e(\cdot)$ is also the expected proportion of the available dwellings S_i^t which will be offered for rent, $1 - Q_i^e(\cdot)$ being the expected proportion to remain vacant. Equation (1) states that expected demand equals expected supply in each of the $i = 1 \dots I$ zones and in each simulation year $t = 1 \dots T$. It has been proven in Anas (1982) that given N_h^t , δ_i , \bar{X}^{Dt} , \bar{Y}_h^t , S_i^t , \bar{X}_i^{St} , $\bar{\alpha}_h$ and $\bar{\beta}$ the system of equations can be solved for a unique and stable equilibrium rent vector \bar{R}^t which clears the market in that year t . The second set of equations states that the number of dwellings in year $t-1$ increases by the expected number of new dwellings constructed, C_i^t , less the number of old dwellings demolished, D_i^t during that year. Equations (3) give the expected number of

built in year $t-1$ in zone i : L_i^{t-1} is the quantity of vacant land available in zone i and g_i the amount of land per dwelling allowable in zone i due to zoning regulations, (L_i^{t-1}/g_i) being the potential new dwellings that can be accommodated in zone i . $Q_i^C(\cdot)$ is the expected proportion of these potential dwellings that will be built in year $t-1$. This function is derived from the developer's profitability decision. It depends on the stream of annual rents per dwelling expected to accrue over the dwelling's lifetime M , on the vector of supply side characteristics \bar{X}^{St-1} , the market interest rate r and $\bar{\gamma}$, a vector of coefficients to be estimated. Equations (4) estimate the number of demolitions, D_i^{t-1} , in year $t-1$. This is the number of old (over thirty years) dwellings, O_i^{t-1} , eligible for demolition multiplied by the expected proportion to be demolished $Q_i^d(\cdot)$. This expected proportion is a function of the stream of annual rentals that can be obtained from the average old dwelling in zone i over its remaining lifetime, the vector of supply side characteristics \bar{X}^{St-1} , the interest rate r and a vector of coefficients to be estimated, $\bar{\delta}$. The age of the average old dwelling in the zone is a_i^{t-1} . Equations (5) update the amount of vacant land in a zone by accounting for land taken up by new constructions and land released by demolitions. Equations (6) adjust the number of dwellings eligible for demolition by adding, A_i^{t-2} the number of dwellings aging into the over thirty years category and thus becoming eligible for demolition. A_i^{t-2} is calculated from a simple cohort-survival model for housing for each zone. Equation (7) shows how the average rent of dwellings s years old can be computed by making a linear adjustment to the average rent of zone i . This is done by estimating a depreciation coefficient θ and multiplying this by $s - x_{i1}^{Dt-1}$ or $s - x_{i1}^{St-1}$ where $x_{i1}^{Dt-1} = x_{i1}^{St-1}$ is the age of the average dwelling in zone i at time $t-1$ (in other words, the age of the average dwelling may be considered to be the first element in the vectors

\bar{X}^{Dt-1} and \bar{X}^{St-1}). Finally equations (8) and (9) adjust the values of some of the variables in these vectors. The changes in the age of the average dwelling is one of these adjustments.

2.2 The Demand Submodel

The choice problem of a commuter with a given workplace h , is to determine the geographic zone of residence location i , the mode of commuting m , and the exact dwelling k within zone i .

The attractiveness (or utility) of an alternative (i, m, k) for the average commuter employed in workplace h is given as,

$$\hat{U}_{imk}^h = U_i^h + U_{im}^h + U_{imk}^h + \epsilon_{imk}^h \quad (10)$$

This equation states that attractiveness consists of four additively separable parts. The first part, U_i^h measures the part of attractiveness due to characteristics which vary by zone. The second part U_{im}^h is the part of attractiveness due to characteristics which vary by zone and mode of commuting. The third part U_{imk}^h includes the part of attractiveness which varies by zone i , mode m and dwelling k . In many cases when these characteristics are not observed for each dwelling but are known in the data as zone averages they will be included in U_i^h or combined with other characteristics in U_{im}^h . The fourth part of attractiveness ϵ_{imk}^h is a random variable due to unknown (unobserved) characteristics including things like personal preference differences, random effects and errors in measurement. The probability that a commuter employed in h will choose (i, m, k) is given as,

$$P_{imk}^h = \text{Prob.} [\hat{U}_{imk}^h > \hat{U}_{jns}^h, \forall (j, n, s) \neq (i, m, k)] \quad (11)$$

The specific form of (11) depends on what is assumed about the random terms, ε_{imk}^h . We follow the assumption that these error terms are correlated within zones (i.e. for different m and k within each i) but uncorrelated for different zones. Under this assumption the probability P_{imk}^h can be computed as the computationally tractable nested multinomial logit model. First, because utility is additively separable we can write the probability as,

$$P_{imk}^h = P_i^h \cdot P_{m|i}^h \cdot P_{k|im}^h \quad (12)$$

Here $P_{k|im}^h$ is the conditional probability that the commuter will choose dwelling k , given that zone i and mode m have been chosen. $P_{m|i}^h$ is the conditional probability that the commuter will choose mode m given that zone i has been chosen and P_i^h is the marginal probability that zone i will be chosen. These probabilities are of the form

$$P_{k|im}^h = 1/S_i, \quad (13)$$

$$P_{m|i}^h = \text{EXP}(U_{im}^h) / \sum_{n=1}^{M_i} \text{EXP}(U_{in}^h), \quad (14)$$

$$P_i^h = S_i^{\alpha_0^h} \text{EXP}[U_i^h + (1 - \alpha_1^h) I_i^h] / \sum_{j=1}^I S_j^{\alpha_0^h} \text{EXP}[U_j^h + (1 - \alpha_1^h) I_j^h], \quad (15)$$

$$I_j^h = \text{LOG} \sum_{m=1}^{M_j} \text{EXP}(U_{jm}^h), \quad (16)$$

$$U_{jm}^h = \alpha_2^h \text{LOG}(R_j + C_{jm}^h) + \frac{1}{\alpha_3^h} Y_{jm}^h, \alpha_2^h < 0, \quad (17)$$

$$U_j^h = \frac{1}{\alpha_4^h} \bar{X}_j^D. \quad (18)$$

Equation (13) states that dwellings within a zone are equally likely to be chosen (because the data is not detailed enough to discriminate among them). Equation (14) states that the probability of choosing a mode m given the choice of zone is a multinomial logit model and thus depends on the relative attractiveness of the modes keeping zone characteristics constant.

Equation (15) is the marginal zone choice probability and this is a nested logit model adjusted for zone size measured by the number of dwellings. The zone choice probability is a function of the zone's attractiveness plus a combined measure of the attractiveness measures of the modes in that zone. The combined measure of the zone's mode attractiveness (called an "inclusive value") is given by equation (16) and is in fact the logarithm of the denominator of the mode choice model (14). Equation (17) states that the attractiveness of a zone-mode combination is a function of the average zone rent plus average travel cost for the mode and also a function of other zone characteristics, Y_{jm}^h , which include travel time, distances to stations etc. (or the logarithms of such variables).

Multiplying (14) and (15) we can compute a joint probability P_{im}^h . This is the probability of choosing zone i and mode m given workplace h . Since all the zones are interconnected through the logit models a change in the attractiveness of a zone or the modes in that zone will have repercussions in the demand of all

the other zones.

2.3 The Occupancy or Existing Housing Supply Submodel

This submodel explains the choices of the owners of dwellings in the short run. The owner of an existing dwelling must decide whether to offer the dwelling for rent in that year or whether to withhold it until next year. The decision is based on profitability. Suppose that the average dwelling is offered for rent. Then it will yield a profit

$$\Pi_{i1} = R_i - M_{i1} + \epsilon_{i1} \quad (19)$$

If it is kept vacant the loss is

$$\Pi_{i2} = -M_{i2} + \epsilon_{i2} \quad (20)$$

Here R_i is the average rent in zone i , M_{i1} is the cost of maintaining the average dwelling if it is occupied and M_{i2} the cost of maintaining the average dwelling if it is vacant, and ϵ_{i1} , ϵ_{i2} are random measurement errors due to unobserved variables. Maintenance costs for occupied dwellings will be higher if the costs of repairs due to occupants exceed the costs of vandalism, neglect etc. for vacant dwellings. These will depend on the type and location of the dwelling's neighborhood. The differential profit is,

$$\Pi_{i1} - \Pi_{i2} = R_i - (M_{i1} - M_{i2}) + \epsilon_{i1} - \epsilon_{i2} \quad (21)$$

The differential maintenance cost is not directly available in the data but since it depends on neighborhood (i.e. zone) characteristics it can be made a function of these characteristics. Thus

$$(M_{i1} - M_{i2}) = \sum_{n=1}^N \beta_n X_{in}^S, \quad (22)$$

where there are $n = 1 \dots N$ supply side zone characteristics and the β_n 's are the coefficients to be estimated. The probability that the average dwelling will be offered for rent can now be computed as,

$$Q_i^e = \text{Prob.}[\pi_{i1} > \pi_{i2}] \quad (23)$$

The simplest model consistent with (23) is the binary logit model. In this case this is,

$$Q_i^e = \frac{\text{EXP}(\beta_0 R_i + \sum_{n=1}^N \beta_n X_{in}^S)}{1 + \text{EXP}(\beta_0 R_i + \sum_{n=1}^N \beta_n X_{in}^S)}, \quad (24)$$

where Q_i^e is the probability that the average dwelling will be offered for rent. The coefficients to be estimated are β_0 and β_1, \dots, β_N .

