

# 1 The structure and control strategies of hybrid solid gravity energy 2 storage system

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## 10 Abstract

11 Hybrid energy storage is an interesting trend in energy storage technology. In this paper, we propose a hybrid solid  
12 gravity energy storage system (HGES), which realizes the complementary advantages of energy-based energy  
13 storage (gravity energy storage) and power-based energy storage (e.g., supercapacitor) and has a promising future  
14 application. First, we investigate various possible system structure schemes for the proposed HGES. In particular,  
15 we also obtained two superior system structure approaches through comparative analysis for two typical application  
16 scenarios, distribution and transmission grids. Subsequently, we theoretically analyze and mathematically model the  
17 energy conversion relationship of HGES based on different subsystems. More specifically, we discuss the control  
18 strategies of HGES in detail at three levels: power electronics, single-type energy storage system, and hybrid energy  
19 storage system. In addition, we propose complementary capacity configuration schemes for power-based energy  
20 storage systems based on the control strategies. Finally, the proposed HGES structures, control strategies, and  
21 capacity configuration schemes for distribution and transmission grid scale are simulated and verified based on  
22 MATLAB/Simulink. The results show that the proposed hybrid energy storage system has the advantages of both  
23 energy-based and power-based energy storage, which significantly improved compared to single energy storage  
24 technologies.

25 *Keywords:* Hybrid Energy Storage; Gravity Energy Storage; Power-Based Energy Storage; Control Strategies;  
26 System Structure

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## 27 1 Introduction

28 In order to fight global warming, more and more renewable energy sources are connected to the  
29 power grid to reduce the use of traditional fossil energy. However, wind and solar energy depend on  
30 natural factors and cannot be controlled by humans. Consequently, the imbalance between power supply  
31 and demand poses a significant challenge to the stable operation of power systems[1-3].

32 The traditional power system includes five major segments: power generation, transmission,  
33 distribution, transformation, and consumption[4, 5]. The supply and demand of electric energy must  
34 ensure real-time balance. Applying energy storage in the new power system changes the power system

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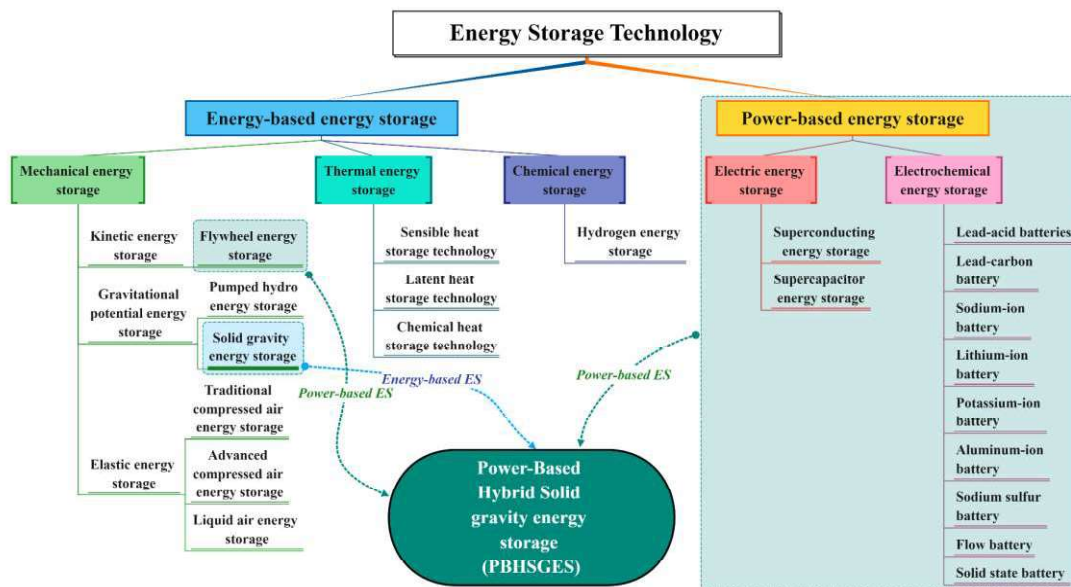
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35 from a stiff system to a flexible system, with greater flexibility, which is necessary for large-scale  
 36 renewable energy access[3, 6-8].

37 According to the energy form, energy storage technology can be divided into mechanical, electrical,  
 38 electrochemical, chemical, and thermal energy storage[9]. Further, mechanical energy storage, chemical  
 39 energy storage, and thermal energy storage have the characteristics of large-rated capacity and can be  
 40 classified as energy-based energy storage technology. On the other hand, electric and electrochemical  
 41 energy storage has high-rated power and can therefore be classified as power-based energy storage  
 42 technology, as shown in Fig. 1[10].

