Working Paper

EVALUATIONS FOR INDUSTRIAL LAND-USE PROGRAM RELATED TO WATER QUALITY MANAGEMENT

Fumiko Seo Masatoshi Sakawa

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International Institute for Applied Systems Analysis A-2361 Laxenburg, Austria

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PREFACE

Since the early period of IIASA activity, researchers on multicriteria decision-making have been forming a core with which IIASA has been contributing to the academic world, and at present it is on a new line. The main characteristics of the complex problems facing humans today are multidimensional and multiple objective. They include noncommensurate and conflicting elements. In order to cope with these, multidisciplinary implementation must be performed. Systems analysis is an integrated approach to meet this request. Particularly in order to solve complex problems with conflicting objectives, an improvement in decision-making processes will be urgently expected.

In the System and Decision Sciences Area of IIASA, Decision Processes and Hierarchical Structure is one of the main projects in Task 1 Decision and Planning Theory. In this project, the emphasis is placed on making mathematical descriptions of hierarchical decision making processes and balancing conflicting objectives. Multiobjective mathematical optimization processes shall be combined with judgemental or coordinating processes. This paper is a part of the modest works which contribute to this direction. The numerical results have been obtained in cooperation with the Systems Engineering Department of Kobe University in Japan, from where Dr. Masatoshi Sakawa came to

IIASA and cooperated with Fumiko Seo. The authors are indebted to Mr. Kozo Tazumi of Kobe University for his excellent contributions to computational works.

ABSTRACT

For analyzing a regional land-use program based on water pollution control, a hierarchical modeling of multilevel systems The overall, large scale objectives complex is is presented. decomposed into functional as well as regional subsystems. device for coordinating and evaluating the sub-system is based on multiattribute utility analysis combined directly with dual variables obtained from mathematical programming. prices are used to derive the component criterion ("utility") functions which is a device for commensurating noncommensurate attributes. In the upper layer of the decision making system, uncertainty based on judgemental probability distributions is explicitly taken into consideration. This procedure is provided as a modified dynamic version of the nested Lagrangian multiplier method and is applied to the northern Senshu area in the Osaka prefecture of Japan.

1. INTRODUCTION

In this paper we are concerned with a regional land-use program combined with water quality management. The purpose of this paper is to present a methodology for planning, management and evaluation of the land-use program based on an industrial reallocation plan, in which economic growth and environmental management are compatible with each other. An illustration is also provided for a suburban area of southern Osaka, the northern Senshu area.

The objective area is the Otsu river basin in the Osaka prefecture. The Otsu river has three tributaries: the Makio (15,134m) the Matsuo (12,331m) and the Ushitaki (17,534m) rivers. These rivers have their origin in the Izumi mountains in the south-eastern border of the Osaka prefecture. The Makio and the Matso rivers flow through Izumi city and the Ushitaki river flows through the agricultural area of Kishiwada city. The Otsu river gathers water from these tributaries, passes through the border between Izumi otsu city and Tadaoka cho and finally flows into Osaka Bay (Figure 1). In Izumiotsu and Tadaoka cho, the southern part of the Sakai-Senboku (northern Senshu) coastal industrial complex is located. In Izumi city, residential, agricultural and forest lands cover a large area.

Among them some industrial plants are located. Thus, the region is a typical example of a regional complex problematique, which is interpreted as an objectives complex.

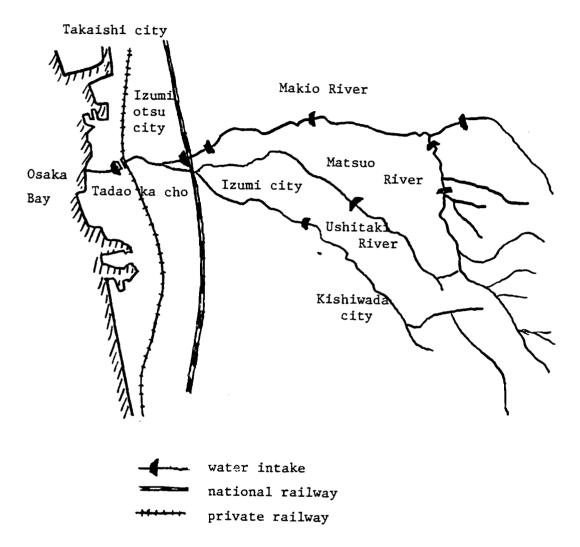


Figure 1. Map of the Otsu River Basin.

The object to be analyzed is large-scale because it includes many objectives and variables (instruments, i.e. the lowest-level objectives) which correspond to various kinds of multidisciplinary aspects. The object also has a complexity because the objectives and variables (instruments) are usually noncommensurate and in conflict with each other. This means that, generally, an overall supreme solution among Pareto-optimal solutions does not exist, which is a major characteristic of multidimensional criteria problems. A methodology for coping

with these difficulties has to be developed based on a multiobjective systems analysis.

In this paper, the nested Lagrangian multiplier method which has been developed by the authors (1977, 1979a, 1979b) is applied in a probabilistic and dynamic version. The main procedure of this method is based on a hierarchical configuration and decomposition of the large-scale complex problematique in multilevel systems. Based on the decomposed subsystems, water quality simulation processes are independently introduced and combined with a main program unit for industrial land-use Mathematical programming is applied to the main proprogram. gram unit in the linkage with the simulation unit. A dynamic loop for iterative evaluation and calculation of optimal solutions is used sequentially during each subperiod of the planning time horizon. The final result of the systems evaluation is presented in terms of the multiattributable utility functions. In the process of deriving the multiattribute functions, component utility functions (or utile index) are treated as uncertain Thus assessments of judgemental probability distriquantities. butions for component utility functions are executed. the expected values of the utility functions, the numerical values of the multiattribute utility functions are derived and calculated.

2. HIERARCHICAL MODELING

The regional complex related to water resources in the objective area, the Otsu river basin, is primarily shown in a model diagram (Figure 2). This diagram almost corresponds to the graphical location order.

For structuring the complex programatique, an overall regional system is decomposed into "independent" subsystems in multilevel. A hierarchical configuration is depicted in Figure 3. There is one main program unit and two subsidiary units: water quality simulation unit and agricultural planning unit. The hierarchical modeling of multilevel systems is composed of two strata. The first stratum is concerned with the analytical

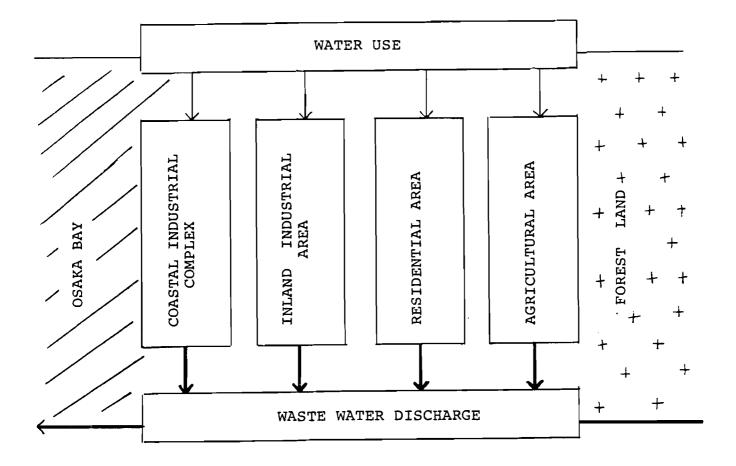
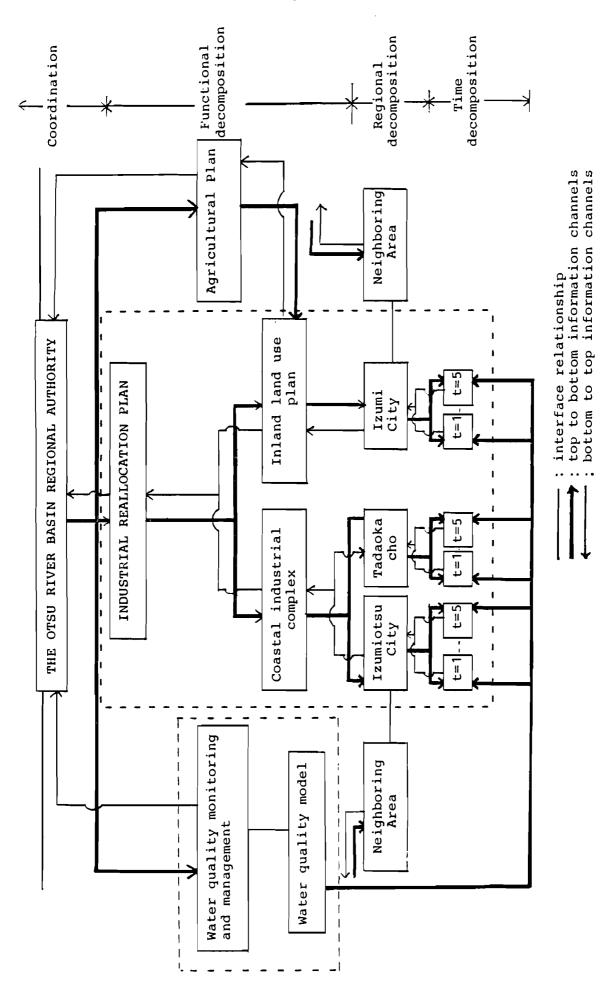


Figure 2. Model Diagram of the Otsu river basin.

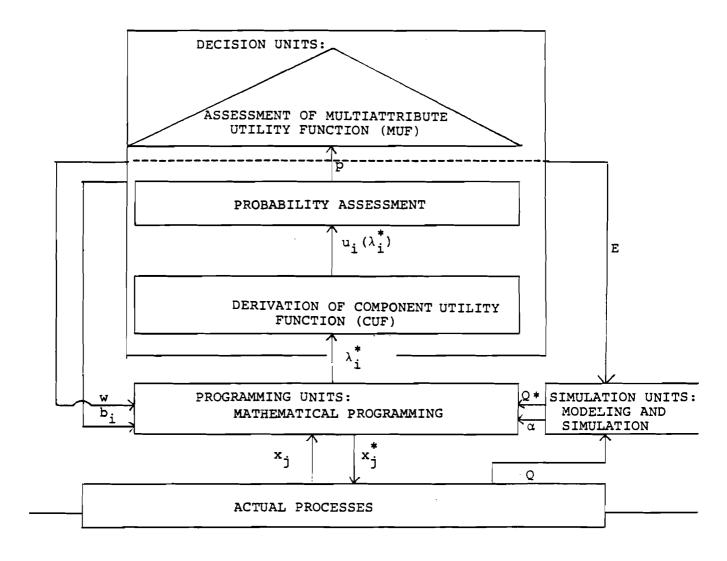
aspect of the system's behavioral description - optimization. The second stratum has a more ambiguous aspect - coordination, for which a subjective evaluation must be made. The analytical aspect is composed of the main program unit (two infimal levels in which regional and time decomposition are executed) and the subsidiary units. The coordination aspect is composed of three levels. The supremal coordination unit in the highest level is the (hypothetical) Otsu river basin regional authority. Infimal coordination units are composed of the two-level industrial reallocation planning in the main program unit and are in the same interface as the two subsidiary units. They correspond to a functional decomposition



Systems decomposition and hierarchical modeling in multilevel for the Otsu river basin. Figure 3:

In the main program unit, land-use programs connected with an industrial reallocation plan for each sub-region are formalized and evaluated. The main concern of the decision maker is to find a compatible way for environmental (water pollution) control and regional economic growth. The subsidiary units provide complementary information for modeling and evaluation of the land-use program. Main information channels have their counterflow in each level. Thus, iterative evaluation and calculation for obtaining optimal solutions are interactively executed through learning and adaption processes. This process forms a closed loop of the information channels via data inputoutput relationship.

Corresponding to the multilevel structurization of the problems, decision making processes are also depicted in multilevel systems (Figure 4). They are composed of two layers - operational and judgemental. At the first layer, the programming unit is concerned with mathematical programming for finding optimal solutions for resource allocations and related evaluations. The simulation unit is concerned with the modeling and simulation of water quality. At the second layer, decision units execute decision analysis in three levels. Assessment and evaluation of the degree of satisfaction for water quality management and economic growth in each region are performed in terms of the multiattribute utility function in which component utility values are treated as uncertainty quantities. Namely, the decision maker at the upper level takes account of the uncertainty with which the systems will be faced in all courses of the planning.