2.4 The Housing Stock Adjustment Submodels

Housing stock adjustments occur yearly, but only the creation of new dwellings on vacant land and the demolition of old dwellings are considered. Both of these decisions depend crucially on the "present value of profits" (PVP) that can be derived from a dwelling over its remaining lifetime. Suppose that the average dwelling lasts M years and let the age of the average dwelling in zone i be a_i . Then the present value of profits that accrue from rental decisions from now (time t) until M can be computed as,

$$(PVP)_{tia_i} = \sum_{s=a_i}^M \frac{(R_{is}^t - M_{ils}^t)Q_{is}^{et} + (-M_{i2s}^t)(1 - Q_{is}^{et})}{(1+r)^{s-a_i}} \quad (25)$$

The numerator measures the "expected annual profit anticipated in the current year t for the year when the dwelling is s years old." Q_{is}^{et} is the probability that the dwelling will be rented when it is s years old, computed from the occupancy submodel. In the denominator, r is the market interest rate.

Now consider the owner of some vacant land parcel on which a dwelling can be constructed in zone i . This will be a new dwelling and thus s will run from one to M in equation (25). Let K_{it} be the cost of constructing the dwelling, then the profit from construction will be,

$$\Pi_{ict} = (PVP)_{tia_i} + J_{iM}/(1+r)^M - K_{it} + \epsilon_{it}^c \quad (26)$$

where J_{iM} is the resale value of the constructed dwelling M years from now and K_{it} is the current cost of constructing the dwelling, ϵ_{it}^c being a random error term. If the land is kept vacant the profits will be equal to the land's price less the present value of all future taxes and other expenses to be incurred on the land. The profits in this case are,

$$\Pi_{iot} = V_{it} - T_{it} + \epsilon_{it}^o, \quad (27)$$

where V_{it} is the land price and T_{it} is the present value of taxes and other costs, ϵ_{it}^o being a random error term.

The present value of profits in equation (26) can be rewritten as

$$(PVP)_{til} = \sum_{s=1}^T \frac{R_{is}^t Q_{is}^{et}}{(1+r)^{s-1}} + \sum_{s=1}^T \frac{(M_{i2s}^t - M_{i1s}^t) Q_{is}^{et} - M_{i2s}^t}{(1+r)^{s-1}}, \quad (28)$$

where the first summation is the "present value of lifetime expected revenue" abbreviated as $(PVR)_{til}$. Differential profits can now be written as,

$$\Pi_{ict} - \Pi_{iot} = (PVR)_{til} + \sum_{n=1}^N \gamma_n x_{in}^{St} + \epsilon_{it}^c - \epsilon_{it}^o \quad (29)$$

where the summation stands for the second summation in (28) plus $V_{it} - T_{it}$ which cannot be independently observed in the data. Thus these quantities are made a function of the supply side variables x_{in}^{St} , and γ_n , $n=1, \dots, N$ are coefficients to be estimated. Under these assumptions the probability that a vacant land parcel will be developed can be derived as a binary logit model of the form,

$$Q_i^{ct} = \frac{\text{EXP}[\gamma_0 (PVR)_{til} + \sum_{n=1}^N \gamma_n x_{in}^{St}]}{1 + \text{EXP}[\gamma_0 (PVR)_{til} + \sum_{n=1}^N \gamma_n x_{in}^{St}]} \quad (30)$$

The case of demolishing an old dwelling involves a similar reasoning. In this case the probability of demolishing the average old dwelling in zone i is given by the binary logit model

$$Q_i^{dt} = \frac{1}{1 + \text{EXP}[\delta_0 (PVR)_{ti} + \sum_{n=1}^N \delta_n x_{in}^{St}]} \quad (31)$$

where $(PVR)_{ti}$ is the "present value of revenue over the remaining lifetime of the average old dwelling in zone i ". The δ 's are coefficients to be estimated.

2.5 Market Clearing Equilibrium at Each Year

As discussed before, the crux of the model is given by the simultaneous equations (1) which are solved for the market clearing rent vector

$\bar{R}^t = [R_1^t, R_2^t, \dots, R_I^t]$ at each year t . For convenience, these equations are rewritten as

$$\sum_{h=1}^H N_h^t \sum_{m=1}^{M_i} \delta_i P_{im}^h(\bar{R}^t, \bar{X}^{Dt}, \bar{C}^{th}, \bar{T}^{th}, \bar{Y}^{th}, \bar{\alpha}_h) = S_i^t Q_i^e(R_i^t, \bar{X}^{St}, \bar{\beta}) . \quad (32)$$

The vectors \bar{C}^{th} , \bar{T}^{th} , and \bar{Y}^{th} contain the travel cost, travel time and other transportation system characteristics (such as station locations, parking availability, etc.). It is proven in Anas (1982) that equations (32) yield a unique equilibrium solution except possibly in the very unusual case when the rent of one or more zones are zero. This case should not be encountered in a meaningful empirical application and is thus not troublesome. It is also proven that the unique equilibrium is globally stable except for very large shifts in rents. Stability in this context means that if some rents are changed so that the system moves out of equilibrium it will return to it.

Anas (1982) also discusses a computational algorithm for solving the system of equations and finding the equilibrium zone rents. This algorithm is the one used in CATLAS to obtain the results to be reported in section 4.

2.6 Steady State Behavior of CATLAS

An important aspect of dynamic tools such as CATLAS is their behavior at steady state. CATLAS produces changes in the housing stock and in the rent of each zone as well as in the age distribution of the housing stock by zone. If the inputs remain constant over time, then the annual predictions of CATLAS will converge to a long run steady state. In the long run the number of vacancies in each zone will be reduced to zero as excess dwellings which remain vacant year after year will become demolished. All other variables determined within the

model will either converge to steady state values or will cycle around a steady state value (i.e. will converge to a limit cycle).

3. EMPIRICAL ESTIMATION

In this section we briefly discuss the data and how it was used to estimate the four submodels of CATLAS. The estimation results for these submodels are then presented and discussed.

3.1 Data, Sampling and Estimation

The demand and supply side submodels of CATLAS can be empirically calibrated using the U.S. Census of Population and Housing. In the Chicago application, the 1970 Census results were used because these were the most recent available. These data have been tabulated to a system of 4918 square zones of 1/2 mile by 1/2 mile covering the Chicago metropolitan area. Each zone of this grid system is called a quartersection. Transportation and travel characteristics data are available for the same zones and were obtained from the Chicago Area Transportation Study (CATS). The CATS data is aggregated to the traffic zone level which consists of one mile by one mile square zones in the city and larger zones in the suburbs. A 2 mile by 2 mile area centered on Madison and State Streets is taken to be the Central Business District or CBD. This area includes the "Loop", Chicago's traditional business center but is more than three times in area and contained 19% of all the jobs in the metropolitan region in 1970.

To estimate the submodels of CATLAS, a random sample of 433 zones or nearly 9% of the total number of zones was selected and used. Maximum likelihood for aggregated data is the technique used to estimate these models.

3.2 Estimation of Demand Submodels

The demand submodels discussed in section 2.2 and consisting of equations

(14) - (18) have been estimated for two workplace categories ($h = 1, 2$). The first workplace ($h = 1$) is the two mile by two mile CBD and the second ($h = 2$) is all other employment dispersed throughout the rest of the Chicago SMSA (hereafter non-CBD). This dispersed "workplace" is represented by the average travel time and cost by each mode from each residential zone to all other employment zones excluding the CBD. This employment classification into CBD and non-CBD is appropriate only because CATLAS has been used to examine the impact of radial rail transit lines serving the CBD. These lines have most of their effects on CBD employment and these effects are quite insensitive to gross variations in dispersed non-CBD employment. Thus the above two-way classification goes a long way toward capturing the essential aspects of rail transit investment.

The actual modal choices of CBD and non-CBD commuters are shown in table 1. The CBD multinomial logit model is estimated with four modes of travel (auto, commuter rail, rapid transit and bus). The non-CBD model is estimated with two modes of travel (auto and bus). All trips by other modes for CBD and non-CBD are treated as fixed in number for each residential zone and are added in as a constant to the left hand side of (1).

Table 2 lists the explanatory characteristics entered into the models, the value of each coefficient estimated and the t-statistic associated with that coefficient.