43 Given that different types of energy storage technologies have different characteristics, hybrid  
 44 energy storage technology combines different energy storage technologies (especially the combination  
 45 of energy-based and power-based technologies) to achieve technical complementarity, effectively  
 46 solving the technical problems caused by the only use of a single energy storage technology[7, 11, 12].  
 47 Considering that a lack of research has systematically investigated the system structure and control  
 48 strategies of hybrid gravity energy storage, we conducted the research in this paper.

49 In the second part of this paper, we combine gravity energy storage (energy-based energy storage,  
 50 hereinafter referred to as GES) and power-based energy storage, then propose a power-based hybrid  
 51 gravity energy storage system (PBHSGES, after this referred to as HGES). We discuss various possible  
 52 structures of the hybrid system and obtain a system structure suitable for two typical application scenarios:  
 53 distribution and transmission grids. Then the third part quantitatively analyzes the energy flow  
 54 characteristics in the system. In the fourth part, the control strategies of the power electronics in the  
 55 HGES, including the machine side inverter, the grid side inverter, and the DC/DC converter, are  
 56 investigated at the device level, and the coordination of the control is also discussed. In the fifth part,  
 57 focusing on the single energy storage system level, the power-based energy storage in the hybrid gravity  
 58 storage system is studied, and three control strategies and their capacity configuration schemes are  
 59 proposed. The sixth part discusses the overall control scheme from the hybrid energy storage system  
 60 level. Finally, the proposed system structure approach, control strategies, and capacity configuration  
 61 schemes for two typical application scenarios (distribution and transmission grids) are simulated and  
 62 verified based on MATLAB/Simulink.



63

64

Fig. 1. Relationship between different energy storage technologies and hybrid gravity energy storage

## 65 2 System structure of HGES

66 This chapter first introduces a new energy-based energy storage technology, solid gravity energy  
67 storage, then gives the basic composition of the HGES, and finally quantifies the energy conversion  
68 relationship of the proposed hybrid system.

### 69 2.1. Introduction of solid gravity energy storage

70 The current energy storage technologies that can be applied on a large scale include pumped storage,  
71 battery storage, and compressed air storage. Pumped storage has a long construction period, high cost is  
72 limited by geography and water resources, and cannot meet the needs of the rapid development of  
73 renewable energy[13, 14]. Battery energy storage can be used in large-scale scenarios, resulting in a  
74 complex control system that can reduce operational reliability and pose significant safety risks[15-18].  
75 The cycle efficiency of conventional compressed air energy storage is limited to less than 70% and  
76 requires fossil fuels due to the inherent loss of the volume change of the gas[19-21].

77 GES technology is a forward-looking technology for achieving large-scale clean energy storage,  
78 which has been honored by the World Economic Forum as one of the 2020 Technology Pioneers for its  
79 high safety and reliability (similar principle to pumped storage), environmental friendliness (no harmful  
80 chemical materials and no damage to the natural environment), and high sustainability of energy  
81 storage[9, 22, 23].

82 Both gravity storage and pumped storage are typical energy-based energy storage technologies that  
83 achieve large-scale electricity storage through conversion between electrical energy and gravitational  
84 potential energy. The storage medium of pumped storage is water, which can achieve stable power output  
85 by using continuous water flow to push the turbine. The storage medium of GES technology is modular  
86 and discrete weights, which causes the motor to repeatedly start and stop, resulting in a significant loss  
87 and noticeable output power fluctuation. Therefore, it reduces the GES system's cycle efficiency and is  
88 unsuitable for the power grid's stable operation.

89 GES technology is still in the early stage of development. The literature [9] has reviewed GES  
90 technology and summarized eight types of current GES technology, as shown in Fig. 2, readers interested  
91 in this can refer to the literature [9] and [10]. Abstracting various technical routes of GES, the essential  
92 operation principle of GES can be obtained: when the electric power of the power system is in excess,  
93 the GES system absorbs the electricity through the motor and lifts the weight; when the electric power  
94 of the power system is insufficient, the GES system puts down the weight and drives the motor to send  
95 out the electricity, which is fed back to the power system[24-31].