NOTATIONS:

Q - observed data set

 α - parameter set (for hard constraints)

Q* - refined data set

x; - primal optimal solution

 λ_i^* - dual optimal solution

u, - component utility function

b; - constraint constants

w - parameter set (for soft constraints)

x; - observed variables

U - multiattribute utility function

p - probability set

E - adjustment parameter set

Figure 4. Structure of multilevel decision making.

3. INTERACTIVE MATHEMATICAL PROGRAMMING

Mathematical programming for the major program unit is formulated in each sub-region: Izumi-otsu and Izumi cities and Tadaoka cho.

Maximize:

$$\sum_{j=1}^{\Sigma H_{j}} \int_{t_{0}}^{t_{1}} \sum_{j=1}^{n} A_{jt_{0}} e^{\mu_{jt}} K_{j}(t) \int_{t_{j}}^{\alpha_{j}} L_{j}(t) \int_{t_{0}}^{\beta_{j}} D_{j}(t) \int_{t_{0}}^{1-\alpha_{j}-\beta_{j}} dt$$
 (1)

Subject to:

$$\sum_{j=1}^{n} \left(k_j / d_{jto} e^{-\psi t} \right) D_j(t) \leq K(t) \qquad (t=1,...,5)$$
 (2)

$$\sum_{j=1}^{n} {\omega_{jto}} e^{-\rho t} / k_{j} K_{j}(t) \leq W(t) \qquad (t=1,...,5)$$
(3)

$$\sum_{j=1}^{n} L_{j}(t) \leq L_{to}e^{\eta_{t}}$$
 (t=1,...,5)

$$\sum_{j=1}^{n} D_{j}(t) \leq D^{U}$$
(t=1,...,5)

$$\left(K/L\right)_{j}^{L} \leq K_{j}(t)/L_{j}(t) \leq \left(K/L\right)_{j}^{U} \qquad (j=1,\ldots,n; t=1,\ldots,5) \quad (6)$$

$$K_{jto}^{-\pi_t} \leq K_{j}(t) \leq K_{jo} e^{\pi't}$$
 (j=1,...,n; t=1,...,5) (7)

$$L_{jto}e^{-\pi t} \le L_{j}(t) \le L_{jto}e^{\pi't}$$
 (j=1,...,n; t=1,...,5) (8)

where j is an industry and t is a planning subperiod. The objective function (1) is the sum of a local Cobb-Douglas-type production function for each industry. Hicks-neutral technological progress is included in each function. Capital value Kj, labour force Lj, and land Dj are decision variables.

In constraint (2), the variable $D_j(t)$ is related to a growth policy for total capital $K(t) = K_{to}e^{\hat{n}t}$. k_j is a capital coefficient and d_j is a land coefficient in each industry. In constraint (3), the variable $K_j(t)$ is related to a pollution control policy, W(t), which shows a target level of COD effluent discharge. ω_j is a unit load of COD per industrial shipment. ω_j and d_j are changed in each subperiod by a gradual reduction policy. These right-hand side constraint constants and indicative parameters are imposed by the second layer decisionmaker.

Constraint (4) shows that all the labour requirements do not exceed the predicted total labour supply. Constraint (5) shows upper bounds of total availability of land for industrial use. Constraint (6) is a technical constraint and shows upper and lower bounds of capital-labour ratio in each industry. Constraints (7) and (8) are frictional constraints and are set for avoiding radical changes of industrial structure. It is admissable for local decisionamkers to assign these constraint constants as their own policy. Actually indicative parameters are set as shown in Table 1.

Table 1. Indicative Parameters in Mathematical Programming

		Percentage change for time period (10 years)
ρ	0.032	(-) 15%
π	0.071	(-) 30%
π	0.139	(+) 100%
ψ	0.022	(-) 10%

In this problem, the constraints (2) and (3) are especially important because they are the main subjects of decisionmaking for the integrated regional planning. Thus, the problem is to find an optimal policy for resource allocation (capital, labour and land) for maximizing local industrial outputs under the conditions performing a prescribed economic growth policy and water quality control, considering the total supply of available labour forces and land resources. In the process of solving nonlinear mathematical programming, an evaluation for local economic growth and environmental management policy is provided with the dual optimal solutions which are combined with constraints (2) and (3). Thus, mathematical programming simultaneously provides the optimal resource allocation policy and its evaluation. In fact, the problem (1)-(8) has been solved iteratively in the time decomposition form. For solving nonlinear mathematical programming, Generalized Reduced Gradient Algorithm developed by Lasdon et al. (1974, 1975) is used.

In addition, iterative learning and adaption processes in a dynamic loop are also embedded in the optimization processes. Namely, the main program unit is combined with the simulation unit by receiving information on the pollutant discharge as an input and by sending information on the industrial shipments as In the simulation unit, an ecological water quality model is used for assessing interrelationships among ecological constituents based on self-purification mechanisms in the river. The river quality model, based on a chemical reaction between dissolved oxygen (DO) concentration and biochemical oxygen demand (BOD) concentration, is well-known as the Streeter-Phelps model. In ecological models which have recently been developed (Beck, 1978), more detailed information on ecological activities such as sunlight effects, water temperatures and photosynthetic activity of plant and algae is included. Beck has presented various types of the ecological model describing the ecological interrelationships and has provided some empirical results of simulation in the River Cam (1978, 1978b). According to his experiment, it is known that to include the algal population does not greatly improve the model fitting of the observed

system. Thus, for simulating self-purification mechanism of the freshwater river, the following model, based on the continuously stirred tank reactor (CSTR) idealization, is utilized on a day-by-day basis. (Beck and Young, 1975, 1976).

$$\dot{X}_{1} = -(\kappa_{1} + Q(\tau)/V) X_{1}(\tau) - \kappa_{2} X_{2}(\tau) +$$

$$+ (Q(\tau)/V) U_{1}(\tau) + \kappa_{1}C(\tau) + \kappa_{4}(h(\tau) - \overline{h}) + S$$
(9)

$$\dot{x}_2 = -(\kappa_2 + \kappa_3 + Q(\tau)/V) X_2(\tau) +$$

+
$$(Q(\tau)/V)U_2(\tau) + \kappa_5(h(\tau) - \bar{h}) + R$$
 (10)

where

$$h(\tau_k) = h(\tau_{k-1}) + 1/T[v(\tau_k)] \left\{ \frac{\theta(\tau_k) - \overline{\theta}}{\overline{\theta}} \right\}$$

$$-h(_{k-1})]$$
 , (11)

$$(h(\tau_k) - \overline{h}) = 0 \text{ for } h(\tau_K) < \overline{h} , \qquad (12)$$

$$h(\tau_0) = 0.0$$
 , (13)

and

$$C(\tau) = 14.5412 - 0.3928 \theta(\tau) - 0.0073[\theta(\tau)]^{2} - 0.000066[\theta(\tau)]^{3}$$
(14)

$$\tau_0 \le \tau_k \le \tau_{365}$$
 , $\tau_k - \tau_{k-1} = 1 \text{ (day)}$ (15)

In this model, it is assumed that there is no transportation delay. Measurement errors are also neglected.

Variables and parameters are explained in Table 2. Values of the parameters are almost similar to the River Cam's data because geographical conditions are not so different from each other. However, some corrections have been made for empirical data in the Otsu river during the whole year. Special consideration is given to the hot and humid weather conditions in Japan in the summer season. A time-series data for the sunlight hours $V(\tau_k)$ are shown in Appendix A.

The simulation output $X_2^*(\tau)$ of this model is used at the input data to the main program along with $Q(\tau)$ in summation. The input variables $U_1(\tau)$ and $U_2(\tau)$ are obtained from optimal values of the industrial shipment $H_1(t)$ which is the value of the production function, multiplied by the pollutant-load parameter $\omega_j(t)$. These values are iteratively revised in each planning subperiod $(t=1,\ldots 5)$.

On the other hand, the main program unit also obtains information on available land resources for the industrial use from the agricultural planning unit. Especially for Izumi city, which includes a large area of agricultural land, constraint constants in the equation (5) are treated as time-variants $D^{U}(t)$, $t-1,\ldots,5$, based on a revised industrialization plan which intends to slow down the conversion speed of agricultural land to industrial uses to less than in the past few years. Here again, iterative learning and adaption processes are also assumed. These interactive processes among the main program unit and two subsidiary units are depicted in Figure 5.

4. EVALUATION PROCEDURE

According to the nested Lagrangian multiplier (NLM) method (Seo 1977,1979), the dual optimal variables obtained in each subsystem are utilized as the basic factor of the system's evaluation. Utilization of Lagrangian multipliers (shadow prices) as a base of the system's evaluation has been developed by Haimes and Hall (1974), Haimes, Hall and Friedman (1975)

Table 2. Variables and Parameters.

VARIABLES and PARAMETERS	DEFINITION	VALUE
υ ₁ (τ)	influent DO concentration	input variable (gm ⁻³)
υ ₂ (τ)	influent SOD concentration	input variable (gm ⁻³)
x ₁ (τ)	effluent DO concentration	output variable (gm ⁻³)
x ₂ (τ)	effluent BOD concentration	output variable (gm ⁻³)
Q(τ)	volumetric flow-rate	121391 $(m^3 da\bar{y}^1)$. 39611 for τ_1, τ_2, τ_3 and afterwards for two days after every five days.
v	mean volumetric hold-up in the reach	121824 (m ³ day ⁻¹)
κ ₁	reaeration rate for DO	0.17(day ⁻¹)
κ ₂	BOD decay rate	0.32 (day ⁺¹⁾
κ ₃	BOD sedimentation rate	0.001 (day ⁻¹)
K 4	coefficient for sustained sunlight effect in 'DO equation	0.31 (gm ⁻³ day ⁻¹)
₹ 5	Coefficient for sustained sunlight effect in BOD equation	$0.32 (gm^{-3} day^{-1})$
h (τ)	sustained sunlight effect at day $\tau_{\mathbf{k}}$	equation(11) (hr. day ⁻¹)
ñ	threshhold level for sustained sunlight effect	6.0 (hr.)
C	saturation concentration of DO	equation (14) (gm ⁻³)
s	additional rate of DO by decomposition of bottom mud deposits	0.0 for $\tau_1 < \tau_k < \tau_{90}$ and $\tau_{335} < \tau_k < \tau_{365}$,
		-0.5 for $\tau_{91} < \tau_k < \tau_{151}$ and $\tau_{274} < \tau_k < \tau_{334}$
		-2.0 for $\tau_{152} < \tau_k < \tau_{181}$ and $\tau_{244} < \tau_k < \tau_{273}$
		-4.5 for $\tau_{182} < \tau_k < \tau_{243}$
v	hrs. of sunlight incident at day $\tau_{\mathbf{k}}$	time-series data (hr)
R	additional rate of BOD by local surface runoff	0.001 (gm ⁻³ day ⁻¹)
θ(τ)	stream water temperature	time-series data (°C)
3 ·	mean river water temperature	8.0 (°C)
T	time constant for discrete-time low-pass filter	4
$\mathbf{x_1}(\tau_0)$	initital condition for effluent DO concentration	9.0 (gm ⁻³)
$x_2(\tau_0)$	initital condition for effluent BOD concentration	4.9 (gm ⁻³)

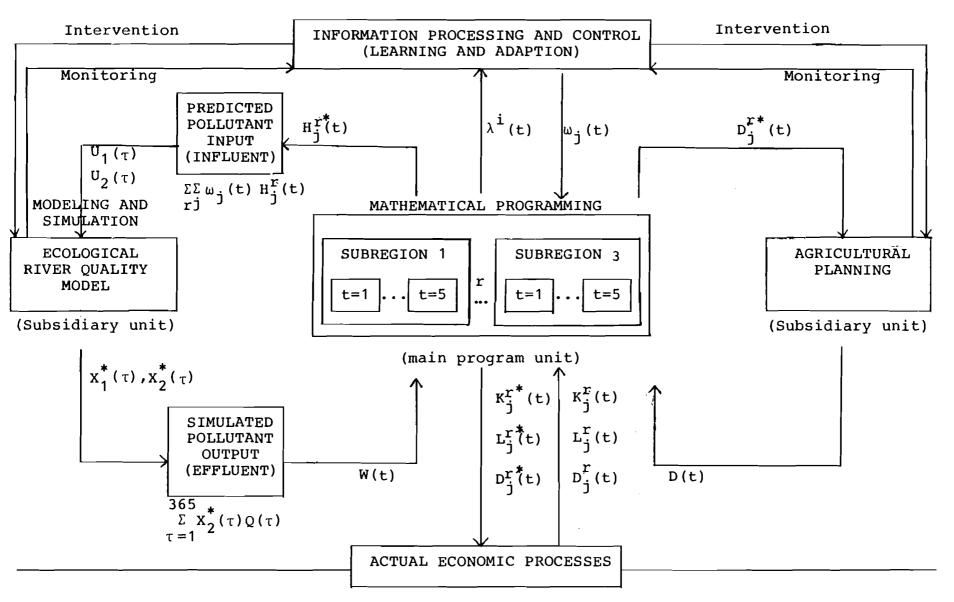


Figure 5. An interactive loop of regional planning.