3.3 Estimation of Occupancy and Stock Adjustment Submodels

The occupancy, new housing construction and old housing demolition submodels discussed in section 2 have been estimated and the results are shown in table 3. Here PVR_{NEW} is the present value of the revenue expected to accrue to a new dwelling and PVR_{OLD} the present value of the revenue expected to accrue to an old dwelling over its remaining lifetime. Characteristics 4-16 are either

dummy variables or zonal average measures proxying the cost sides of the occupancy, construction, and demolition decisions as explained in section 2. The occupancy and new construction submodels are estimated from the zonal data using maximum likelihood with the number of occupied units in each zone and the number of newly constructed units between 1969-1970 in each zone being known from the census. The number of dwellings demolished is not known by zone since it is not surveyed in the census. For this reason, the demolition submodel is estimated using a cruder method. The number of dwellings demolished in the entire Chicago SMSA in the 1960's is used to determine a crude annual metropolitan demolition rate. The model coefficients are then adjusted by trial and error to achieve a good fit to this aggregate demolition rate. For this reason standard errors (and t-statistics) cannot be computed for the demolition submodel.

4. SIMULATIONS AND POLICY IMPLICATIONS

In this section we present and discuss the simulation results obtained from the application of CATLAS to evaluate rapid transit projects proposed for the Southwest side of Chicago. The results are rich in policy implications regarding transit financing and these are discussed in this section.

4.1 Simulation Data and Assumptions

For the purposes of performing equilibrium simulations with CATLAS the zones of the Chicago SMSA are aggregated to the 1690 traffic zones as shown in figure 1. The same figure also shows the boundary of the Southwest corridor expected to be impacted in a major way by the proposed transit projects. Figure 2 shows the alignment of existing commuter rail and rapid transit lines within the corridor and also the alignment of three alternative proposed rail lines: the Archer Avenue subway, the Gulf Mobile and Ohio right-of-way project and the

Indiana Harbor Belt right-of-way project. The last two projects would be built on the rights-of-way of freight railroads known by the same name.

Introduction of any one of these rail projects would change the zone-to-CBD transit travel times and costs of the zones within the Southwest corridor. To compute these new times and costs we need to take into account the changed costs of access to the new rapid transit stations. This was done by adopting an access mode choice model developed for the Chicago area by Sajovec and Tahir (1976). This model allows access to stations by walking, bus and automobile. The access costs and times computed from this model are added to the station-to-CBD line haul times and the minimum time route is then computed for each zone. The costs and times of these zones are then entered into the demand model for the CBD, replacing the times and costs existing prior to the new project.

In the policy simulations to be reported, it is assumed that the new transit projects will influence the decisions of CBD commuters only. Since in reality the transit project will draw trips from other employment locations as well, its impact on housing values and land use will be larger than that predicted in these simulations. In fact these results should be taken as lower bounds of the impact of the transit lines.

Tables 4 and 5 show the 1970 aggregate descriptive data for the Chicago SMSA and Southwest corridor respectively. The construction costs of the three rail projects were computed using detailed project descriptions and the unit costs from Permut and Zimring (1975) and Krueger et al. (1980). In 1970 dollars, the GM&O project would cost \$120.4 million, the Archer subway \$235.5 million and the IHB project \$249.1 million respectively.

4.2 Simulation Results and Transit Finance Implications

Two kinds of simulations are performed using CATLAS. The first of these is a static simulation in which the housing stock in each zone is held fixed at its

1970 level. This simply means that the housing stock adjustment submodels are removed from the recursive structure and the model deals only with the allocation of households to dwellings by employing the demand and occupancy submodels. The second type of simulation uses the full recursive structure to simulate changes in the housing stock over time. The static simulations provide sufficient insight into certain basic results. Thus the results of these simulations will be presented first.

4.2.1 Static Simulations

Table 6 shows the effects of the three projects on aggregate rent changes, mode patronage (or demand) changes for CBD and non-CBD commuters. These can be looked at for the entire SMSA and for the Southwest corridor and by city and suburb in each case. The projects have the following effects: they increase the attractiveness or utility of central city zones by reducing transit travel times and costs and by extending such service to where it was not previously available. The effect is to attract some households to relocate from the suburbs to the city thus raising city rents while reducing suburban rents. Aggregate metropolitan rents are reduced because the movement of households is from the higher rent suburbs to the lower rent central cities. When we look into the Southwest corridor we see that aggregate rents increase in both the city and suburban parts of the corridor. A zone by zone view of these rent changes are shown in figures 3, 4 and 5 for the three projects. Rent changes outside the Southwest corridor are extremely small in magnitude (amounting to several dollars per dwelling annually at most) and can be ignored from a taxation viewpoint. If the special assessment district is defined to coincide with the boundary of the corridor and an incremental special assessment tax is implemented within this corridor taxing away the increases from the dwellings which appreciate in value and giving rebates to dwellings which decline in

value, the incremental revenue collected in this way amounts to \$6.4 - \$8.2 million annually.

How big is the tax burden of such a special assessment on the housing owners in the corridor? The maximum zonal average rent increases are \$247, \$235 and \$235 per year from figures 3-5 respectively, or about \$20 per month. In the vast majority of zones, rent increases are a lot lower. The average rent increase per dwelling in the corridor is just under \$25 per year for the GM&O project. These figures show that the tax burden on the average housing owner is small and thus a special assessment policy is not likely to encounter major political opposition if it is carefully explained to the public and if the potential for rent increases is carefully documented. We also see that where rents decrease the decreases are negligible and thus if no rebates are given to such housing owners there will be no political opposition.

The next question of policy interest is "what percentage of the capital cost of these transit lines can be captured via the incremental tax method?" The answer depends crucially on what interest rate is used in discounting the annual tax revenues. Moody's Bond Survey Record gave a Ba rating to the Chicago Transit Authority in 1970. Bonds issued in 1970 with a Ba rating generally paid 10% interest. Using this interest rate the project capital costs are annualized over a 35-year horizon and the annual operating costs are computed using a procedure of the Chicago Transit Authority (1980).

4.2.2 Dynamic Simulations

The purpose of the dynamic simulations is to determine whether the policy implications of the static simulations hold up or are substantially altered by the introduction of the stock adjustment submodels. The results obtained from the dynamic simulations depend crucially on what assumptions are made regarding the increase of employment (and population) for the Chicago SMSA. The results

are also sensitive to year-by-year changes in the input variables.

Because the time path of the input variables are uncertain, one approach to dynamic simulation is to keep these constant over time. If this is done, then the housing stock adjustment submodels will forecast the redistribution and ageing-renewal of a fixed total housing stock.

The following assumptions were employed:

1) The aggregate number of households and commuters is determined within the model by assuming that the aggregate housing vacancy rate will stay at the 1970 level and the number of households will adjust year by year according to changes in the housing stock.

2) All other input variables remain at their 1970 levels.

3) The distribution of jobs between the CBD and the non-CBD locations maintain their 1970 proportions.

We believe these assumptions to be the most prudent given our limitations in forecasting the future paths of the input variables .

Given the above assumptions, we performed a twenty-year simulation (i.e. from 1970-1990) without introducing any changes in the transportation system (this is called a baseline simulation or base run) and a twenty-year simulation in which the GM&O project is introduced (this is called a policy simulation or policy run).

The results of these baseline and policy simulations are shown in tables 7-10 for both the entire SMSA and for the Southwest corridor.

The aggregate rent changes and other fluctuations are caused by two factors. The first is the change in total housing stock and the second the housing redistribution among the zones. For the SMSA results (table 7) the aggregate rent changes are larger than the housing stock changes in the first several years because the new housing constructed in the suburbs is more

valuable and there are fewer housing units remaining in the city due to demolitions. Following the construction of new housing units, the available vacant land is reduced; thus fewer housing units can be constructed. In the meantime, as the old housing units age, more of them will be demolished. Beginning with the ninth year, the housing stock decreases. When the pace of population increase starts to slow down, owners find that it is more difficult to rent or sell dwellings and demand lower rents. This explains the decrease of aggregate rents in the later years. The results for the Southwest corridor (table 8) are similar to the SMSA results, but because the average housing age is higher and the available vacant land is less than in the SMSA, the housing stock within the corridor begins to decrease from the first year and so do the aggregate rents.

The results of the GM&O policy simulation are shown in tables 9 and 10 which document the difference between the policy simulation and the corresponding baseline simulation. The most notable result is that the transit project has a very small net influence on the housing stock changes. In other respects the results are similar to the static simulations.

Two other policies were also simulated. In one of these the GM&O project is introduced and it is assumed that CBD parking fees double. In the second, it is assumed that the price of gasoline doubles. The estimated cost and cost recovery ratios are shown in table 11. In obtaining these figures, it was assumed that the incremental special assessment tax would be levied on vacant land as well as on housing units. It can be seen that the aggregate land value change in the Southwest corridor due to the project is quite small because less than 8% of the available vacant land is within the corridor. The cost recovery ratios are quite close to those of the static simulations.

4.3 Caveats and Conclusions

Any large scale simulation analysis is not an exact science and is subject to numerous sources of error and bias. Most of these are inherent in the data and in the mathematical form and assumptions of the analysis. Such sources of error and bias are unavoidable. The best one can do is to gain an intuition for the magnitudes of these errors and biases by performing extensive sensitivity testing on the various aspects of the analysis system including the estimated coefficients and elasticities. Such sensitivity tests were performed and have been reported in Anas (1982) and Duann (1982). Despite the fact that results can change substantially if some coefficients are doubled or tripled or if some data has not been accurately measured, little reason exists to doubt the basic conclusions. In the final analysis we remain confident in the general approach and method used because we cannot identify any systematic sources of bias that weaken our conclusions.