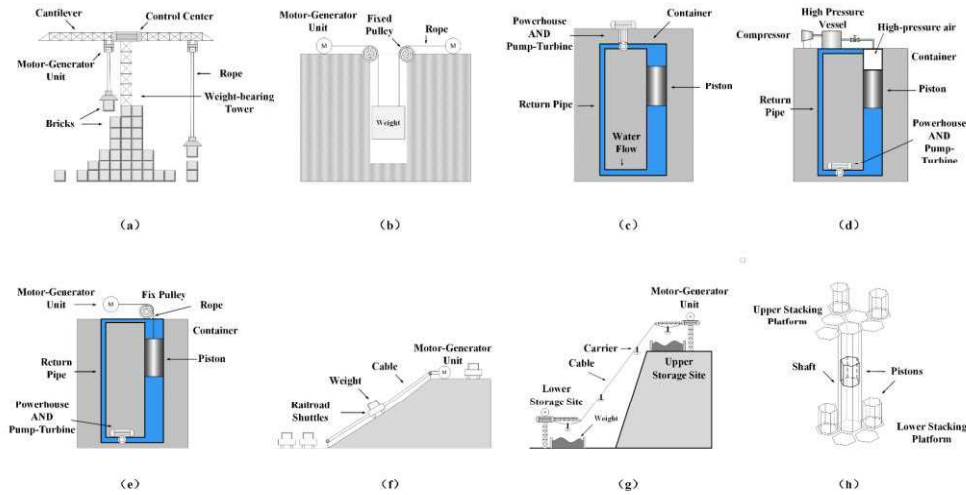


Fig. 2. Schematic diagram of a typical gravity energy storage technology route [10]

### 2.2. The basic structure of HGES

This paper combines GES and power-based energy storage to solve the technical problems of GES technology in the prior art, where repeated starting and stopping of the motor tends to cause large losses and also leads to significant fluctuations in output power.

The basic structure of HGES includes a GES module and a power-based energy storage module, as shown in Fig. 3. The GES unit, as energy-based energy storage, provides a large enough storage capacity for absorbing excess power from the grid or releasing power when the grid power is insufficient. The power-based energy storage module can be composed of any of the power-based energy storage technologies in Fig. 1, whose primary role is to provide a sufficiently large rated power for compensate the fluctuating amount of active power during the operation of the GES device mentioned or to provide fast power support to the grid at the millisecond scale or above.

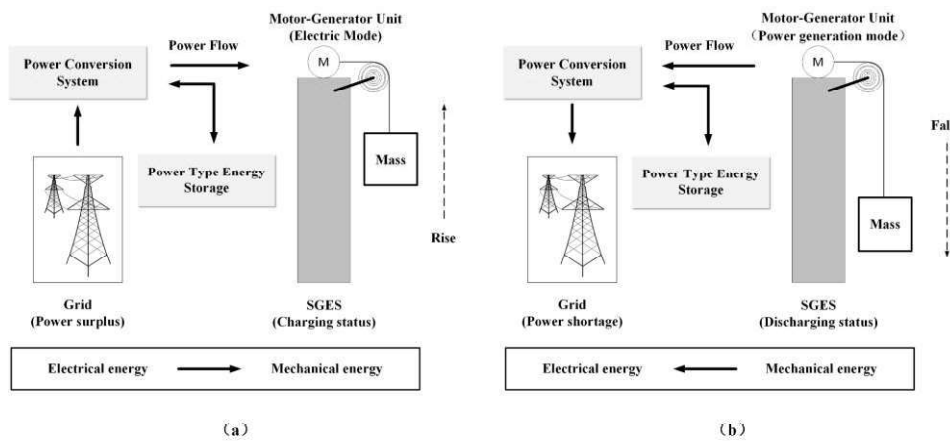


Fig. 3. Schematic diagram of the basic structure and operation principle of HGES

### 2.3. Types of HGES

According to the type of motor, the electric drive equipment, the grid access method, the power-based energy storage access position, and the approach, the HGES has diverse structural composition, as shown in Fig. 4.