In their method the shadow prices are mediately used via the trade-off rate functions. Worth functions are assessed simply with subjective judgement in ordinal scale.

In our method, it is asserted that numerical ordering of the shadow prices corresponds to preference ordering for local decisionmaking. This is because numerical values of the Lagrangian multiplier in optimal are regarded as an expression of the degree of marginal sacrifice of local objective functions in terms of constraint constants, which are imposed by the upper-level decisionmaker. Thus, the shadow prices are considered as a difficulty index for local decisionmakers in methematical terms, and used directly as inverse images of the utility functions (utile index). For numerically evaluating the difficulty index on a cardinal scale, the Lagrangian multipliers are positive-linearly transformed into normalized values from 0 to 1. With this device, noncommensurate attributes are measured in commensurate terms. We call the normalized values the component utility function.

Then trade-offs between each pair of numerical values of the component utility functions are examined. Based on the trade-off experiments and 50-50 chance lottery techniques, scaling constants are calculated. Multiattribute utility functions are derived using the component utility functions and the scaling constants. Raiffa (1968) and Keeney (1974), Keeney and Raiffa (1976) have greatly contributed to this aspect. However, in our method, the trade-off experiments are performed in terms of the normalized utility values, differing from the original device in which the experiments are in terms of the attributes.

Thus, in our method, the subjective or judgemental phase for the coordination processes of decisionmaking is immediately based on results from the mathematical phase for the programming processes. The basic evaluation factor is the shadow-prices as difficulty index for the management system, which is regarded as opportunity costs for interorganizational decision-making at multilevel. This device intends to minimize ambiguity which will be introduced into primal evaluation processes at lower levels of multi-layer systems.

Thus, in the original NLM method, values of the component utility functions which have been transformed from Lagrangian multipliers are treated as deterministic values.

However, decisionmaking for the coordination processes at upper levels of the multi-layer systems is much more complex. and uncertain or fuzzy elements must be included. As one device for such an inclusion, the values of the component utility functions are treated as uncertain quantities. Namely, expected values of the component utility functions with judgemental or hypothetical probability distributions are assessed and used for deriving the multiattribute utility functions at upper levels. Thus, hazardous factors in decisionmaking processes are introduced into systems evaluation.

The multiattribute utility functions are derived at multilevel. According to Fishburn-Keeney's representation theorems, the multiattribute utility functions are assessed in additive or multiplicative forms under the preferencial and utility independence conditions:

Additive form:

$$U\{\lambda(x)\} = \Sigma_{i}k_{i}\tilde{u}_{i} \{\lambda_{i}(x)\}$$
(16)

where

$$\Sigma_i k_i = 1, \quad 0 \leq U, \tilde{u}_i \leq 1$$

Multiplicative form:

$$U\{\lambda(x)\} = 1/K[\Pi_{i}\{K k_{i}\tilde{u}_{i}\{\lambda_{i}(x)\} + 1\} - 1]$$
 (17)

where

$$\Sigma_{i}k_{i} \neq 1$$
, $0 < k_{i} < 1$, $0 \le U$, $\tilde{u}_{i} \le 1$, $K > -1$

 λ is a vector of Lagrangian multipliers in optimal and $\lambda_{\mbox{i}}$ is an element in it. x is a vector of attributes. $\tilde{u}_{\mbox{i}}$ is an expected

value of the component utility function and U is a multiattribute utility function. $k_{\hat{1}}$ and K are scaling constants and obtained by the trade-off experiments and 50-50 chance lottery technique among the utility values. With nesting procedures, the multiattribute utility functions are derived one after another in the hierarchical systems. Actually the value $u_{\hat{1}}^{s}$ for the cumulative distribution function

$$F_i^s(u_i^s \leq \bar{u}_i)$$

is assessed for several fractiles of distribution. Schlaifer (1969,1970) has contributed to derive judgemental distribution functions and to computerize them. Expected values of the component utility functions with probability distribution function $f_i^s(u_i^s)$

$$\tilde{u}_{i} = Eu_{i} = \sum_{s} f_{i}^{s}(u_{i}^{s}) u_{i}^{s} ,$$

are used for calculating the multiattribute utility functions. Alternative experiments which take account of probalistic factors in any level of the utility functions are efficiently performed with ICOPSS/1 computer package which has been newly developed by the authors (Sakawa and Seo 1980a, 1980b).

Using these numerical values, spots where the difficulties for executing the integrated regional program exist are searched in the whole system. The results are utilized for better understanding of implications of the current management plan and for decision-aid for framing and evaluating more desirable alternative plans.

5. SOME NUMERICAL RESULTS

For obtaining numerical results, major industries in each sub-region have been chosen. The number of industries is nine in Izumiotsu, seven in Izumi and three in Tadaoka. Details are shown in Table 3.

Alternative plans for the integrated regional managementland use program are formed and evaluated over five planning periods (t=1,...,5). Active constraint constants for all the

Table 3. Selected industries in each subregion.

<u>Code</u>	Industry	<u>Izumiotsu</u>	Tadaoka	Izumi
18-19	Foods			0
20	Textile Mill products	0	0_	0
21	Apparel products	0		0
22	Lumber & related products		0	
24	Pulp & Paper products	0		0
26	Chemicals & related products	0		0
30	Clay & Stone products	0		
31	Iron and Steel	0		
33	Fabricated Metal products	0	0	0
34	Machinery	0	•	0
36	Transportation Equipment	0		
	To	tal 9	3	7

alternatives are shown in Appendix $\mbox{\scriptsize B}$. The selection of measurement units is crucial and assumed to be reasonable and practically meaningful.

Alternative I.

First, as one of the alternative land-use plans, a radical industrial reallocation program between coastal and inland areas is examined. The total capital formation at the end of the planning period will reduce about 18% in the coastal area (Izumiotsu and Tadaoka), but will increase about 26% in the inland area (Izumi). Connected with the industrial reallocation program in the coastal area, industrial land areas are reduced about 45 and 51% at the end of the planning period. In the inland area (Izumi city), the industrial land is decreased about 20%. The total volume of COD, which will be discharged into Osaka Bay, is reduced about 28%. The reduction rate ψ for land coefficient is 0.022 for industry code no. 21, 22, 24, 34 and 36 (-10% for five periods), and is 0.08616 for no. 18-19, 20, 26, 30, 31 and 33 (-35% for five periods). Other data are the same as in Table 1.

Results:

- (1) Among industries in Izumiotsu city, capital formation in machinery is increased and there are some aspects for increasing capitals in Fabricated Metal products as well as in Clay and Stone. Pulp and Paper and Iron and Steel industries are constantly decreased. In Tadaoka cho, capitals in Textile, Lumber and Fabricated Metal industries are constantly decreased. In Izumi city, capitals in Fabricated Metal and Machinery are increased. Because the production functions include Hicks-neutral technological progress, the total amount of industrial shipment will increase about 17% in Izumiotsu, 80% in Tadaoka and 45% in Izumi.
- (2) The results of water pollution control are shown in Table 4. As you see, the capacity of natural purification is rather large. Under the given conditions on the COD unit load ($\rho=0.032$), the waste water treatment rate for COD discharge is increased. However, required rates of treatment are less than 50% and the current capacity of sewage treatment plants will meet these requirements. Actually, water quality constraint constant W(t) has been changed in accordance with an adjustment parameter EPSI which is a reduction rate from the predicted value of COD discharge $\sum_{i=1}^{\infty} \omega_{i}(t) H_{j}^{r*}(t)$ in order to secure prescribed values of U_{2} in each planning period and the control parameter EPSI is set as follows:

$$\frac{\text{EPSI} \cdot \sum \sum \omega_{j}^{r}(t) H_{j}^{r}(t)}{365 \cdot Q(\tau)} = U_{2}(\tau)$$

With revised (gradually reduced) values of $\mathbf{U}_2(\tau)$ a simulation result:

365

$$\Sigma \quad x_{2}^{*}(\tau)Q(\tau)$$

 $\tau=1$

is calculated and assigned as constraint constant $w^{r}(t)$ for each subregion in the main programming unit. (Subscript r shows each subregion). A similar procedure is followed in other alternatives.

Table 4. Results of water pollution control (Alternative I).

					reduc	tion rate	
Period	^U 1	u ₂	х ₁	x ₂	via natural purification (BOD) 365 $\Sigma X_{2}(\tau)Q(\tau)$ $\tau=1$ 365	via control	(COD <u>w(t)</u> w(0)
					$ \Sigma U_2(\tau)Q(\tau) \\ \tau = 1 $	r j	
0 → I	12.0	6.4	9.0	4.9	% 23	7 [%]	6.3
I → II	11.1	5.9	8.5	4.6	23	22	13.5
II + III	10.4	5.5	7.9	4.3	22	27	17.1
III+ IV	9.6	5.1	7.4	4.0	22	39	22.9
in + n	8.9	4.8	6.9	3.8	21	47	27.8
Note:							
υ ₁ =	365 Σ Q τ=1	(τ) Մ.	1 (τ)	365 / Σ Q τ=1	?(τ)		
x ₁ =	365 Σ Q τ=1	(τ) Χ.	1 ^(τ)	365 / Σ Q τ=1)(τ)		
υ ₂ =	365 Σ Q =1	(τ)υ,	2 (τ)	365 / Σ Q =1	2(τ)		
x ₂ =	365 Σ Q =1	(τ) X	2 (τ)	365 / Σ Q =1	! (τ)		

⁽³⁾ Total labor force consistent with this plan will decrease about 16% in Izumiotsu, 1% in Tadaoka, and increase about 18% in Izumi. Thus, a labor force transfer from the coastal area to the inland area is predicted.

(4) The evaluation for this policy is shown in Table 5. Policy constraints on K(t) show much more difficulty in terms of the local objective functions than on W(t). Degrees of difficulty for the capital reallocation policy which is combined with a land-use policy are lowest in Izumiotsu at t=1,2, and in Tadaoka at t=3,4,5. This means that the guided capital reformation policy must be rearranged or some complementary means for performing it are required.

The difficulty of the land-use policy is at its worst in Izumi after t=2. This is a matter of course as, in Izumi, a growth policy for capital formation has been introduced. The capital growth policy has some effect on labor availability in Izumi; namely, although the difficulty in labor availability is fairly moderate until t=4, it is at its worst at t=5.