There are several strong qualitative arguments that the total impact of transit on property values is stronger than that estimated in our application. This means that our quantitative results may be better viewed as lower bounds. We know, for example, that if CATLAS is extended to deal with nonwork trips as well as with work trips, then the impacts of transit on housing values will be higher because travel cost and time savings in nonwork travel will be capitalized into housing values. Similarly, if the non-CBD workplaces are identified by exact location rather than lumped together into one category, there will be additional gains in work travel translated into housing price increases. Finally, if we include commercial and industrial properties into the analysis, we will find that these too, and especially commercial floor space, appreciates in value substantially.

Another caveat is that the value capture cost recovery ratio of bus systems is surely higher than that for rail. This does not necessarily occur because

bus systems have a stronger impact on housing values, but because the rolling stock cost of bus systems is much lower than the construction and rolling stock cost of rail systems. Thus, it should not be surprising if a similar analysis were to yield a cost recovery ratio for bus systems of 100% or higher. Such a result is not very useful, however, because it is the finance of rapid rail systems, and particularly of their capital cost, that poses the major challenge in the years ahead. It is clear that these costs cannot be covered out of the farebox if reasonable levels of ridership are to be maintained. Incremental special assessment taxes on real estate appear to be a promising way of financing a significant part of the capital costs of rail systems.

REFERENCES

- Adkins, W.G., 1959, Effect of the Dallas Central Expressway on Land Values and Land Use, Texas Transportation Institute.
- Alonso, W., 1964, "Location and Land Use", Harvard University Press, Cambridge, Mass.
- Anas, A., 1981, "The Estimation of Multinomial Logit Models of Joint Location and Travel Mode Choice from Aggregated Data", J. Regional Sci., 21(2), p.223-242.
- Anas, A., 1982, Residential Location Markets and Urban Transportation, Academic Press.
- Arnott, R.J. and Stiglitz, J.E., 1981, "Aggregate Land Rents and Aggregate Transport Cost", The Economic Journal, 91, pp. 331-347.
- Ashley, R.N., 1965, "Interchange Development Along 180 Miles of I-94", Highway Research Record 96, Highway Research Board.
- Beckmann, M.J., 1969, "On the Distribution of Rent and Residential Density", J. Econ. Theory.
- Boyce, D.E. and Allen, B., 1973, "Impact of Rapid Transit on Suburban Residential Property Values and Land Development", Department of Regional Science, University of Pennsylvania, Philadelphia, Pa.
- Chicago Transit Authority, 1980, "Estimates of Heavy Rail Operating Costs: Southwest Transit Study", General Operations Division, Operations Planning Department.
- Davis, J.L., 1965, The Elevated System and the Growth of Northern Chicago, Northwestern University, Studies in Geography No. 10.
- deLeeuw, F. and Struyk, R.M., 1975, The Web of Urban Housing: Analyzing Policy with a Simulation Model, The Urban Institute, Washington, D.C.
- Deweese, D.N., 1976, "The Effect of a Subway on Residential Property Values in Toronto", J. Urban Econom., 3(4), 357-369.
- Domencich, T., and McFadden, D., 1975, "Urban Travel Demand: A Behavioral Analysis", North-Holland Publ., Amsterdam.
- Duann, L.S., 1982, "A Dynamic Simulation Model for Residential Location, Travel Mode Choice and Residential Land Development", PhD Dissertation, Department of Civil Engineering, Northwestern University.
- Golden, J.S., 1968, "Land Values in Chicago: Before and After Expressway Construction", The Chicago Area Transportation Study.
- Ingram, G., Kain, J., and Ginn, J.R., et al., 1972, "The National Bureau of Economic Research, Detroit Prototype, Urban Simulation Model", Columbia University Press, New York, and the NBER.

- Krueger, C., Heramb, C., Kunze, B., and Gallery, M., 1980, Southwest Transit Study, Phase I Report: Preliminary Alternatives Analysis. City of Chicago, Department of Public Works, Bureau of Transportation Planning and Programming.
- Lemly, J.H., 1959, "Changes in Land Use and Value Along Atlanta's Expressways", Highway and Economic Development, Highway Research Board Bulletin 277.
- Lerman, S.R., 1977, Location, Housing and Automobile Ownership and Mode to Work: A Joint Choice Model, Transportation Res. Record, (610).
- McFadden, D., 1973, "Conditional Logit Analysis and Qualitative Choice Behavior", in "Frontiers in Econometrics", Academic Press, N.Y.
- McFadden, D., 1978, Modelling the Choice of Residential Location. In "Spatial Interaction Theory and Planning Models" (A. Karlqvist et al., eds.) North-Holland Publishing, Amsterdam.
- Mohring, H., and Harwitz, M., 1962, "Highway Benefits: An Analytical Framework", Northwestern University Press, Evanston, Illinois.
- Mudge, R., 1972, The Impact of Transportation Savings on Suburban Residential Property Values, PhD Dissertation, University of Pennsylvania, Philadelphia.
- Muth, R.F., 1969, "Cities and Housing", University of Chicago Press, Chicago.
- Permut, H. and M. Zimring, 1975, "Capital and Operating Costs for the Expansion of the Chicago Rapid Transit System", Technical Report, Regional Transportation Authority, Chicago, Illinois.
- Quigley, J., 1976, Housing Demand in the Short Run: An Analysis of Polytomous Choice, in "Explorations in Economic Research", (S.D. Winter, ed.), Vol. 3, No. 1, pp. 76-102.
- Sajovec, J. and Tahir, N., 1976, "Development of Disaggregate Behavioral Mode Choice Models for Feeder Bus Access to Transit Stations", M.S. Thesis, Northwestern University, Evanston.
- Shelton, J.P., "The Cost of Renting Versus Owning a Home", Land Econ., February 1968, pp. 59-72.
- Sleng, E.H., 1930, Land Values in New York in Relation to Transit Facilities, AMS Press.
- Wheaton, W.C., 1974, "A Comparative Static Analysis of Urban Spatial Structure", Journal of Economic Theory.
- Wootan and Haning, 1960, Changes in Land Values, Land Use and Business Activity Along a Section of the Interstate Highway System in Austin, Texas, Texas Transportation Institute.

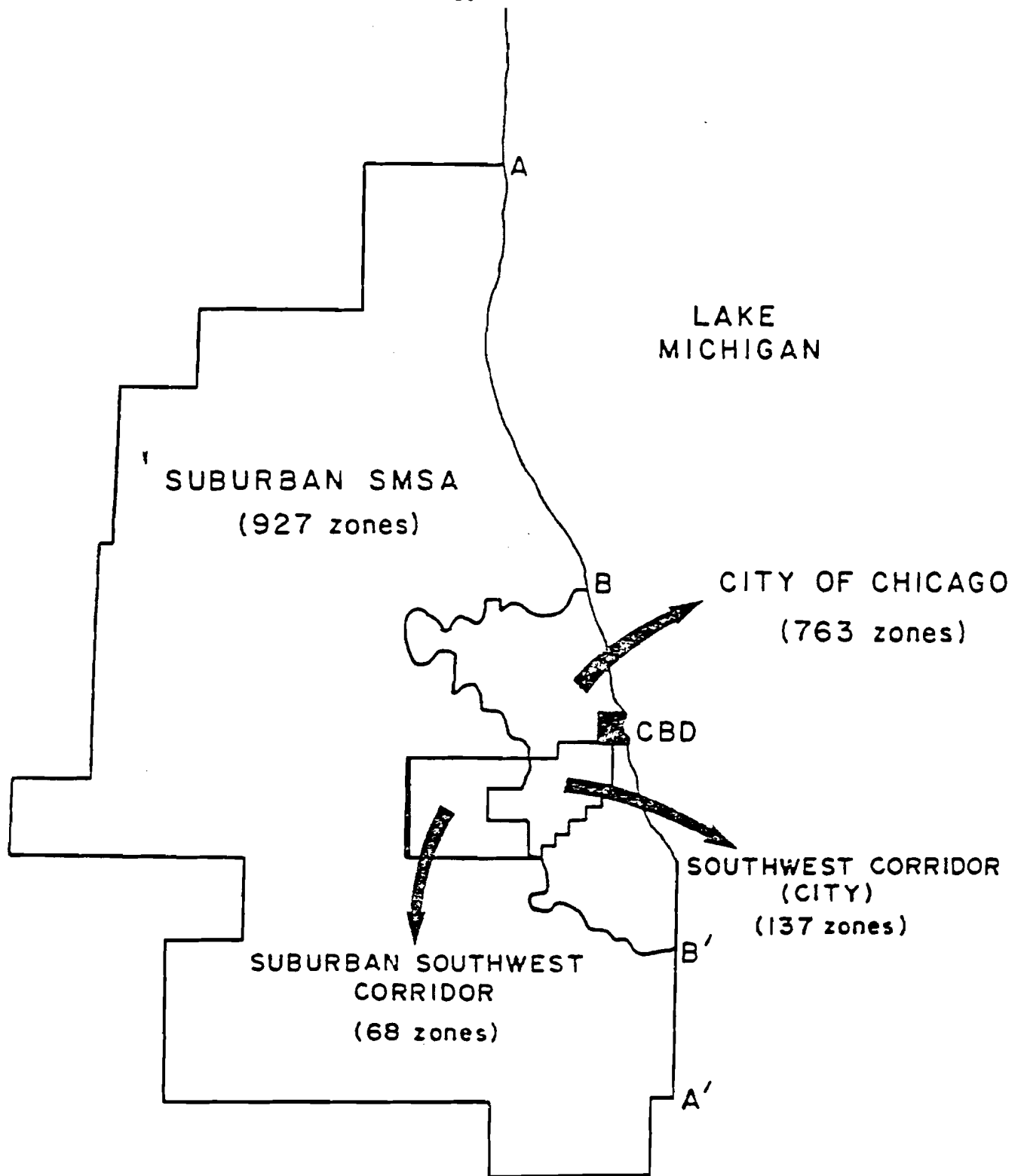


Figure 1: The 1690 Zone System Used for Policy Simulations with CATLAS.