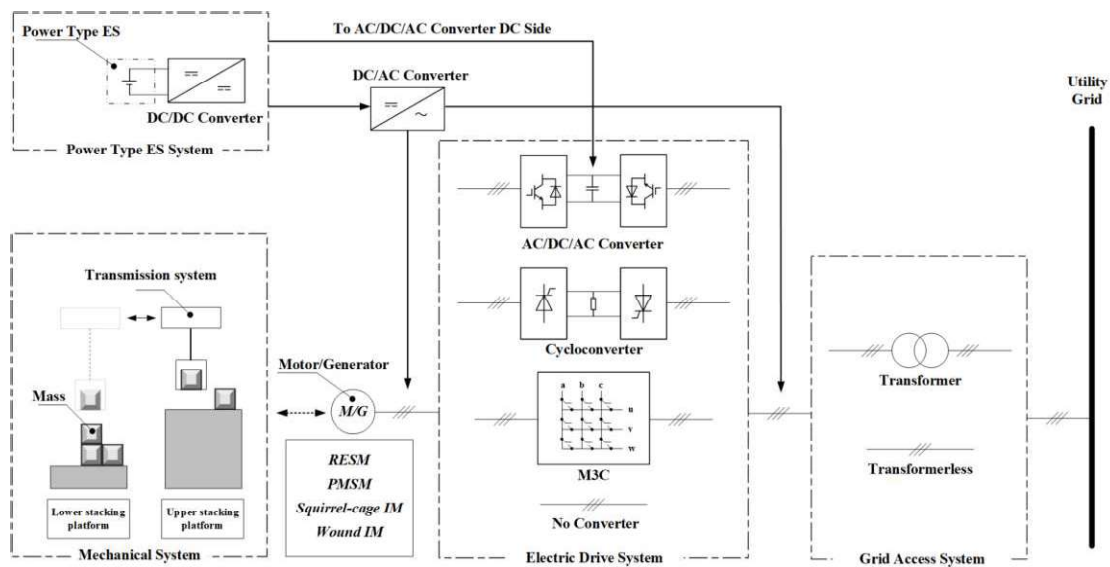


Fig. 4. Different structural solutions for HGES systems

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117 AC motors can be divided into synchronous motors, which include rotor excited synchronous  
 118 motors (RESM) and permanent magnet synchronous motors (PMSG), and asynchronous motors  
 119 (induction motors, IM), which include squirrel-cage asynchronous motors (Squirrel-cage IM) and wound  
 120 asynchronous motors (Wound IM). From a practical aspect, asynchronous motors are by far the most  
 121 mature and widely used motors. Pumped storage, for example, is the most similar energy storage  
 122 technology to gravity storage, and asynchronous motors are used in 84.3% of large pumped storage  
 123 projects[32]. From the economic point of view, the asynchronous motor is cheaper than the synchronous  
 124 motor, which matches the advantage of the low cost of GES. Therefore, asynchronous motors are  
 125 attractive for the gravity storage motor segment.

126 In the electrical drive system part, four possible options include no inverter, Cycloconverter (direct  
 127 AC/AC converter), matrix converter (M3C), and AC-DC-AC converter (indirect AC/AC converter).  
 128 Although the Cycloconverter was initially used extensively in variable-speed pumped storage power  
 129 plants in Japan, it has been phased out due to the advantages of the AD-DC-AD inverter and is only used  
 130 in a small number of large-scale applications[32-34]. M3C is more suitable for offshore wind power  
 131 stations and other occupation-sensitive large-scale application scenarios (more than tens of MW), but the  
 132 current control technology is not yet mature[35-37]. Therefore, the electrical drive section can consider  
 133 using an AC-DC-AC inverter for motor control or no inverter to simplify the equipment.

134 For grid access systems, the possible options are direct access to the grid and access to the grid via  
 135 transformers, which can be discussed for two typical application scenarios: distribution and transmission  
 136 grids. Direct connection to the grid can be considered for lower voltage distribution grids, thus avoiding  
 137 the additional investment and losses caused by transformers. When a higher voltage transmission grid is  
 138 required, a transformer should be considered to provide the required supply voltage for the motor.  
 139 Regarding the electrical drive system, if the electrical drive system uses inverters, it is possible to connect  
 140 the grid access system to a lower voltage grid without using transformers. Therefore, the grid access  
 141 system should consider the voltage level that needs to be connected and the structural configuration of  
 142 the electrical drive system.

143 There are three types of approaches for accessing the power-based storage system: accessing it as  
 144 the front stage of the electrical drive system, accessing it as the backstage of the electrical drive system,

145 and accessing into the electrical drive system (only if the electrical drive system is feasible with an AD-  
146 DC-AD inverter). The first two access strategies require a DC/DC converter for primary power storage  
147 control and an additional inverter as the electrical interface, which adds additional investment without  
148 significant performance improvement compared to the third access strategy. In contrast, direct access to  
149 the electrical drive system improves system reliability and reduces costs, making it a worthy option for  
150 power storage access strategies. On the other hand, adopting the direct access strategy also increases the  
151 attractiveness of the AD-DC-AD inverter in the electrical drive system.