(5) Multiattribute utility functions and their numerical values at t=1,3 and 5 are evaluated in deterministic terms.

t=1

Izumiotsu:
$$U_{IO}(u_{w'}u_{K'}u_{D'}u_{L}) = 0.786$$

$$U_{IO} = \frac{1}{K}[(1+0.83K u_{w}) (1+0.2905K u_{K})$$

$$(1+0.249K u_{D}) (1+0.166K u_{L})-1]$$

$$K = -0.8516$$

Tadaoka:
$$U_{TA}(u_{w'}u_{K'}u_{D'}u_{L}) = 0.895$$

$$U_{TA} = \frac{1}{K}[(1+0.9K u_{w}) (1+0.315K U_{K})$$

$$(1+0.36K u_{D}) (1+0.225K u_{L})-1]$$

$$K = -0.9453$$

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In terms o	of t=1		t=2		t=3		t=4		t=5	
	λ	u	λ	u	λ	u	λ	u 	λ	u
IZUMI OTSU	<u>J</u>									
K(t)	0.3315	9.37×10 ⁻⁵	0.0674	9.15×10 ⁻⁶	0.370	0.0055	0.7349	0.0039	0.705	0.002
W(t)	1326.26	0.9468	1767.40	0.9296	29.410	0.9485	34.170	0.9759	35.560	0.960
L(t)	1.1730	6.95×10 ⁻⁴	1.206	6.08×10 ⁻⁴	1.969	0.0574	1.499	0.0261	2.259	0.045
D(t)	2.5953	1.71×10 ⁻³	2.046	0.0011	1.400	0.0390	0.960	0.0105	1.4033	0.022
TADAOKA K(t) W(t) L(t) D(t)	1.095 31.432 1.8324 6.1695	0.0063 0.9816 0.0300 0.1694	1.478 36.844 2.329 8.139	0.0049 0.9686 0.0280 0.1864		0.0033 0.9724 0.0272 0.1022	1.0247 63.730 2.594 6.488	0.0020 0.9801 0.0264 0.0872	1.660 79.790 3.135 9.633	0.002 0.984 0.020 0.102
IZUMI K(t)	1.176	0.0300	1.700	2 2275		0.0100	1.160	0.0122	1 220	0.007
W(t)	29.220	0.0229	1.720	0.0335		0.0186	1.160	0.0132	1.220	0.004
L(t)	1.670	0.9736 0.0397	32.590 2.390	0.9578 0.0536	36.850 11.288		42.03 o 2.236	0.9770 0.0386	50.733 1.4878	0.975

Izumi:
$$U_{IZ}(u_w, u_K, u_D, u_L) = 0.737$$

$$U_{IZ} = \frac{1}{K}[(1+0.75K u_w) (1+0.225K u_K) (1+0.2625K u_D) (1+0.1875K u_L)-1]$$

$$K = -0.7461$$

Region:
$$U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.908$$

$$U_R = \frac{1}{K}[(1+0.18K\ U_{IO})\ (1+0.9K\ U_{TA})\ (1+0.27K\ U_{IZ})-1]$$

$$K = 0.8398$$

t=3

Izumiotsu:
$$U_{IO}(u_w, u_K, u_D, u_L) = 0.830$$

$$U_{IO} = \frac{1}{K}[(1+0.87K u_w) (1+0.2871K u_K) (1+0.2175K u_D) (1+0.1305K u_L)-1]$$

$$K = -0.8672$$

Tadaoka:
$$U_{TA}(u_{W}, u_{K}, u_{D}, u_{L}) = 0.901$$

$$U_{TA} = \frac{1}{K}[(1+0.92 \text{K u}) (1+0.276 \text{K u}_{K})$$

$$(1+0.3496 \text{K u}_{D}) (1+0.184 \text{K u}_{L})-1]$$

$$K = -0.9492$$

Izumi:
$$U_{IZ}(u_w, u_K, u_D, u_L) = 0.777$$

$$U_{IZ} = \frac{1}{K}[(1+0.78K u_w) (1+0.2184Ku_K)$$

$$(1+0.2574K u_D) (1+0.156K u_L)-1]$$

$$K = -0.7578$$

Region:

$$U_{R}(U_{IO}, U_{TA}, U_{IZ}) = 0.851$$

$$U_{R} = \frac{1}{K}[(1+0.2975K U_{IO}) (1+0.2125K U_{TA}) (1+0.85K U_{IZ})-1]$$

$$K = -0.7929$$

t=5:

Izumiotsu:
$$U_{IO}(u_w, u_K, u_D, u_L) = 0.867$$

$$U_{IO} = \frac{1}{K}[(1+9.9 \text{K } u_w) (1+0.27 \text{K } u_K)$$

$$(1+0.18 \text{K } u_D) (1+0.09 \text{K } u_L)-1]$$

$$K = -0.875$$

K = -0.9609

Tadaoka:

$$U_{\text{TA}}(u_{\text{w}}, u_{\text{K}}, u_{\text{D}}, u_{\text{L}}) = 0.939$$

$$U_{\text{TA}} = \frac{1}{K}[(1+0.95\text{K } u_{\text{w}}) (1+0.2375\text{K } u_{\text{K}})$$

$$(1+0.3325\text{K } u_{\text{D}}) (1+0.1425\text{K } u^{\text{L}})-1]$$

Izumi:
$$U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.782$$

$$U_{IZ} = \frac{1}{K}[(1+0.8K u_{w}) (1=0.16K u_{K})$$

$$(1+0.24K u_{D}) (1+0.12K u_{L})-1]$$

$$K = -0.7109$$

Region:
$$U_{R}(U_{IO}, U_{TA}, U_{IZ}) = 0.907$$

$$U_{R} = \frac{1}{K}[(1+0.8K U_{IO}) (1+0.32K U_{TA}) (1+0.24K U_{IZ})-1]$$

$$K = -0.7524$$

Therefore, during the planning period, utility values are highest in Tadaoka and lowest in Izumi. This is mainly due to the fact that degrees of satisfaction for land constraints are highest in Tadaoka and lowest in Izumi $^{1/}$. Generally, utility values of each subregion are increasing, corresponding to the increase of scaling constants for $\mathbf{u}_{\mathbf{K}}$, $\mathbf{u}_{\mathbf{D}}$, and $\mathbf{u}_{\mathbf{L}}$.

^{1/} In the case where activeness of land constraints is neglected, the degree of satisfaction for the same policy is highest in Izumi and lowest in Izumiotsu (Seo and Sakawa 1980).

Alternative II.

In the second alternative plan, the industrial allocation policy between coastal and inland areas nearly follows current trends. Thus, in the coastal area (Izumiotsu and Tadaoka), the total capital formation increases about 22% and 28%. In the inland area (Izumi), the capital formation increases about 17%.

However, more radical land-use and water quality management policies are pursued. Namely, reduction rate ψ of the land coefficients is revised to 0.08618 for industry code no.24, 30 and 31 (i.e. -35% for five periods), to 0.1386 for no.18,19,20,26 and 30 (i.e. -50% for five periods), and to 0.022 for no.21,22, 34 and 36 (i.e. -10% for five periods). Reduction rate ρ for the COD unit load is increased to 0.05754 for all the industries (-25% for five periods).

Thus, industrial land areas are reduced about 29% in Izumiotsu, 20% in Tadaoka and 38% in Izumi. The total volume of COD, which will be discharged into Osaka Bay, is reduced about 30%.

Results:

- (1) Among industries in Izumiotsu, Alternative II allows an increase of capital formation in the Clay and Stone industry. The increase in Fabricated Metal is much more than Alternative I. The increase in Chemicals as well as the decrease in Iron and Steel is less than Alternative I. In Tadaoka, the capital formation in Lumber and Fabricated Metal industries increases. In Izumi, on the contrary to Alternative I, an increase in Chemicals is permitted. However, decreases in Textile and Apparel industries are more than Alternative I. The total amount of industrial shipment will increase about 45% in Izumiotsu, 133% in Tadaoka, and 15% in Izumi, until the end of the planning period.
- (2) The results of water pollution control are shown in Table 6. The capacity of natural purification for Alternative II is as effective as Alternative I. As a result of an overall capital growth policy, reduction rates for COD discharge are slightly increased to 54%.

Table 6.	Results	οf	water	pollution	control	(Alternative	II)
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				4	R	eduction rate	s
Period	^U 1	^U 2	х ₁	x ₂	via natural purification (BOD) 365	via control policy (COD)	(COD)
					$\begin{array}{c} \Sigma X_2(\tau)Q(\tau) \\ \tau = 1 \\ \hline 365 \\ \Sigma U_2(\tau)Q(\tau) \\ \tau = 1 \end{array}$	$\frac{\sum w^{r}(t)}{\sum \sum \omega_{j}H_{j}^{r*}(t)}$	<u>₩(t</u>) ₩(0)
0 → I	12.0	6.4	9.1	4.9	23 1/2	4 %	4.0%
I → II	11.3	6.0	8.5	4.6	23	25	10.9
II + III	10.4	5.5	7.9	4.3	22	38	17.2
III→ IV	9.8	5.2	7.5	4.1	22	45	21.9
IV + V	9.1	4.8	7.0	3.8	21	54	29.6

- (3) Total labor force for Alternative II increases about 23% in Izumiotsu and 9% in Tadaoka and decreases 30% in Izumi. Thus, a labor force transfer from the inland area to the coastal area will still continue. Moreover, capital intensive technological changes in Izumi will be especially induced.
- (4) The utility evaluations for this policy is shown in Table 7. Degrees of satisfaction for the regional planning are generally lowest for land resource constraints, differing from Alternative I. This is natural from the viewpoint of the radical reduction policy for land coefficients. In particular, the land resource policy has most difficulty in Tadaoka. This phenomena is combined with the highest rate of capital formation in Tadaoka.
- (5) Multiattribute utility functions and their numerical values at t=1,3 and 5 are evaluated in deterministic terms. For the evaluation, trade-off ratios or scaling constants for the component utility fuctions are the same as for Alternative I. Thus, forms and parameters of the multiattribute utility functions are the same as those in Alternative I.

POLICY EVALUATION (ALTERNATIVE II)

TABLE 7.

In terms of	t = 1	n	t=2	n	t=3	n	t=4 λ	n	t=5	a
IZUMIOTSU										
K(t)	0.4515	0.0901	0.5845	0.0185	0.634	0.0153	0.790	0.0107	0.9665	0.0202
W(t)	3.760	0.9384	30.459	0.9826	34.067	0.9732	36.515	0.9867	42.024	0.9772
L(t)	2.780	0.6872	1.4117	0.0452	1.587	0.0426	1.780	0.0377	2.00	0.0443
D(t)	0.224	0.0318	0.0148	0.0002	0.209	0.0031	0.531	0.0036	0.178	0.0018
TADAOKA										
K(t)	0.626	0.0084	0.788	0.0157	0.8615	0.0139	0.9193	0.0123	0.997	0.0107
W(t)	38.133	0.9776	49.20	0.9840	069.09	0.9771	74.265	0.9899	91.88	0.9877
L(t)	2.351	0.0530	2.492	0.0498	3.035	0.0489	3.80	0.0507	7.466	0.0480
D(t)	0.420	0.0031	0.002	2.0×10 ⁻⁵	1.58×10 ⁻³	1.58×10 ⁻³ 9.3×10 ⁻⁶	9.9×10 ⁻⁵	2.5×10^{-7}	1.68×10 ⁻⁴	1.68×10 ⁻⁴ 7.3×10 ⁻⁷
IZUMI										
K(t)	0.8705	0.0486	0.8343	0.0216	1.066	0.0248	0.9031	0.0375	1.057	0.1238
W(t)	13.287	0.9483	15.135	0,9440	39,625	7996.0	19.1613	0.9577	4.643	0.9205
L(t)	1.818	0.1172	1.977	0.0953	1.97	0.0469	1.388	0.0619	2.10	0.3555
D(t)	0.3465	0.0106	0.644	0.0093	0.0765	900000	0.1825	0.0011	0.73	0.0511

t=1

Izumiotsu:
$$U_{IO}(u_w, u_K, u_D, u_L) = 0.828$$

Tadaoka:
$$U_{TA}(u_w, u_K, u_D, u_L) = 0.883$$

Izumi:
$$U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.728$$

Region:
$$U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.901$$

t=3

Izumiotsu:
$$U_{IO}(u_w, u_K, u_D, u_L) = 0.850$$

Tadaoka:
$$U_{TA}(u_w, u_K, u_D, u_L) = 0.903$$

Izumi:
$$U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.759$$

Region:
$$U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.844$$

t=5

Izumiotsu:
$$U_{IO}(u_w, u_K, u_D, u_L) = 0.882$$

Tadaoka:
$$U_{TA}(u_w, u_K, u_D, u_L) = 0.939$$

Izumi:
$$U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.771$$

Region:
$$U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.915$$

General characteristics of utility values are almost similar to Alternative I. However, the degrees of satsifaction for Izumiotsu in Alternative II are higher than in Alternative I, and those for Izumi are lower. This is mainly due to the difference of the

degree of satsifaction for the capital formation policies which has been described above. (See Tables 5 and 7).

Alternative III.

In the third alternative plan, an overall capital growth policy is followed. It is worth noting that the growth rate increases to 29% in Izumi. Connected with this policy, industrial land area increases 6% in Izumi. Details of this plan are shown in Table 8 and compared with other alternatives. On the other hand, reduction rates of land coefficients are mitigated; namely the reduction rate ψ is 0.0220 for the industry code no.21,22, 34 and 36 (i.e. -10% for five periods) and 0.0446 for no.18-19, 20,24,26,30,31 and 33 (i.e. -20% for five periods). Reduction rate ρ for the COD unit load is the same as Alternative II.