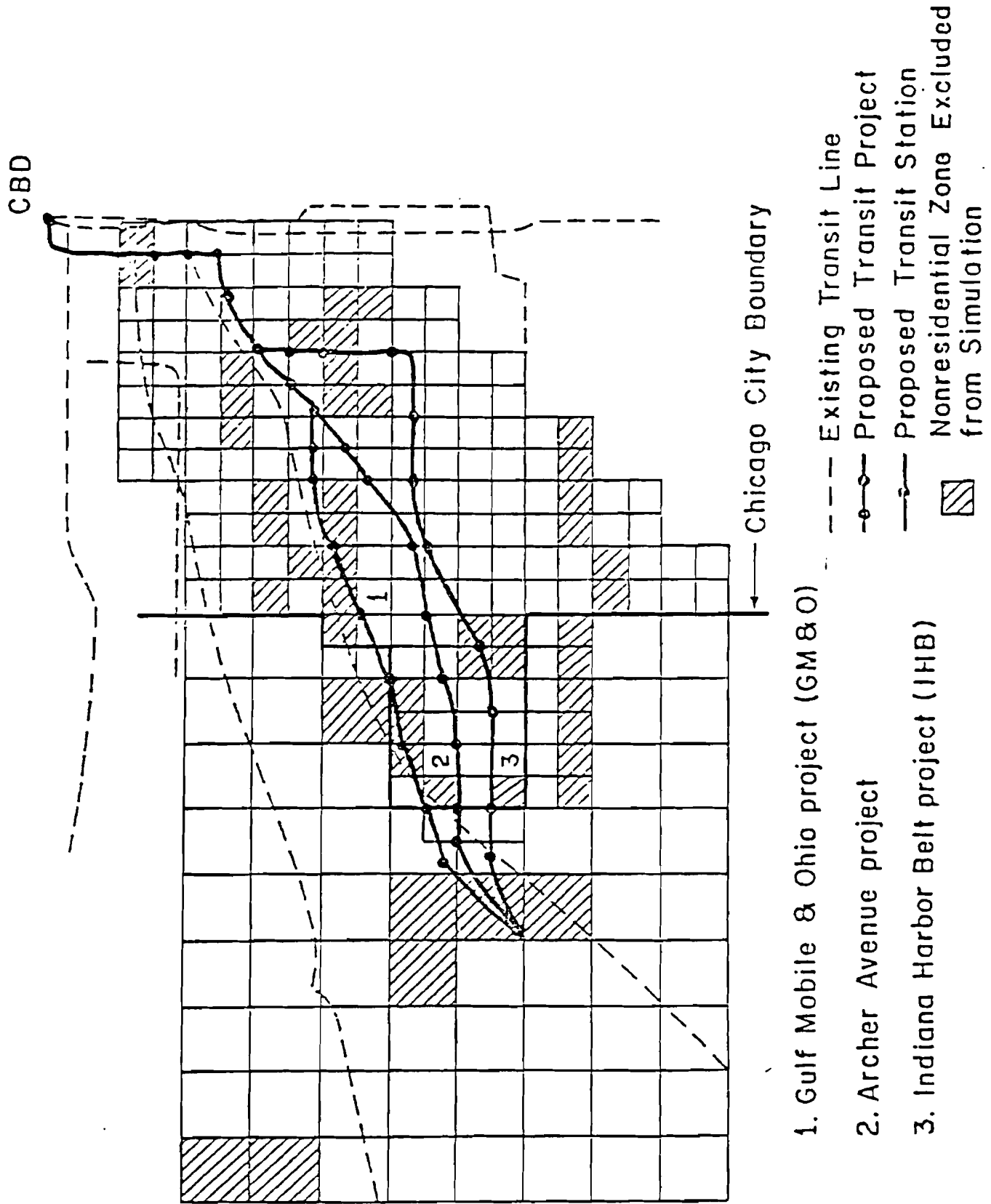


Figure 2: Three Transit Projects Proposed for the Southwest Corridor.

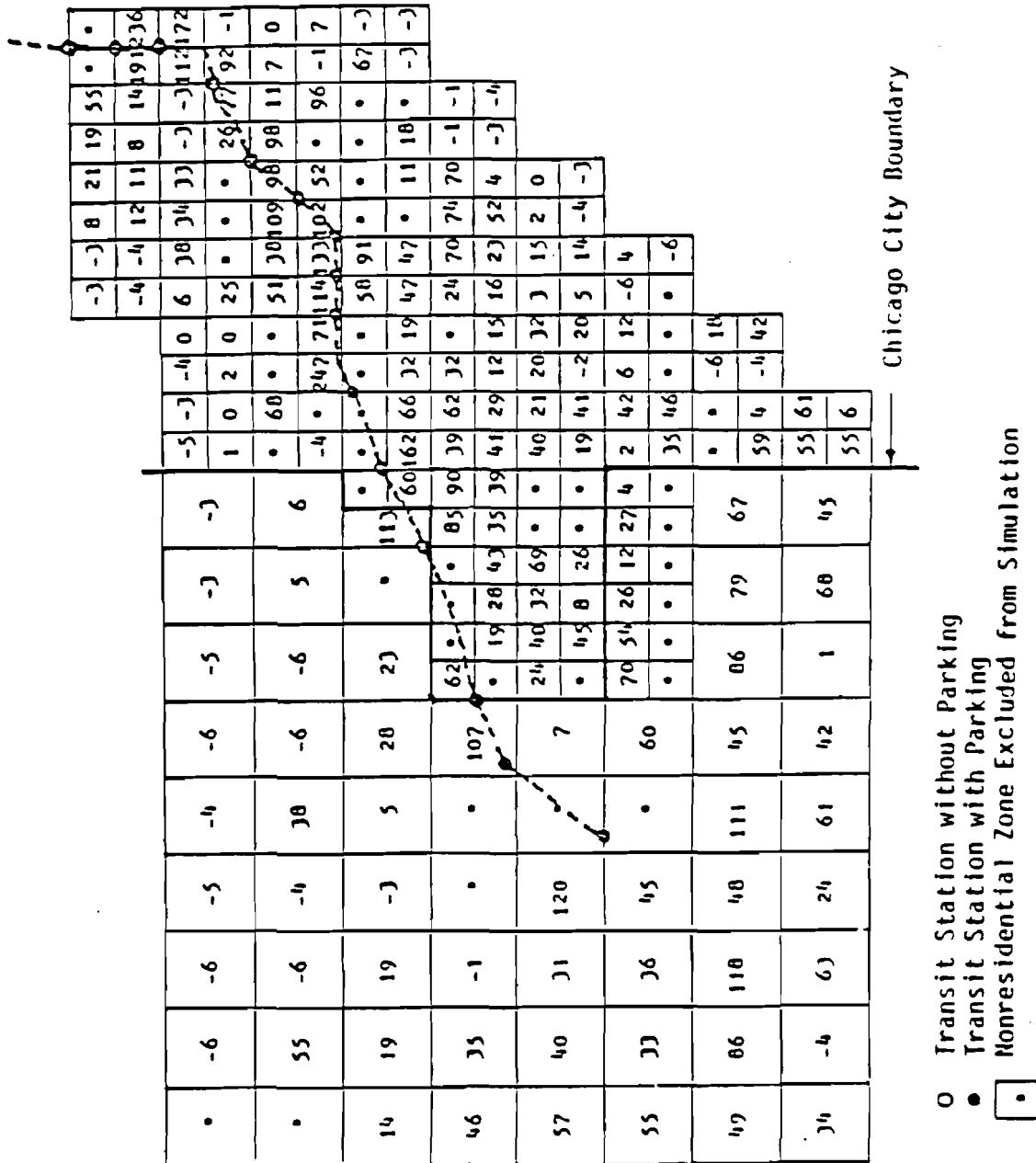


Figure 3: Average Zonal Rent Changes in the Southwest Corridor Due to the Gulf Mobile & Ohio Project.

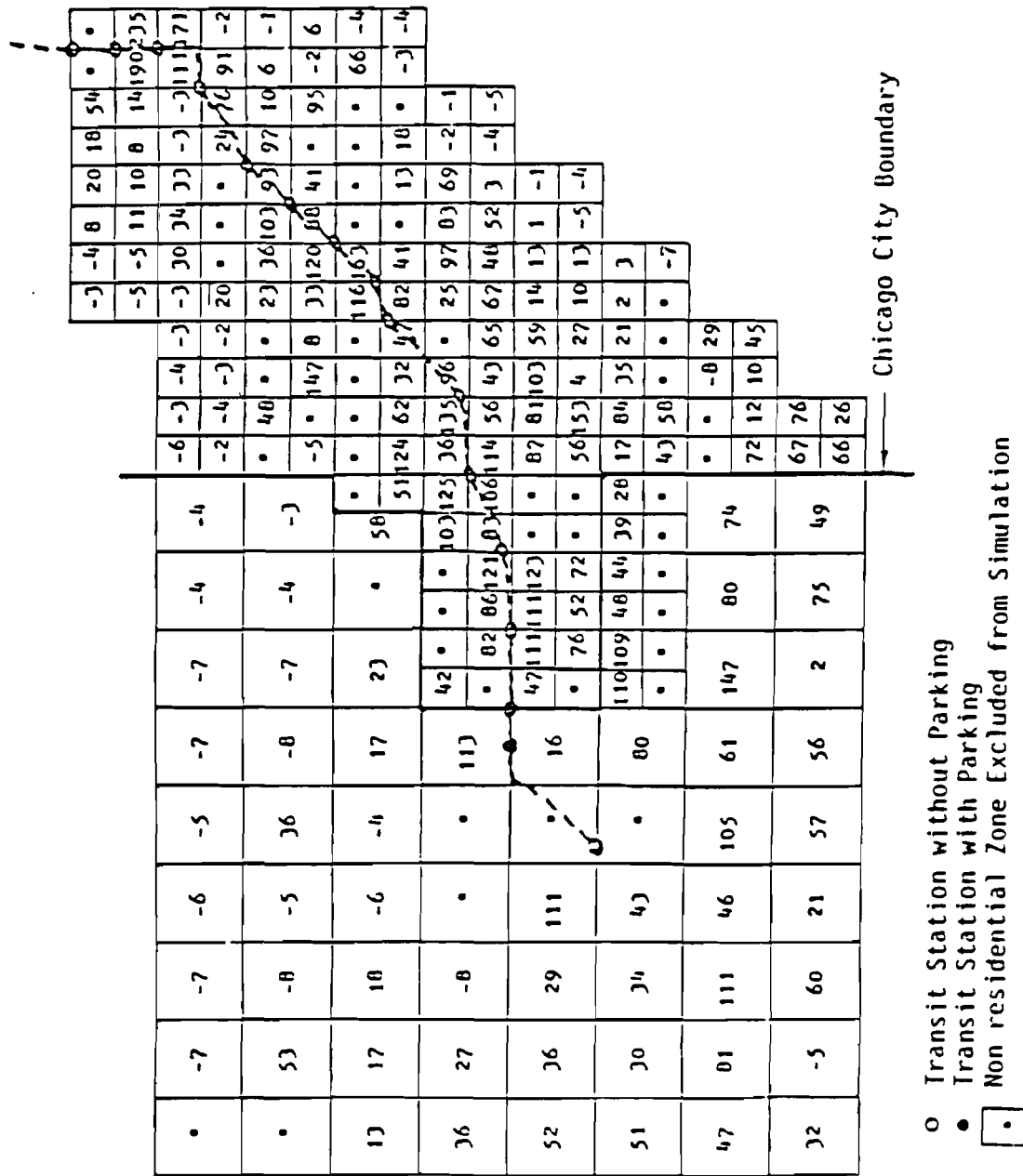


Figure 4: Average Zonal Rent Changes in the Southwest Corridor Due to the Archer Avenue Project.

Location of Workplace

Travel Modes	Inside CBD	Outside CBD	Mode Totals
Auto driver	129,995 (29%)	1,184,372 (61%)	1,314,367 (55%)
Auto passenger	28,251 (6%)	230,598 (12%)	258,849 (11%)
Commuter rail	77,908 (17%)	26,665 (1%)	104,573 (4%)
Rapid transit	83,092 (18%)	38,849 (2%)	121,941 (5%)
Bus	108,400 (24%)	232,109 (12%)	340,509 (14%)
Other	26,050 (6%)	231,373 (12%)	257,423 (11%)
Total	453,696 (19%)	1,943,966 (81%)	2,397,662

TABLE 1 : Mode Choices of Chicago SMSA Commuters in 1970

Explanatory
Characteristics
in Utility Function

Estimated Coefficient
CBD Model Non-CBD Model

1. Housing supply	$\alpha_0 = 1.000$ (-)	1.000 (-)
2. Inclusive value	$\alpha_1 = 0.723$ (30.7)	0.955 (15.3)
3. Commuter rail (CR) dummy	$\alpha_2 = -.846$ (23.0)	-
4. Rapid transit (RT) dummy	$\alpha_3 = -1.701$ (39.0)	-
5. Bus dummy	$\alpha_4 = -0.636$ (12.3)	-2.627 (175.0)
6. Log (Travel time)	$\alpha_5 = -2.392$ (55.5)	-0.910 (25.7)
7. Log (Travel cost + rent)	$\alpha_6 = -1.488$ (12.4)	-5.461 (42.6)
8. Bus miles/square mile	$\alpha_7 = 0.020$ (54.4)	0.017 (70.5)
9. RT stations within 0-0.5 miles	$\alpha_8 = 0.294$ (20.9)	-
10. RT stations within 0.5-1 miles	$\alpha_9 = 0.134$ (9.9)	-
11. RT stations within 1-2 miles	$\alpha_{10} = 0.246$ (23.2)	-
12. CR stations within 0-1 miles	$\alpha_{11} = 0.349$ (19.9)	-
13. Log (Housing age)	$\alpha_{12} = -0.188$ (14.0)	-0.097 (14.5)
14. Log (Zone income)	$\alpha_{13} = 1.015$ (53.2)	-0.117 (8.4)
15. Log (Distance to the CBD)	$\alpha_{14} = 0.447$ (18.4)	0.426 (47.9)
16. Log (Angle from Lake Michigan)	$\alpha_{15} = 0.001^*$ (0.08)	-0.206 (23.0)
17. D1 (0-10 miles)	$\alpha_{16} = 0.490$ (19.6)	0.287 (20.2)
18. D2 (10-20 miles)	$\alpha_{17} = 0.122$ (6.0)	0.296 (29.9)
19. D3 (> 25 miles)	$\alpha_{18} = -0.591$ (20.6)	0.132 (12.3)
20. Log (Rooms)	-	1.194 (62.0)
$\frac{2}{\rho}$	0.420	0.828

TABLE 2: Estimated coefficients and t-statistics of the CBD and non-CBD multinomial logit demand functions.

Explanatory Characteristics	Estimated Coefficients		
	Occupancy (β 's)	New Construction (γ 's)	Demolition (δ 's)
1. Annual rent	0.000131 (19.5)	-	-
2. PVR_{NEW}	-	0.00001018 (12.95)	-
3. PVR_{OLD}	-	-	0.00002135 (-)
4. Rental dummy	-0.679 (17.2)	-	-
5. Build dummy	-	2.214 (62.88)	-
6. Don't demolish dummy	-	-	4.595 (-)
7. City location dummy	-	-0.6162 (34.35)	-
8. Distance to CBD	-	-0.09660 (137.2)	-0.03853 (-)
9. Angle	0.00131 (19.9)	-0.003345 (35.51)	-0.001892 (-)
10. Rooms	-	-	-0.1135 (-)
11. Housing age	-	-	-0.0146 (-)
12. $\log(\text{Housing age})$	0.516 (53.0)	-	-
13. % Black Households	-0.00347 (32.2)	-0.007379 (30.94)	-0.002736 (-)
14. % Developed land	0.0119 (61.1)	-	-
15. % Single family housing	0.0181 (119.1)	0.0119 (61.1)	0.01137 (-)
16. Zonal income	-	0.00003756 (21.7)	0.00010326 (-)
ρ^2	0.981	0.835	-

Table 3: Estimated coefficients and t-statistics of the occupancy, new housing construction and old housing demolition submodels.