Table 8. Alternative policies for the integrated regional management (ratios of constraint constants for t=5 to those for t=0)

	Alt	ernati	ive I	Alte	rnativ	re II	Alt	ernati	ve III
	<u>10</u>	TA	IZ	<u>10</u>	TA	<u>IZ</u>	<u>10</u>	TA	IZ
K(t)	% -18.3	% -18.6	% +25.8	% +22.1	% +27.8	% +17.1	% +21.9	% +28.4	% +29.4
W(t)	-27.8	-27.8	-27.8	-26.8	-26.8	-33.4	-36.7	-27.1	-27.1
L(t)	-16.3	- 1.3	+17.5	+23.0	+ 8.8	-29.4	-21.6	+ 3.0	+ 5.0
D ^u (t)	-50.8	-43.3	- 20.3	-29.0	-19.8	-38.5	-31.8	+ 2.4	+ 6.2

IO = Izumiotsu

TA = Tadaoka

IZ = Izumi

Thus, industrial lands will increase about 2% in Tadaoka and 6% in Izumi, but decrease about 32% in Izumiotsu. The total volume of COD which will be discharged into Osaka Bay is reduced about 31%.

Results:

(1) Among industries in Izumiotsu, capital formation in Iron and Steel, as well as Fabricated Metal industries, is decreased as much as in Alternative I. The increase in Chemicals

is also the same as in Alternative I and the decrease in Textile industry is as in Alternative II. The capital formation in Machinery increases less than in Alternative I and II. In Apparel, Pulp and Paper, and Clay and Stone industries, capital formation constantly decreases. In Tadaoka, predicted results are almost the same as in Alternative II. In Izumi, the decrease in Pulp and Paper, and Chemicals, is the same as in Alternative I, and the decrease in Apparel, and Fabricated Metal is the same as in Alternative II. However, in Izumi, an increase in Textile is permitted. The total amount of industrial shipment increases about 16% in Izumiotsu, 142% in Tadaoka and 58% in Izumi.

(2) The results of water pollution control are shown in Table 9. An overall capital growth policy which is the most generous among the three alternatives has an effect on reduction policy for COD discharge. Thus reduction rates of COD discharge to Osaka Bay amount to 56% at the final stage of the planning period.

Table 9. Results of water pollution control (Alternative III).

					1	Reduction rate	es
Period	^U 1	^U 2	x ₁	x ₂	via natural purification (BOD) 365		(CQD)
					$\sum_{\tau=1}^{\Sigma} X_{2}(\tau)Q(\tau)$	$\frac{\Sigma W^{r}(t)}{r}$	<u>W(t)</u>
					365 $\sum_{\tau=1}^{\Sigma} U_{2}(\tau)Q(\tau)$	ΣΣω H*r rj j j	W (0)
0 → I	-	6.9		4.9	% 23	% 5	% 4.9
I + II		5.9		4.6	23	29	15.7
II → III		5.5		4.3	22	33	17.4
III → IV		5.1		4.0	22	46	23.3
IV → V		4.8		3.8	21	56	31.4

- (3) Total labor force for Alternative III increases about 9% in Tadaoka, 5% in Izumi and decreases about 22% in Izumiotsu. This means that, in Izumiotsu, the capital intensive technological change in particular will be greatly induced.
- (4) The utility evaluation for Alternative III is depicted in Table 10. Degrees of satisfaction for this plan are the lowest for capital formation policy in Tadaoka and for land resource in Izumi. Difficulty in labour availability is at its worst in Izumi and this is combined with the highest rate of capital growth. This situation is almost the same for land resource policy.
- (5) First, multiattribute utility functions with the same scaling constants as other alternatives and their numerical values are evaluated in the deterministic terms at t=1,3 and 5.

t=1

Izumiotsu: $U_{TO}(u_w, u_K, u_D, u_L) = 0.833$

Tadaoka: $U_{m\lambda}(u_w, u_K, u_D, u_L) = 0.854$

Izumi: $U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.743$

Region: $U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.884$

t=3

Izumiotsu: $U_{IO}(u_w, u_K, u_D, u_L) = 0.839$

Tadaoka: $U_{TA}(u_w, u_K, u_D, u_L) = 0.912$

Izumi: $U_{IZ}(u_{w}, u_{K}, u_{D}, u_{L}) = 0.766$

Region: $U_R(U_{IO}, U_{TA}, U_{IZ}) = 0.847$

POLICY EVALUATION (ALTERNATIVE III)

TABLE 10.

In terms of:	C≡1	ם	ς γ	מ	ر د ا	מ	τ=4 γ	ם	C≝1 ~	ם
IZUMIOTSU									:}	
K(t)	0.503	0.1033	0.4879	0.0003	0.337	0,0068	0.455	0.0089	0.288	0.0040
W(t)	3.837	0.9582	1461.44	0.9976	33.58	0,9592	37.90	0.9488	21.47	0.9763
L(t)	2.059	0.5023	2.065	0,0013	2.16	0.0590	2.65	0,0640	19.95	0.9065
D(t)	0.1915	0.0235	0.178	5.5×10 ⁻⁵	0.8631	0.0219	0.1427	0.0011	2.511	0.1061
TADAOKA										
K(t)	0.265	0.0016	0.291	0.0018	0.218	2.87X10 ⁻⁴	0.1231	0.0003	0.04	0.0002
W(t)	37.80	0.9438	49.40	0.9889	61.27	0.9881	0.97	0.9715	93.30	0.9794
L(t)	2,33	0.0535	2.469	0.0456	3.0617	0.0463	3.83	0.0477	76:57	0.0520
D(t)	1.34	0.0286	1.343	0.0230	1.816	0.0261	2.40	0.0294	3.29	0.0343
IZUMI										
K(t)	0.769	0.0385	0.944	0.0191	0.7569	0.0157	0.888	0.0259	1.30	0,0134
W(t)	14.584	0.9724	33.79	0.9947	40.94	0.9761	21.893	0.9522	58.14	0.9684
L(t)	1,7836	0.1071	1.55	0.0371	1.811	0.0409	1.56	0.0556	2,125	0.0273
D(t)	0.307	0.0072	0.4179	0.0035	0.118	0.0004	0.36	0.0027	962.0	0.0050

t=5

Izumiotsu: $U_{IO}(u_w, u_K, u_D, u_L) = 0.902$

Tadaoka: $U_{TA}(u_w, u_K, u_D, u_L) = 0.932$

Izumi: $U_{IZ}(u_w, u_K, u_D, u_L) = 0.778$

Region: $U_R(U_{TO}, U_{TA}, U_{TZ}) = 0.925$

Compared to the other alternative plans, Alternative III is generally most acceptable. Namely, the degree of satisfaction of Alternative III for each sub-region is the best, or very close to the best among alternative plans, especially at the end of the planning period. For many cases in the other planning period, Alternative III is preferable, or almost preferable, to the other alternatives. The degrees of satisfaction for the overall region increase during the whole of the planning period.

Alternative I is least preferable for Izumiotsu and Alternative II is least preferable for Izumi.(Table 11).

Table 11. Ranking for degree of satisfaction of each alternative (AI, AII, AIII) among sub-regions).

	I	zumic	otsu	T	adac	ka	:	Izum	Ĺ	I	Regi	on
t	A1	AII	AIII	AI	AII	AIII	AI	AII	AIII	AI	AII	AIII
1	3	2*	1*	1	2	3	2*	3	1*	1	2	3
3	3	1	2	3*	2*	1	1*	3	2*	1*	3	2*
5	3	2	1	1*	1*	2	1*	3	2*	3	2	1

Note: * means almost the same as other alternatives for each sub-region.

(6) Now we will introduce probabilistic elements to the utility evaluation, namely the component utility values for Alternative III are treated as uncertainty quantities. Thus,

judgemental probability distribution for the prescribed values of the component utility functions are assessed at t=1,3 and 5. It is assumed that uncertainty is the largest in the beginning of the planning period and decreases up to the end of the period. Assessment of the judgemental probability distribution functions is performed in terms of cumulative functions, and their evaluations are effectively executed with CDISPRI computer program of MANECON collection (Schlaifer 1971). Characteristics of the probability distribution functions are listed in Appendix C and D.

Using these probability distribution functions, the expected values of the component utility functions are calculated.

Numerical values of multiattribute utility functions (MUF) based on the same scaling constants as the previous ones are also derived. The calculations can be more effectively executed with ICOPSS/I which is a new integrated computer package for subjective systems. Numerical results are listed in Table 12.

Compared with the deterministic cases, dispersement of the utility values for resource constraints is reduced. Consequently, MUF values for each sub-region are generally decreased. This is due to large weights on the water quality constraints which have high utility values but, in a probabilistic case, whose numerical values are reduced. In many cases, the utility values for land resource constraints increase and those for capital formation decrease. This is because uncertainty of capital formation is supposed to be larger than that of land constraints.

6. CONCLUDING REMARKS

Decision processes usually face uncertain or fuzzy elements. In this paper, the uncertaintry which is included in the industrial land-use program combined with water quality management has been treated in terms of probability distribution of the utility values for environmental constraint constants.

The nested Lagrangian multiplier method, which has been developed by the authors since 1977, is applied for evaluating the land-use prgram with some revision. Systems configuration has been constructed in two layers: operational and judgemental. In the first layer, a simulation unit is combined with a programming

Table 12.

COMMAND:	COMMAND:
=	*
INPUT ALT NAME:	= EVAL
= 0=0100-5	INPUT ALT NAME:
INPUT UTIL NAME (OR A	LL): = PERIOD-1
= ALL	INPUT UTIL NAME (OR ALL):
EVALUTION OF PERIOD-5	= ALL
NAME : UTIL VALU	
R : 0.8369	
IO : 0.7910	
*	IO : 0.6999
TA : 0.7935	
IZ : 0.6932	
IOW : 0.8442	
IOD : 0,0765	
IOK : 0.0464	
IOL: 0.7602	
TAW : 0.8255	
TAD : 0.0562	
TAK : 0.0416	
TAL : 0.0653	
1ZW : 0.8509	
IZD	
IZK : 0.0456	
IZL : 0.0527	17L : 0.1222

COMMAND:	
= EVAL	
INPUT ALT	NAME:
= PERIOD-	.3
INPUT UTI	L NAME (OR ALL):
= ALL	
EVALUTION	OF PERIOD-3
NAME	: UTIL VALUE
R	: 0.7204
	_: _ D.7128
TA	: 0.7606
_ <u>IZ</u>	: 0.6065
IOW	: 0.8049
IOD	÷ . 0.0475
IOR	: 0.0454
*	
IOL	: 0.0653
TAW	: 0.8140
TAD	: 0.0509
TAK	: 0.0417
TAL	: 0.0532
IZW	: 0.7553
170	: 0.0418
IZK	: 0.0498
IZL	: 0.0640

unit. A closed loop via input-output relationship is composed with intervention inputs of adjustment parameters from the decision maker in the second layer. With the intervention inputs, the programming unit can revise the data for water quality management based on simulation output from ecological modeling. Thus, learning and adaption processes are embedded in the decision making processes in the first layer. For further research, more prompt adaptation processes such as real-time control can be included in water quality management.

In the second layer, expected values of the multiattribute utility function can also be constructed. For this purpose, the way to assess probability functions must be further developed.

The nested Lagrangian multiplier method is one device for multiobjective systems evaluation. With this device, satisfaction degrees for prescribed policy plans are numerically compared among periods and alternatives as well as sub-regions and also the spots which have major troubles or difficulty are sought through all the systems. The information is utilized as a reference for better understanding of a prescribed policy and for installing some complementary or alternative means for improving the current situation.