HOUSING

	Rent (\$/year)	Housing Stock	Vacant Units	Vacancy Rate (%)
CITY	1,859,632,333 (42.1)	1,197,370 (54.2)	70,344 (68.3)	5.87
SUBURBAN	2,556,541,980 (57.9)	1,013,781 (45.8)	32,682 (31.7)	3.22
Total	4,416,174,314 (100.0)	2,211,151 (100.0)	103,026 (100.0)	4.66

WORK TRIPS (daily, one-way)

	Auto	Computer rail	Rapid transit	Bus	Other	Total
CBD	158,246 (35.0)	77,908 (17.0)	83,092 (18.0)	108,400 (24.0)	26,050 (6.0)	453,696 (19.0)
Non-CBD	1,414,970 (73.0)	26,665 (1.0)	38,849 (2.0)	232,109 (12.0)	231,373 (12.0)	1,943,966 (81.0)
Total	1,573,216 (66.0)	104,573 (4.0)	191,492 (5.0)	340,509 (14.0)	257,423 (11.0)	2,397,662 (100.0)

TRAVEL TIME AND COST FOR WORK TRIPS (daily, one-way times (min); annual two-way costs, \$)

	Auto	Commuter rail	Rapid transit	Bus	Total
CBD travel time	7,976,401	4,601,530	3,155,762	4,719,653	20,453,346
Non-CBD travel time	50,124,207	*	*	7,608,463	*
CBD travel cost	208,888,515	47,580,759	25,865,238	25,861,800	308,196,313
Non-CBD travel cost	1,559,869,108	*	*	52,400,825	*

TABLE 4 : Selected Aggregate Characteristics of the Metropolitan Data

HOUSING

	Rent (\$/year)	Housing Stock	Vacant Units	Vacancy Rate (%)
CITY	232,506,706 (53.5%)	173,986 (66.8%)	8,382 (81.4%)	4.82
SUBURBAN	202,400,397 (46.5%)	86,662 (33.2%)	1,917 (18.6%)	2.21
Total	434,907,103 (100%)	260,648 (100%)	10,299 (100%)	3.95

WORK TRIPS (daily, one way)

	Auto	Commuter Rail	Rapid Transit	Bus	Other	Total
CBD	20,422 (38.6%)	5,689 (10.7%)	4,894 (38.6%)	20,502 (38.6%)	1,464 (2.8%)	52,991 (18.8%)
Non-CBD	159,196 (69.4%)	1,575 (0.7%)	2,132 (0.9%)	37,196 (16.2%)	29,193 (12.7%)	229,292 (81.2%)
Total	179,638 (63.6%)	7,264 (2.6%)	7,026 (2.5%)	57,698 (20/4%)	30,657 (10.9%)	282,283 (100%)

TRAVEL TIME AND COST FOR WORK TRIPS (daily, one-way times (min); annual two-way cost, \$)

	Auto	Commuter Rail	Rapid Transit	Bus	Total
CBD travel time	957,842	270,167	206,895	830,690	2,265,594
Non-CBD travel time	5,858,183	*	*	1,243,073	7,101,256
CBD travel cost	19,471,295	2,739,071	1,607,423	4,637,050	28,454,839
Non-CBD travel cost	146,705,281	*	*	8,369,100	155,074,381

GASOLINE CONSUMPTION FOR WORK TRIPS BY AUTO (daily, one way)

CBD auto trips	17,470 gallons
Non-CBD auto trips	98,666 gallons

TABLE 5 : Selected Aggregate Characteristics of the Southwest Corridor Data

Metropolitan Changes

Project	% Aggregate Rent Change			% Mode Demand Changes							Employee Change ¹		Consumer Surplus ²	
	City	Suburb	Total	CBD				Non-CBD			CBD	Non-CBD	CBD	Non-CBD
				Auto	Rail	Transit	Bus	Auto	Bus					
GM&O	0.003	-0.089	-0.051	-0.84	-0.29	3.59	-1.32	0.02	-0.15			2.3	-0.0074	
ARCHER	0.033	-0.128	-0.060	-1.05	-0.32	4.50	-1.70	0.02	-0.15			2.9	-0.016	
IHB	0.027	-0.115	-0.055	-1.01	-0.30	4.24	-1.57	0.02	-0.14			2.8	-0.017	

Southwest Corridor Changes

GM&O	2.14	0.72	1.48	-5.21	-2.12	62.45	-6.6	0.31	-2.66	516	-499	-	-
ARCHER	2.92	0.70	1.89	-6.45	-2.07	78.31	-8.5	0.33	-3.13	657	-634	-	-
IHB	2.73	0.73	1.80	-6.23	-1.91	73.79	-7.8	0.31	-2.96	622	-601	-	-

TABLE 6: Simulation Results for the Three Rail Projects

¹ Number of employees who relocate into or more out of the Southwest corridor Study Area

² ($\times 10^{-3}$)

Year	Rent Change (%) ¹			Mode Demand Change (%) ¹						Housing Stock Change ²			Consumer Surplus ¹	
	City	Suburb	Total	CBD			Non-CBD			City	Suburb	Total	CBD	Non-CBD
				Auto	Rail	Transit	Bus	Auto	Bus					
1	-2.19	1.87	0.16	0.58	2.96	0.24	0.07	0.82	0.79	-8580	2660	18080	0.0029	0.011
2	-1.63	5.49	2.49	1.44	5.22	0.10	-0.45	1.85	-1.40	-8793	21452	12659	-0.0032	0.015
3	-1.16	8.14	4.23	2.07	7.13	-0.06	-1.00	2.63	-3.27	-8480	17510	9030	-0.012	0.018
4	-0.99	9.83	5.28	2.46	8.76	-0.20	-1.51	3.19	-4.63	-80.3	14430	6350	-0.018	0.019
5	-1.03	10.75	5.79	2.68	10.18	-0.33	-1.98	3.57	-5.58	-7714	12014	4301	-0.024	0.021
6	-1.23	11.12	5.92	2.77	11.42	-0.46	-2.42	3.82	-6.24	-7178	10079	2701	-0.030	0.021
7	-1.51	11.07	5.77	2.77	12.51	-0.58	-2.85	3.97	-6.70	-7083	8510	1427	-0.035	0.022
8	-2.14	10.37	5.10	2.62	13.50	-0.66	-3.20	3.99	-6.66	-6821	7231	410	-0.039	0.023
9	-2.65	9.60	4.44	2.44	14.38	-0.77	-3.57	3.96	-6.65	-6590	6139	-451	-0.034	0.023
10	-3.07	8.77	3.77	2.23	15.16	-0.89	-3.93	3.90	-6.64	-6391	5244	-1147	-0.048	0.022
11	-3.48	7.84	3.07	1.97	15.86	-1.02	-4.29	3.80	-6.60	-6205	4486	-1719	-0.052	0.022
12	-3.83	6.06	2.35	1.73	16.49	-1.15	-4.65	3.67	-6.52	-6028	3044	-2185	-0.057	0.021
13	-4.13	5.03	1.63	1.44	17.05	-1.29	-5.00	3.52	-6.42	-5871	3290	-2582	-0.060	0.020
14	-4.41	4.76	0.90	1.14	17.57	-1.43	-5.34	3.34	-6.27	-5725	2806	-2919	-0.065	0.019
15	-4.63	3.66	0.16	0.83	18.05	-1.58	-5.68	3.15	-6.11	-5600	2308	-3232	-0.069	0.018
16	-4.83	2.53	-0.57	0.50	18.48	-1.73	-6.01	2.93	-5.91	-5487	2005	-3402	-0.073	0.016
17	-4.97	1.38	-1.29	0.16	18.87	-1.89	-6.34	2.70	-5.67	-5390	1677	-3713	-0.076	0.015
18	-5.06	0.21	-2.01	-0.20	19.24	-2.04	-6.67	2.45	-5.40	-5299	1376	-3723	-0.080	0.014
19	-5.11	-0.98	-2.77	-0.57	19.57	-2.19	-6.98	2.18	-5.07	-5212	1100	-4111	-0.083	0.012
20	-5.07	-2.16	-3.39	-0.94	19.88	-2.36	-7.29	1.90	-4.75	-5129	856	-4273	-0.087	0.011

TABLE 7: Aggregate results of the twenty year baseline simulation for the metropolitan area.