Date	9					Ноц	ırs					
<u> </u>	Jan.	<u>Feb.</u>	Mar.	Apr.	May	<u>June</u>	July	Aug.	Sept.	<u>Oct.</u>	Nov.	Dec.
1	3.7	3.9	5.8	11.2	2.9	10.1	-	11.6	11.5	10.8	10.0	9.3
2	4.4	4.9	10.5	-	10.5	5.4	=	4.6	8.5	10.7	4.4	1.4
3	1.8	7.4	9.8	3.5	6.9	2.6	0.5	0.5	4.0	10.7	6.9	9.0
4	5.4	7.3	-	10.7	3.7	-	0.9	10,9	7.0	10.5	8.4	2.3
5	5.9	6.7	4.9	11.0	9.4	8.8	0.4	11.5	5.6		9.0	6.6
6	4.4	2.2	10.2	3.8	-	5.5	2.3	11.8	10.7	9.2	8.7	7.1
7	6.1	8.9	8.8	8.8	0.1	10.0	-	7.2	11.8	5.7	0.7	9.0
8	1.6	7.8	8.7	11.5	2.3	8.3	-	6.9	, X	7.4	7.8	8.3
9	1.9	0.3	5.4	10.6	4.2	4.9	-	9.7	10.0	6.6	7.8	6.6
10	3.3	0.8	3.4	9.7	_	3.0		12.6	6.7	6.8	8.5	4.8
11	4.6	2.5	8.4	1.3	0.1	-	1.7	12.7	6.4	8.3	2.1	3.8
12	7.6	0.1	6.7	4.5	11.2	0.7		12.1	0.4	9.7	0.3	8.9
13		3.9	6:6	2.6	7.0	4.2	2.1	8.3	9.3	3.3	0.1	7.3
14	7.1	5.2	8.6	11.4	9.6	5.6	3.3	12.1	2.9	. 7.9	8.7	4.5
15	8.3	3.8	5.9	9.6	6.2	2.8	3.7	11.1	7.1	· -	5.6	0.5
16	5.4	9.9	9.3	1.4	4.5		1.7	7.6	3.9	8.7	6.4	9.0
17	1.6	8.3	10.6	2.4	0.1	2.7	6.4	9.8	10.3	9.5	0.6	6.2
18	3.0	6.3	7.2	-	1.2	4.3	3,2	10.5	11.7	6.0	8.6	8.7
19	8.4	7.4	6.9	10.9	1.3	1.2	0.5	8.3	11.2	6.7	6.0	1.7
20 21	5.8	9.3	10.8	7.9	7.7	1.5	1.8	7.6	4.4	9.5	6.2	4.8
22	3.3	5.3	-	4.9	7.2	1.4	4.8	12.5	5.6	4.2	9.4	6.3
23	5.4	6.6	1.5	10.2	1.9	_	4.7	8.9	4.8	8.5	9.1	3.8
24	6.9	6.4	7.4	4.2	9.2		6.5	11.4	3.5	10.0	7.1	
2 4 25	- 8.5	9.1 0.3	11.1 9.8	0.7 6.0	9.6	0.1	3.8	9.5	6.4	6.4	8.0	7.3
26	5.4	9.1	10.2	12.0	4.0	1.4	X	11.8	8.4	8.7	9.0	9.0
27	8.5	8.3	1.3	11.2	9.6	-	11.2	11.4	7.5	1.4	0.2	8.8
28	0.5	1.9	-	5.3	7.7 1.0	1.6	12.7	11.4	0.5	1.2	2.1	3.1
29	7.0	1.9	10.8	0.1	0.1	1.5	11.2 6.1	11.0	1.4	0.2	2.2 2.9	3.6
30	6.3		9.0	8.6	0.4	-		11.1		8.4	6.1	6.9
31	7.7		9.9	8.0	3.9		12.1 12.7	8.8 9.7	7.8	9.9	0.1	7.2
Total	149.7	153.9	219.5	196.0	143.5	87.6	114.3	304.9	189.3	206.9	172.9	175.8

APPENDIX B: ACTIVE VALUES OF CONSTRAINT CONSTANTS

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	2	10921.	656.47	3689.7	3100.	82333.
	7	10864.	700.55	3847.7	3100.	73146.
	3	13414. 12495. 11638. 10841. 10864. 10921.	908.9 849.79 803.58 753.08 700.55 656.47	3737. 3948.0 3260.8 3948.0 3847.7 3689.7	5466. 3500.0 3100. 3100. 3100.	45540.54670. 55912. 65641. 73146. 82333.
<u>Tadaoka</u>	2	11638.	803.58	3260.8	3100.	55912.
Tade	-	12495.	849.79	3948.0	3500.0	54670.
	0	13414.	908.9	3737.	5466.	45540.
	2	21060.	2295.9	1. 11990. 8758.5	8592.1	.141817.
	7	21000.	2450.1	11990.	10100.	146830
	3	23841. 22361. 20829. 21000. 21060.	2960.9 2670.8 2633.8 2450.1 2295.9	9411.	10100 . 10100 . 10000 . 10100 . 8592.1	133058
ns	2	22361.	2670.8	11857. 11473. 9411	10100.	117335.
Izumiotsu	-	23841.	2960.9	11857.	10100.	115500.
	0	25773.	3178.8	10409.	17450.	$\sum_{j} H_{j}^{T}(t)$ 121114. 115500.117335.133058.146830.141817.
		K(t)	W(t)	L(t)	D ^u (t)	$\sum_{j} H_{j}^{\dagger}(t)$

	2	19648.	2170.4	10386.	10925.	141907	
	Ħ	14548. 13550. 15500. 17021. 19648	2837.9 2656.8 2489.8 2316.2 2170.4	6652.	10562.	116556	
	٣	15500.	2489.8	7101.	10250.	111760	
	2	13550.	2656.8	9981. 7548. 7101.	9539.6	103479	
	-	14548.	2837.9	9981.	11065.7 9539.6 10250. 10562.	$\sum_{j} H_{j}^{*}(t)$ 98163. 100603. 103479 111760 116556 141907	
Izumi	0	15617.	3004.8	.0488	13704.	98163.	
		K(t)	W(t)	L(t)	D ^u (t)	$\sum_{j} H_{j}^{*}(t)$	

	<u>Izumi</u>				
	1	2	3	4	5
K(t)	16093.	16583.	17088.	17608.	18291.
W(t)	2837.9	2677.5	2488.0	2346.4	2000.1
L(t)	8407.	8194.	8070.6	7995.9	6240.
$D^{\mathbf{u}}(t)$	11470.1	10410.4	9259.1	8306.8	8433.7
∑j ^H ; (t)	98141.	103933.	118992.	115538.	112707.

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Alternative III

	2	17224.	662.9	4066.	5600.	110087.
	⊅	16384.	700.0	4042.	5600.	95871.
	ო	15585.	750.9	4019.	5600.	83931.
ka	2	14825.	4.667	3995.	5600.	73029.
<u>Tadaoka</u> t	_	14102.	1018.2 799.4	3791.	5600.	. 48869
	2	31478.	2011.6	8165.3	11902.5	139925.
	7	30245.	2426.	8148.	17999.	142534.
	3	29058.	2626.4 2426.	9328.	16327.5	149406.
ns Ns	7	27920.	2539.6	9235.	15644.2 15646.3 16327.5 17999.	112835.
Izumiotsu	-	26825.	2887.1	9825.	15644.2	$\sum_{j} H_{j}^{*}(t)$ 111811. 112835. 149406. 142534. 139925.
		K(t)	W(t)	L(t)	D ^u (t)	$\sum_{j} H_{j}^{*}(t)$

	2	20215,	2191.6	9282.	14553.	155120.
	⇉	19799.	2313.4	7037.9	13568.	112089. 127867. 120995. 155120.
	က	17874.	2482.7	9102.	12137.	127867.
	2	17087.	2642.9	7756.	12741.	112089.
<u>Izumi</u>	_	16470.	2837.9	8197.	12875.	99538.
		K(t)	W(t)	L(t)	$D^{u}(t)$	$\sum_{j} H_{j}^{*}(t)$

Note: K(t) = million yen/year W(t) = ton/year L(t) = person $D^{u}(t) = 100m^{2}$ $H_{j}^{*}(t) = million yen/year$

```
Characteristics of the probability distributions
APPENDIX C.
             for component utility values
t=1: Izumiotsu ; uw
    VALUES OF UQ IN ASCENDING ORDER
    = 0 .73 .85 .90 1
    CUMULATIVE PROBABILITIES IN ASCENDING ORDER
    = 0 .25 .5 .75 1
   MEAN
                  0.791
   *
   STD DEV =
                   0.165
   VARIANCE =
                  U.273E-U1
   FRACTILES
     .UUI
                           -25
                          7300
     589
            1862
                   5890
                                 8500
                                        9000
                                               9368
                                                      9800
                                                             9937
        UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
   Izumiotsu: uk
  VALUES OF UQ IN ASCENDING ORDER
  = 0 .01 .035 .11 1
  CUMULATIVE PROBABILITIES IN ASCENDING ORDER
  = 0 .25 .5 .75 1
  OPTION?
  *
  = 1
                 0.096
                 0.153
  5!D DEV =
                 0.233E-01
  VARIANCE =
  FRACTILES
                  . 1
                         .25
   .001 .01
                                350 1100 2409 7600 9241
                  40
                         100
       UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 1DE-4
   Izumiotsu: u<sub>T.</sub>
 VALUES OF UQ IN ASCENDING ORDER
 = 0 .001 .005 .02 1
 CUMULATIVE PROBABILITIES IN ASCENDING ORDER
 ≈ 0 .25 .5 .75 1
 OPTION?
 := 1
       = 0.05i
MEAN
                0.140
 STD DEV =
 VARIANCE =
               0.196E-01
 FRACTILES
                                                     .99
                                                           .799
  .001
      UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
```

```
Izumiotsu: u<sub>D</sub>
     VALUES OF UQ IN ASCENDING ORDER
     ≈ O .07 .175 .4 1
     CUMULATIVE PROBABILITIES IN ASCENDING ORDER
     = 01.251.51.75 1
     OPTION?
     = 1
         ≂ 0.255
    MEAN
    STD DEV =
                0.227
    VARIANCE =
                 0.514E-01
    FRACTILES
     .001
            .01
                  . 1
                        .25
                                                     .779
                                    .75
                                          .9
                                                • 77
          28 280 700
                             1750 4000 6053 8744
                                                      9603
        UO VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
Tadaoka: uw
   VALUES OF UQ IN ASCENDING ORDER
   = 0.58.78.901
   CUMULATIVE PROBABILITIES IN ASCENDING ORDER
   = 0.25.5.751
   TOPTIONS
   = 1
               0.721
   MEAN
   STD DEV =
               0.220
   VARIANCE =
               0.483E-01
   FRACTILES
                                   .75
                       . 25
                            .5
    .001
          .01
                . 1
         UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
Tadaoka: uk
   VALUES OF UQ IN ASCENDING ORDER
   = 0 .CC05 .DC1 .CC15 1 ----
   CUMULATIVE PROBABILITIES IN ASCENDING ORDER
    <del>- 0 .05 .5 .75 1</del>
   OPTION?
   MEAN = 0.043
   STD DEV = 0.138
                <u>0.1915~01</u>
 ___FRACTILES _____
   .001 .01 .1 .25 .5 .75 .9 .99
                                               .99
                                                     .979
        UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 105-4
```

Tadaoka: uL

CUMULATI	_			ASCEND:	ING ORDE	R		
OPTION?	<u></u>							
MEAN	_=	0.066				<u>_</u>		
STD DEV		0.143 0.204E	-D1					
FRACTILE	S O1	4	25	ς.	75		50	220
*								

Tadaoka: u_D

	= 0 .001								
	* CUMULATI	VE PRO	BABILIT	IES IN A	SCENDIN	NG ORDE	:R		
	= 0 .25 OPTION?	.5 .75	1						
	= 1								_
	-								
	MEAN		0.053						
 -	MEAN STD DEV	=	0.053 0.141						-
		=		D1					
	STD DEV	=	0.141	- 01					
	STD DEV VARIANCE	=	0.141	.25	.5	.75	.9	. 79 .	.777

Izumi: uw

CUMULAT:	.75 .8 <u>IVE PRO</u>		CIES IN	ASCENDI	NG ORDE	<u> </u>		
= 0 .25	.5 .75	1						
OPTION?					·			
= 1								
MEAN		0.716						
STD DEV	=	0.197						
*								
VARIANC	=	0.3888	E-01		·- 			
FRACTIL	ES							
.001	-01	1	25	3	75		99	799
451	1426	4478	4000	7500	8700	9437	9898	9953
		—	_	7500 RE TO BE				9958