¹ Changes compared to the initial period

² Changes from previous year

Year	Rent Change (\$) ¹			Mode Demand Change (\$) ¹								Housing Stock Change ²			Net Employee Change ¹	
				COO				Non-COO							COO	Non-COO
	City	Suburb	Total	Auto	Rail	Transit	Bus	Auto	Bus	Transit	Bus	City	Suburb	Total		
1	-2.63	-1.78	-2.23	-0.17	1.20	-0.21	0.06	-0.75	1.21			-1408	652	-836	41	-751
2	-2.38	-1.14	-1.80	0.15	2.12	-0.79	-0.47	-0.74	-1.10			-1469	520	-949	16	-1592
3	-2.25	-0.92	-1.64	0.32	2.84	-1.32	-1.00	-0.05	-3.03			-1418	393	-1025	-43	-2481
4	-2.45	-1.22	-1.88	0.33	3.47	-1.60	-1.40	-1.10	-4.38			-1362	297	-1065	-127	-3386
5	-2.00	-1.09	-2.42	0.22	4.04	-2.24	-1.92	-1.46	-5.28			-1309	222	-1087	-229	-4295
6	-3.46	-2.81	-3.16	0.01	4.56	-2.64	-2.33	-1.90	-5.86			-1259	164	-1095	-345	-5199
7	-4.12	-3.87	-4.01	-0.26	5.03	-3.02	-2.71	-2.37	-6.22			-1214	118	-1076	-471	-6093
8	-5.15	-5.35	-5.24	-0.65	5.50	-3.33	-3.02	-2.97	-6.03			-1173	82	-1072	-603	-6975
9	-6.05	-6.72	-6.36	-1.05	5.91	-3.66	-3.35	-3.55	-5.03			-1138	51	-1007	-744	-7835
10	-6.00	-8.05	-7.42	-1.46	6.28	-3.99	-3.68	-4.12	-5.76			-1103	27	-1076	-890	-8701
11	-7.65	-9.34	-8.44	-1.87	6.62	-4.32	-4.02	-4.60	-5.62			-1073	7	-1066	-1041	-9543
12	-8.39	-10.60	-9.42	-2.30	6.93	-4.64	-4.35	-5.23	-5.46			-1044	-7	-1053	-1194	-10370
13	-9.11	-11.03	-10.38	-2.73	7.22	-4.95	-4.69	-5.79	-5.27			-1017	-20	-1037	-1350	-11181
14	-9.80	-13.03	-11.31	-3.17	7.49	-5.27	-5.02	-6.34	-5.07			-993	-34	-1027	-1508	-11981
15	-10.40	-14.21	-12.21	-3.61	7.73	-5.58	-5.35	-6.08	-4.84			-971	-42	-1013	-1660	-12766
16	-11.14	-15.37	-13.11	-4.06	7.95	-5.88	-5.60	-7.44	-4.50			-953	-53	-1006	-1830	-13544
17	-11.79	-16.51	-13.99	-4.52	8.17	-6.18	-6.01	-7.98	-4.33			-933	-59	-992	-1972	-14308
18	-12.44	-17.65	-14.86	-4.98	8.37	-6.47	-6.33	-8.53	-3.98			-915	-69	-984	-2155	-15055
19	-13.08	-18.77	-15.72	-5.45	8.56	-6.76	-6.65	-9.09	-3.63			-903	-75	-978	-2319	-15814
20	-13.70	-19.86	-16.57	-5.92	8.73	-7.04	-6.96	-9.63	-3.26			-886	-80	-966	-2484	-16553

TABLE 8: Aggregate results of the twenty year simulation for the southwest corridor.

¹ changes compared to the initial period

² changes from previous year

Year	Rent Change (%) ¹			Node Demand Change (%) ¹						Housing Stock Change ²			Consumer Surplus ²	
	City	Suburb	Total	CBD			Non-CBD			City	Suburb	Total	CBD	Non-CBD
				Auto	Rail	Transit	Bus	Auto	Bus					
1	0.05	-0.05	-0.01	-0.83	-0.30	3.60	-1.33	0.03	-0.20	0	0	0	0.0021	-0.193
2	0.06	-0.04	0.00	-0.83	-0.32	3.60	-1.33	0.03	-0.21	3	-5	-2	0.0021	-0.564
3	0.07	-0.03	0.01	-0.84	-0.32	3.60	-1.32	0.04	-0.22	5	-2	3	0.0021	-1.148
4	0.08	-0.03	0.01	-0.83	-0.32	3.60	-1.31	0.03	-0.22	5	0	5	0.0021	-1.223
5	0.07	-0.02	0.02	-0.83	-0.32	3.60	-1.31	0.04	-0.23	5	2	7	0.0020	-1.257
6	0.08	-0.03	0.02	-0.83	-0.33	3.60	-1.30	0.04	-0.23	5	2	7	0.0020	-1.268
7	0.08	-0.02	0.02	-0.84	-0.33	3.60	-1.30	0.04	-0.23	4	2	6	0.0020	-1.257
8	0.08	-0.02	0.03	-0.84	-0.33	3.59	-1.30	0.04	-0.23	4	2	6	0.0020	-1.271
9	0.08	-0.01	0.03	-0.84	-0.34	3.59	-1.29	0.04	-0.24	4	1	5	0.0020	-1.263
10	0.08	-0.02	0.03	-0.84	-0.34	3.60	-1.29	0.03	-0.24	3	1	4	0.0020	-1.252
11	0.08	-0.01	0.03	-0.84	-0.35	3.60	-1.29	0.04	-0.24	3	2	5	0.0020	-1.240
12	0.08	-0.01	0.02	-0.84	-0.35	3.59	-1.28	0.05	-0.25	2	1	3	0.0020	-1.229
13	0.07	-0.02	0.03	-0.83	-0.34	3.58	-1.28	0.04	-0.24	2	1	3	0.0020	-1.220
14	0.08	-0.01	0.02	-0.83	-0.35	3.58	-1.28	0.05	-0.26	4	1	5	0.0020	-1.221
15	0.07	-0.01	0.03	-0.83	-0.36	3.57	-1.28	0.04	-0.25	0	1	1	0.0020	-1.203
16	0.03	-0.01	0.03	-0.83	-0.36	3.57	-1.28	0.05	-0.25	1	1	2	0.0020	-1.201
17	0.07	-0.01	0.02	-0.83	-0.35	3.57	-1.27	0.04	-0.26	1	1	2	0.0020	-1.202
18	0.07	-0.01	0.02	-0.82	-0.36	3.56	-1.26	0.04	-0.26	1	1	2	0.0020	-1.202
19	0.08	0.00	0.03	-0.82	-0.36	3.55	-1.27	0.05	-0.26	0	1	1	0.0020	-1.203
20	0.07	-0.01	0.02	-0.82	-0.36	3.55	-1.26	0.04	-0.26	1	1	2	0.0020	-1.201

TABLE 9: Aggregate results of the twenty year simulation of the Gulf Mobile & Ohio project for the metropolitan area.

¹ changes compared to the initial period

² changes from previous year

Year	Rent Change (%) ¹			Mode Demand Change (%) ¹							Housing Stock Change ²			Net Employee Change ²	
				CBD				Non-CBD			City	Suburb	Total	CBD	Non-CBD
	City	Suburb	Total	Auto	Rail	Transit	Bus	Auto	Bus						
1	2.17	0.70	1.52	-5.13	-2.17	62.79	-6.64	0.33	-2.70		0	0	0	533	-505
2	2.20	0.82	1.56	-5.15	-2.20	62.82	-6.61	0.33	-2.72		16	6	22	543	-489
3	2.21	0.85	1.58	-5.16	-2.23	62.82	-6.57	0.32	-2.67		12	4	16	547	-476
4	2.21	0.87	1.59	-5.17	-2.25	62.81	-6.53	0.32	-2.64		12	3	15	551	-466
5	2.21	0.89	1.59	-5.19	-2.28	62.80	-6.50	0.32	-2.62		12	2	14	554	-456
6	2.20	0.89	1.59	-5.18	-2.30	62.80	-6.47	0.33	-2.61		10	2	12	557	-440
7	2.18	0.89	1.59	-5.18	-2.32	62.76	-6.45	0.33	-2.61		8	2	10	559	-441
8	2.17	0.90	1.57	-5.18	-2.35	62.75	-6.43	0.34	-2.62		7	1	8	562	-435
9	2.14	0.89	1.56	-5.17	-2.37	62.73	-6.41	0.34	-2.63		8	1	9	564	-430
10	2.13	0.89	1.55	-5.16	-2.39	62.70	-6.40	0.35	-2.66		6	1	7	566	-424
11	2.11	0.89	1.54	-5.16	-2.41	62.65	-6.38	0.35	-2.67		5	1	6	568	-419
12	2.09	0.89	1.53	-5.14	-2.43	62.59	-6.37	0.36	-2.68		5	1	6	568	-416
13	2.07	0.88	1.52	-5.14	-2.45	62.51	-6.35	0.37	-2.70		5	1	6	570	-412
14	2.05	0.88	1.51	-5.12	-2.47	62.45	-6.33	0.37	-2.71		4	1	5	570	-408
15	2.04	0.88	1.49	-5.12	-2.48	62.37	-6.32	0.38	-2.73		3	0	3	571	-407
16	2.03	0.87	1.48	-5.11	-2.50	62.28	-6.30	0.39	-2.75		2	0	2	572	-404
17	1.99	0.87	1.47	-5.09	-2.51	62.20	-6.28	0.39	-2.77		1	0	1	572	-402
18	1.98	0.87	1.46	-5.08	-2.53	62.10	-6.27	0.40	-2.79		1	0	1	572	-401
19	1.96	0.87	1.44	-5.07	-2.55	62.01	-6.25	0.41	-2.81		1	1	2	571	-400
20	1.94	0.86	1.44	-5.06	-2.57	61.91	-6.25	0.41	-2.83		1	0	1	571	-398

TABLE 10: Aggregate results of the twenty year simulation of the Gulf Mobile & Ohio project for the southwest corridor.

¹ Changes compared to the initial period

² Changes from previous year

Policy	Operating cost	Capital & operating cost	Rent value captured	Rent & land value captured	Fare revenue	Fare revenue to operating cost ratio	Total value captured to capital cost ratio	Total value captured plus fare revenue to total cost ratio
GM&O	104,271	280,165	70,518	71,049	20,705	.199	.404	.328
GM&O Project with doubled CBD parking cost	104,383	280,277	52,315	52,669	27,061	.259	.299	.284
GM&O project with doubled gasoline price	104,290	280,184	62,179	62,635	21,806	.209	.356	.301

TABLE 11: Estimated costs and cost recovery ratios for the three policies obtained from the Dynamic Simulations (All values and costs in thousands in 1970 dollars. Interest rate used in discounting annual values to obtain value captured is 10%)