Izumi: u_k

* UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: u_L VALUES OF UQ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .C01 .01 .1 .25 .5 .75 .9 .99 .799 1 12 120 300 650 1500 2823 .7331 .5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: u_D VALUES OF UQ IN ASCENDING ORDER = 0 .C01 .D02 .C04 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1515-01 * ** ** ** ** ** ** ** ** ** ** ** **		= 0 .005 CUMULATI			IES IN	ASCENDI	NG ORDE	· ⇒		
### OPTIONS ### O						un 10ean leithean 11. haf air		·- y		
MEAN = 0.060 ST0 DEV = 0.140 VARIANCE = 0.197E-D1 FRACTILES .001 .01 1 .25 .5 .75 .7 .99 .99 .799 * UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 VALUES OF UQ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 ST0 DEV = 0.156 VARIANCE = 0.242E-D1 FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .799 1 12 120 300 650 1500 2823 .773: 9282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: uD VALUES OF UQ IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .005 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1315E-C1 ** ** ** ** ** ** ** ** ** ** ** ** *										=
STD_DEV =		= 1								
STD DEV = C.140		MEAN		0.060				 -		
FRACILES .001 .01 .1 .25 .5 .75 .7 .97 .977 0			_=							
.001 .01 .1 .25 .5 .75 .9 .99 .999 0 2 20 50 150 350 1441 7300 9144 **UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-9 IZUMI: U_L VALUES OF UQ IN ASCENDING ORDER = D .03 .065 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STO DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .59 .399 1 12 120 300 650 1500 2823 7731 5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 IZUMI: U_D VALUES OF UQ IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .001 .002 .004 1 OPTION? = 1 MEAN = 0.244 STO DEV = 0.138 VARIANCE = 0.1315-01 * ** ** ** ** ** ** ** ** ** ** ** **				0.197E	-01					
D 2 20 50 450 350 144: 7500 9144 * U0 VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 UALUES OF U0 IN ASCENDING ORDER							75			
UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 VALUES OF UQ IN ASCENDING ORDER = 0 .03 .065 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .97 .999 1 12 120 300 650 1500 2825 .731 5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 IZUMI: UD VALUES OF UQ IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 5 .75 1 OPTION? = 1 MEAN = 0.844 STD DEV = 0.138 VARIANCE = 0.1315-01 * FRACTILES * FRACTILES 0.15 .75 .75 .75 .75 .75 .75 .75 .75 .75 .7										
VALUES OF U@ IN ASCENDING ORDER						,				
VALUES OF U@ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .759 1			VALUES	JUST A	BOVE AS	E_TO_BE	LMULTIE	LIED BY	/_10E-4	
VALUES OF U@ IN ASCENDING ORDER = 0.03.045.15.1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0.25.5.75.1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .99 .999 1										
VALUES OF U@ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .759 1										
VALUES OF U@ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .759 1										
VALUES OF U@ IN ASCENDING ORDER = 0 .03 .045 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .759 1										
= D .03 .065 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .59 .79 .799 1 12 120 300 .650 .1500 1823 .731 .5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: uD VALUES OF U0 IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .05 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1515-01 * FRACTILES - 75 .757 .757	Izum	i: u _{r.}					•			
= D .03 .065 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .59 .79 .799 1 12 120 300 .650 .1500 1823 .731 .5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: uD VALUES OF U0 IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .05 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1515-01 * FRACTILES - 75 .757 .757										
= D .03 .065 .15 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .001 .01 .1 .25 .5 .75 .9 .59 .79 .799 1 12 120 300 .650 .1500 1823 .731 .5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: uD VALUES OF U0 IN ASCENDING ORDER = 0 .001 .002 .004 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .05 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1515-01 * FRACTILES - 75 .757 .757					STAC OF					
CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.122 STD DEV = 0.156 VARIANCE = 0.242E-01 * FRACTILES .CO1 .O1 .1 .25 .5 .75 .9 .99 .799 1 12 120 300 650 1500 2823 7731 5282 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumi: uD VALUES OF UQ IN ASCENDING ORDER = 0 .D1 .D02 .CO4 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.044 STD DEV = 0.138 VARIANCE = 0.1515-01 * FRACTILES	•				ING OR	DER				
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STD DEV = 0.138	Izum	i: uD VALUES 0 = 0 .001 CUMULATI = 0 .25 OPTION?	.002 VE PRO .5 .75	.004 1 BABILIT: 1	IES IN	DER ASCENDI	NG ORDE	R 		
STD DEV = 0.138	Izum	i: uD VALUES 0 = 0 .001 CUMULATI = 0 .25 OPTION? = 1	.002 VE PRO .5 .75	.GO4 1 BABILIT:	IES IN	DER ASCENDI	NG ORDE	R 		
VARIANCE = 0.1915-01 * FRACTILES75 .77 .77	Izum	i: uD VALUES 0 = 0 .001 CUMULATI = 0 .25 OPTION? = 1	.002 VE PRO .5 .75	.GO4 1 BABILIT:	IES IN	DER ASCENDI	NG ORDE	R 		
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** STD DEV = 0.162 VARIANCE = 0.263E-01 FRACTILES .OD1 .O1 .1 .25 .5 .75 .9 .99 .999 A13 1939 A131 7500 8A00 9100 945A 9830 994A UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumiotsu: u K VALUES OF UQ IN ASCENDING ORDER = 0 .Q01 .Q03 .Q1 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 DPIION? * = 1 MEAN = 0.047 STD DEV = 0.139 VARIANCE = 0.193E-01 FRACTILES .Q01 .Q1 .Q1 .1 .25 .5 .75 .9 .99 .995	ALIMIT ATT	.86 .9	1 1						
#EAN = 0.805 * STD_DEV = 0.162 /ARIANCE = 0.263E-01 FRACTILES .0D1 .01 .1 .25 .5 .75 .9 .97 .979 A13 1939 A131 7500 8A00 9100 9456 9830 9946 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumiotsu: u VALUES OF U@ IN ASCENDING ORDER = 0 .001 .003 .01 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 DPIION7 * = 1 MEAN = 0.047 STD_DEV = 0.139 VARIANCE = 0.193E-01 FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .995 0 0 4 10 30 100 1177 7210 9118	= 0 35	VE PRO	<u>BABILIT</u>	IES IN A	SCENDIN	G ORDE	R		
** SID DEV = 0.162 VARIANCE = 0.263E-01 FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .979 613 1939 A131 7500 8A00 9100 9454 9830 9944 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumiotsu: uk VALUES OF UQ IN ASCENDING ORDER = 0 .001 .003 .01 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 DPIION2 * = 1 MEAN = 0.047 SID DEV = 0.139 VARIANCE = 0.193E-01 FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .979 0 0 4 10 30 100 1177 7210 9118	- 0 .23	.5 ./5	1						
### DEV = 0.162 ### OPEN	MEAN	=_	0.805						
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ERACTILES .001 .01 .1 .25 .5 .75 .9 .99 .999 .613			0.162						
.001 .01 .1 .25 .5 .75 .9 .99 .979 613 1939 6131 7500 8600 9100 9456 9830 9946 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Izumiotsu: u VALUES OF UQ IN ASCENDING ORDER = 0 .001 .003 .01 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? * = 1 MEAN = 0.047 STD DEV = 0.139 VARIANCE = 0.193E-01 FRACTILES .001 .01 .1 .25 .5 .75 .9 .99 .999 0 0 4 10 30 100 1177 7210 9118			0.263E-	01				- 	
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RACTILES001 _01 _1 _25 _5 _75 _9 _9790				·O1					
<u>.001 .01 .1 .25 .5 .75 .9 .99 .999</u>									
			_1	. 25	5	.75	9	<u> </u>	999
UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4			•						9118
	<u> </u>	ALUES	JUST AB	OVE ARE	TO BE	MULTIPL	TED BA	10E-4	
Izumiotsu: u _T	Izumiots	nu: u _{T.}							
Izumiotsu: u _L	Izumiots	u: u _L							
VALUES OF UQ IN ASCENDING ORDER	VALUES (OF_UG_		NDING OF	<u>DER</u>				
VALUES OF UQ IN ASCENDING ORDER = 0 .005 .01 .05 1	VALUES (<u>of UQ</u> 5 .01	.05 i						
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER	VALUES (= 0 .005 CUMULATI	DF_U&_ 5 .01 IVE_PRO	.05 1 DBABILI			ING_ORD	ER		
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VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1	VALUES (= 0 .005 CUMULAT) = 0 .25 OPTION?	DF_U&_ 5 .01 IVE_PRO	.05 1 DBABILI			ING ORD	ΞR		
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1	VALUES (= 0 .005 CUMULAT) = 0 .25 OPTION? = 1	OF UQ 5 .01 IVE PRO .5 .75	.05 1 DBABILI 5 1	TIES IN		NG ORD	≅R		
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.065	VALUES () = 0 .005 CUMULATI = 0 .25 OPTION? = 1 MEAN	OF UG 5 .01 IVE PRO .5 .75	.05 1 DRABILI 5 1	TIES IN	ASCENDI				
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.065	VALUES (= 0 .005 CUMULATI = 0 .25 OPTION? = 1 MEAN STD DEV	OF UG 5 .01 IVE PRO .5 .75	.05 1 DBABILI 5 1 0.065 Q.144	TIES IN	ASCENDI				
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.065 STD DEV = 0.144 VARIANCE = 0.206E-01 ERACTILES	VALUES (= 0 .005 CUMULAT) = 0 .25 OPTION? = 1 MEAN STD DEV VARIANCE	OF UG 5 .01 IVE PRO .5 .75	.05 1 DBABILI 5 1 0.065 Q.144	TIES IN	ASCENDI				
VALUES OF UG IN ASCENDING ORDER = 0 .005 .01 .05 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN = 0.065 STD DEV = 0.144 VARIANCE = 0.206E-01	VALUES (= 0 .005 CUMULATI = 0 .25 OPTION? = 1 MEAN STD DEY VARIANCE FRACTILE	0F UG 5 .01 IVE PRO .5 .75	0.065 0.065 0.144 0.206	TIES IN E-O1	ASCENDI	.75	.9	. 79	

Izumiotsu: \mathbf{u}_{D}

	VALUES OF UG IN ASCENDING ORDER
	= 0 .003 .004 .01 1 cumulative probabilities in Ascending Order
	= 0 .25 .5 .75 1
	OPTION?
	= 1
	*
	<u>MEAN = 0.048</u>
	STD DEV = 0.138 VARIANCE = 0.191E-01
	<u>.001 .01 .1 .25 .5 .75 .9 .999 .999</u>
	0 1 12 50 60 100 1163 7206 9116
	UG VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 105-4
	······································
	·
	Tadaoka: u _w
	VALUES OF UQ IN ASCENDING ORDER
	= 0 .75 .87 .93 1
	CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1
	OPTION?
	= 1
	$ \frac{\text{MFAN}}{\text{STD DEV}} = \frac{0.814}{0.170} $
	STD DEV = 0.170 VARIANCE = 0.289E+01
	FRACTILES
	<u>.001 .01 .1 .25 .5 .75 .9 .99 .999</u>
	607 1920 6071 7500 8700 9300 9677 9925 9975
· #	ON VALUES JOST ABOVE ARE TO BE MOLITIFITED BY THE-4
	Tadaoka: ^u k
	VALUES OF UQ IN ASCENDING ORDER
	= 0 .00010 .00018 .00035 1
	CUMULATIVE PROBABILITIES IN ASCENDING ORDER
	=-0 .25 .5 .75 ! OPTION?
	oriton: = 1
	MEAN = 0.042 STD DEV = 0.138
	VARIANCE = 0.138 VARIANCE = 0.191E-01
- —	FRACTILES
	.001
	O O O 1 2 3 1040 7173 9104
	THE VALUES HER ABOVE ARE IN SECURE OF THE

VALUES 01 = 0 .005			DING ORE	ER				
CUMULATI			IES IN A	SCENDI	NG ORDE			
= 0 .25								
OPTION?								
= 1		_						
MEAN	=	0.063						
STD DEV	=	0.143						
VARIANCE	_=	0.204E	-01					
FRACTILES	3							
.001	01	. 1	.25	5	.75	.9	.99	<u>. 999</u>
0	2	20	50	100	450	1622	7351	9162
<u></u>	VAL <u>UES</u>	<u>JUST A</u>	BOVE ARE	TO BE	MULTIP	<u>LIED BY</u>	10E-4	
		•	•	••				
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Tadaoka: u _r)							

= 0 .00 CUMULAT	1 .005 IVE PRO .5 .75	.02 1 BABILIT	DING ORD		NG ORDE	₹		
= 1		_						
MEAN STD DEV		0.051		_				
VARIANO FRACTIL	E =	0.196E	-01					
*	- O 1	4	às.	E	75	0	- 99	000
0 <u>0</u>	0	4 JUST A	10 BOVE ARE	50 TO BE	200	1303	7250 10E-4	<u>.999</u> 9130

Izumi: u_w

	TIVE PR		TIES IN	ASCEND:	ING_ORDE	IR		
OPTION								
= 1		•						
MEAN	=	0.755		. <u>-</u>				
STD DE	<u> </u>	0.194						
VARIAN	CE =	0.378	E-01					
FRACTI	LES							
.001	.01	. 1	.25	.5	.75	. 9	.99	.79
483	1528	4795	450 <u>0</u>	8200	9000	9513	9874	9960

	ATIVE P		ITIES IN	ASCEND	ING ORG	ER		
OPTIO = 1	N?							
MEAN_		0.050					··	
STD D	EV ≃ NCE ≈	0.139 0.192						
FRACT								
001					.75		<u> 99</u>	39
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VALUES	. .		DING ORE)ER				
VALUES = 0 .0:	OF UQ I L O2 O TIVE PRO	4 1 BABILIT	DING ORD		IG ORDEF	₹		
VALUES = 0 .0:	OF UQ I L 02 0 IVE PRO	4 1 BABILIT			IG ORDEF	3		
VALUES = 0 .0: CUMULAT = 0 .25	OF UQ I L 02 0 IVE PRO	4 1 BABILIT			IG ORDER	₹		
VALUES = 0 .0: CUMULAT = 0 .25 OPTION:	OF UQ I L D2 D IVE PRO 3 -5 -75	4 1 BABILIT			IG ORDER	₹		
VALUES = 0 .01 CUMULAT = 0 .25 OPTION: = 1 MEAN STD DEV	OF UQ I 1 02 0 IVE PRO 3 5 .75	0.064 0.140	IES IN A		G ORDER	?		
VALUES = 0 .0: CUMULAT = 0 .2: OPTION: = 1 MEAN STD DEV	OF UQ I L 02 0 IVE PRO 5 5 75	DEABILIT	IES IN A		G ORDER	?		
VALUES = 0 .0: CUMULAT = 0 .2: OPTION: = 1 MEAN STD DEV VARIANCE FRACTIL	OF UQ I L 02 0 IVE PRO 5 5 75	0.064 0.140	IES IN A		. ORDER	. 9	.79	.799
VALUES = 0 .00 CUMULAT = 0 .00 OPTIONS = 1 MEAN STD DEV VARIANC FRACTIL .001	OF UQ I 1.02.0 IVE PRO 3.5.75 2.5.75	0.064 0.140 0.195E	-Q1 -25	SCENDIN	. 75 400	.9 1505	7314	9151
VALUES = 0 .00 CUMULAT = 0 .00 OPTIONS = 1 MEAN STD DEV VARIANC FRACTIL .001	OF UQ I 1.02.0 IVE PRO 3.5.75 2.5.75	0.064 0.140 0.195E	-Q1	SCENDIN	. 75 400	.9 1505	7314	9151

VALUES 0 = 0 .000				DER		_		
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 OPTION?	<u> </u>							
 = 1								
MEAN	<u>=</u>	0.042						<u>-</u>
STD DEV	=	0.138						
VARIANCE		<u>0.1915</u>	-01					
FRACTILE	E 3							
 .001	01	1	25	5		7		799
٥	0	1	2	3	5	1062	7173	9106
110	VALUES	JUST A	BOVE AR	TO 85	MULTIE	LIED SI	<u> </u>	

t=5:	Izumiotsu:	u_w
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	VALUES OF UQ IN A		DER				
	<u>= 0 .82 .88 .93 1</u>						
	CUMULATIVE PROBAG	BILITIES IN A	SCENDI	NG ORDER			
	= 0.25.5.751						
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	MEAN = U	. 844					
	*	٠					
	STD DEV = 0.	. 147					
	VARIANCE = 0.	.217E-01					
	FRACTILES						
		.1 .25	5	75	0	. 59	000
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	VALUES OF UQ IN A		ER				
	= 0.001.003.01			•	_		
	CUMULATIVE PROBAG	SILITIES IN A	45CENDII	NG ORDER			
	= 0.25.5.751						
	OPTION?						
	*						
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	- 1						
	MEAN = O.	.047					
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	FRACTILES						
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	_						
	VALUES OF UQ IN A	SCENDING ORD)ER				
	= 0.65.83.911						
	CUMULATIVE PROBAB	ILITIES IN A	SCENDIN	NG ORDER			
	= 0 .25 .5 .75 1						
	OPTION?						
	= 1 .						
							
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		760					
		199					
	VARIANCE = D.	397E-01					
	FRACTILES						
	FRACTILES	1 .25	5	.75	. 7	.74	. 7 4 7
	FRACTILES .001 .01 . 476 1507 47	1 .25 22 6500 ST ABOVE ARE	8300	9100	9597	9913	. 585 9973

Izumiotsu: up VALUES OF UQ IN ASCENDING ORDER = 0 .01 .02 .07 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 0 .25 .5 .75 1 OPTION? = 1 MEAN 0.077 0.145 STD DEV = 0.211E-01 VARIANCE = FRACTILES . 25 .001 .01 .75 100 200 700 1920 40 UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4 Tadaoka: u_w VALUES OF UQ IN ASCENDING ORDER = 0 .75 .90 .95 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = 1 OPTION? = 1 0.816 MEAN STD DEV 0.144 VARIANCE = 0.209E-01 FRACTILES -.5 .001 .01 . 25 9980 1861 5874 7500 9000 9500 7800 588 UQ VALUES JUST AROVE ARE TO BE MULTIPLIED BY 108-4 Tadaoka: uk VALUES OF UQ IN ASCENDING ORDER = 0 .00005 .00012 .0002 1 CUMULATIVE PROBABILITIES IN ASCENDING ORDER = .0 .25 .5 .75 1 OPTION? MEAN 0.042 0.138 STO DEV VARIANCE = 0.1915-01

FRACTILES .001

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UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4

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Tadaoka: u<sub>L</sub>
     VALUES OF UQ IN ASCENDING ORDER
     = 0 .005 .01 .05 1
     CUMULATIVE PROBABILITIES IN ASCENDING ORDER
     = 0 .25 .5 .75 1
     OPTION?
     = 1
                    0.065
     MEAN
     STD DEV =
                    0.144
     VARIANCE =
                    0.206E-01
     FRACTILES
                            .25
                                   .5
                                                .9
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                                                              .999
      .001
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         UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
    Tadaoka: u<sub>D</sub>
     VALUES OF UQ IN ASCENDING ORDER
     = 0 .003 .009 .03 1
     CUMULATIVE PROBABILITIES IN ASCENDING ORDER
     = 0 .25 .5 .75 1
     OPTION?
     = 1
     ¥
                    0.056
     MEAN
                    0.141
     STD DEV =
     VARIANCE =
                    0.197E-01
     FRACTILES
                                          .75
                                                        .99
                                                              . 999
      .001 .01
                                    90
                                                             9142
                      12
                             30
                                          300
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                1
          UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
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    Izumi: uw
    VALUES OF UQ IN ASCENDING ORDER
    = <u>0 .83 .91 .93 1</u>
    CUMULATIVE PROBABILITIES IN ASCENDING ORDER
    = 0.25.5.751
    OPTION?
    = 1
                   0.851
    MEAN
                   0.148
    STD DEV
                   0.219E-01
    VARIANCE =
    FRACTILES
                   77,799
     .001
             .01
                   7024
                                               9474
                                                     9833 9947
                          8300 9100 9300
         UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 108-4
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Izumi: uk
VALUES OF UQ IN ASCENDING ORDER
= 0 .003 .005 .006 1
CUMULATIVE PROBABILITIES IN ASCENDING ORDER
= 0 .25 .5 .75 1
OPTION?
= 1
MEAN
              0.046
              0.138
STD DEV =
              0.190E-01
VARIANCE =
FRACTILES
 .001 .01
                . 1
                       .25
                             .5
                                    .75
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                                                  .99
                       30
                15
                              50
                                     60
                                          1114
                                                 7190
                                                        7111
    UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 105-4
Izumi: u<sub>T</sub>
VALUES OF UQ IN ASCENDING ORDER
= 0 .005 .01 .02 1
CUMULATIVE PROBABILITIES IN ASCENDING ORDER
= 0 .25 .5 .75 1
OPTION?
= 1
               0.053
MEAN
STD DEV =
               0.139
VARIANCE =
               0.193E-01
FRACTILES
                       . 25
                             -.5
                                           .9 .99 .799
                                    .75
 .001
         .01
                . 1
                      50 100
                                    200
               20
          2
                                          1280
                                                 7242
     UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 10E-4
Izumi: uD
VALUES OF UQ IN ASCENDING ORDER
= 0 .0017 .0035 .0055 1
CUMULATIVE PROBABILITIES IN ASCENDING ORDER
= 0 .25 .5 .75
OPTION?
MEAN
               0.045
STD DEV
               0.138
               0.191E-01
VARIANCE =
FRACTILES
                                                        .999
                                                  .99
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    UQ VALUES JUST ABOVE ARE TO BE MULTIPLIED BY 1GE-4
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- +	APPENDIX D:
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VALUES ON UG AXIS ARE TO BE MULTIPLIED	
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VALUES ON UG AXIS ARE TO BE MULTIPLIED	1.0
VALUES ON UG AXIS ARE TO BE MULTIPLIED	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20*	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
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VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 .10 .2 .4 .6 .8 .10 .4 .8 .10 .4	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for
VALUES ON UG AXIS ARE TO BE MULTIPLIED .0 .2 .4 .6 .8 20	(d) cumulative function for

APPENDIX E.. PARAMETERS OF PRODUCTION FUNCTIONS (α_j, β_j)

	Izumiotsu			Tadaoka			Izumi			
Industry code	αj	βj	$1-\alpha_{j}-\beta_{j}$	άj	βj	$1-\alpha_{j}-\beta_{j}$	αj	βj	1-α _j -β _j	
18-19	-	-	-	-	-	•	0.7349	0.0754	0.1879	1
20	0.7143	0.1386	0.1471	0.7280	0.1220	0.1500	0.7284	0.1217	0.1499	56
21	0.6423	0.2046	0.1531		-	-	0.6045	0.2479	0.1476	1
22	-	-	-	0.6776	0.1320	0.1904	-	-	-	
24	0.6375	0.1897	0.1728	-	-	-	0.6775	0.1387	0.1838	
26	0.7552	0.1146	0.1302	-		-	0.7842	0.0807	0.1351	
30	0.7700	0.0717	0.1583		-	••	-	_	-	
31	0.7439	0.0886	0.1675	-	-	_		_	_	
33	0.6041	0.1152	0.2807	0.5561	0.1849	0.2590	0.5627	0.1757	0.2616	
34	0.6588	0.1839	0.1573	-	-	-	0.6540	0.1902	0.1558	
36	0.5556	0.2017	0.2427	-	_	_		_	_	

APPENDIX F . PARAMETER OF PRODUCTION FUNCTIONS ($\mu_{\mbox{\scriptsize j}}$) AND CONSTRAINT CONSTANTS

	j			ωjto_	djto	kj			
	Izumiotsu	Tadaoka	Izumi			Izumiotsu	Tadaoka	Izumi	
18-19	-	-	0.07842	0.08488	0.0692	-	-	0.1604	
20	0.06411	0,16577	0.10387	0,03353	0.1516	0.1507	0.2861	0.1718	
21	0.0	-	0.11157	0.03353	0.1068	0.1229	-	0.2099	
22	_	0.0	-	0.00153	0.0608	_	0.2546	-	
24	0.0	-	0.02091	0.23368	0.0765	0.1479	_	0.1121	
26	0.14946	-	0.08551	0.07689	0.1952	0.4876	_	0.1199	
30	0.0	-	-	0.00213	0.3107	0.18805	_	-	(J)
31	0.0	-	-	0.00633	0.1086	0.4318	-	-	57
33	0.08893	0.0	0.0	0.00125	0.1442	0.4738	0.1093	0.2731	1
34	0.10825	-	0.04711	0.00089	0.0966	0.3179	-	0.2421	
36	0.0	-	-	0.00079	0.0681	0.1516	-	-	

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