152 In summary, in the distribution grid scenario, where the voltage level is low and the system capacity  
153 is relatively small given the same current limit, it is oriented to the small-scale application scenario of  
154 energy storage. Relevant studies have shown that GES is not economical in small-scale scenarios[38, 39].  
155 Therefore, priority should be given to reducing the system cost. Considering the voltage level in the  
156 distribution grid is lower and investment, the direct access strategy should be considered for both the  
157 electrical drive system and the grid access system; in addition, to ensure system reliability, the motor  
158 should be a wound asynchronous motor. Hence, the power storage can only be connected to the grid  
159 using an inverter, and the usage of this part should be combined with the actual demand for technical and  
160 economic evaluation.

161 In the transmission grid scenario, the higher voltage levels and the larger system capacity provide  
162 greater room for large-scale energy storage technology. Considering the additional losses caused by  
163 transformers (which will be more obvious in large-scale scenarios) and investments, AD-DC-AD inverter  
164 could be employed in transmission grids when voltage levels are relatively low (below 3kV, considering  
165 the current voltage-withstand level of power electronics). Neutral point clamped (NPC) or fly-across  
166 capacitor (FC) topologies in higher voltage-level scenarios. Furthermore, for high-voltage, the modular  
167 multilevel topology (MMC) or cascaded full-bridge topology (CHB) can be considered for the  
168 transmission grid. In addition, the motor module can use simpler and cheaper squirrel cage asynchronous  
169 motors due to an inverter based on fully controlled device. Therefore, for transmission grid scenarios, it  
170 is possible to consider configurations that use inverters in the electrical drive system, which avoid using  
171 transformers and use squirrel-cage asynchronous motors to reduce costs.

### 172 3 Energy flow characteristics of HGES

173 Generally speaking, the operating state of the energy storage system can be divided into two primary  
174 states: charging and discharging. In particular, for HGES, the two primary states of charging and  
175 discharging include three sub-states of starting, stable operating, and braking, so there are six basic states  
176 of HGES.

177 From the perspective of system structural composition, HGES can be divided into mechanical  
178 systems (including mass modules), motors, electrical drive systems, grid access systems, and power-  
179 based energy storage systems. The power flow relationship of each part is shown in Fig. 5.

180 The power flow of each system in the charging state in Fig. 5 is represented by green arrows; blue  
181 arrows represent the power flow in the discharging state; red arrows represent the loss of power flow;  
182 the final energy conversion state is represented by yellow; the intermediate energy conversion state is  
183 represented by gray, and the lost energy is symbolized by red.



208 (2) to Eq. (4):

$$209 P_{Cu} = 3I_s^2 R_s + 3I_r^2 R_r \quad (2)$$

$$210 P_{Fe} = 3I_m^2 R_m \quad (3)$$

$$211 P_M = T_L \omega \quad (4)$$

212 Where  $R_s$  is the motor stator resistance;  $I_r$  is the rotor current which is converted to the motor  
 213 stator side;  $R_s$  is the rotor resistance which is converted to the motor stator side;  $I_m$  is the motor  
 214 excitation current;  $R_m$  is motor reluctance;  $T_L$  is the motor mechanical torque;  $\omega$  is the motor  
 215 mechanical angular velocity.

216 The mechanical power  $P_M$  produced by the motor through the transmission system yields a  
 217 mechanical loss  $p_{ML}$  and finally becomes the power  $P_m$  obtained by the mass module.  $p_{ML}$  exists  
 218 because the actual speed of the mass block is low, while the motor speed is high, requiring transmission  
 219 equipment (such as gearboxes, traction equipment, etc.) for speed matching, and the gearbox ratio  $K$  is  
 220 calculated by Eq. (5):

$$221 K = \frac{D\omega}{2v_N} \quad (5)$$

222 Where  $D$  is the diameter of the motor;  $v_N$  is the rated speed of the mass block.

223 Based on the conservation of power on both sides of the transmission system, we can obtain the  
 224 tractive force  $F$  by increasing the mechanical torque  $T_L$  from the motor after the transmission system:

$$225 F = \frac{2K}{D} T_L - \frac{p_{ML}}{v_N} \quad (6)$$

226 Based on the force analysis of the mass module, the following equation can be obtained from  
 227 Newton's second theorem:

$$228 F = m(a + g) \quad (7)$$

229 Based on Eq. (7), the instantaneous acceleration  $a$  of the mass block can be calculated as:

$$230 a = \frac{D}{2K} \frac{d\omega}{dt} \quad (8)$$

231 The motor's rotor kinematic equation is:

$$232 \frac{d\omega}{dt} = \frac{\pm T_e \mp T_L - T_0}{J} \quad (9)$$

233 Where  $T_e$  is the electromagnetic torque of the motor, and the positive sign is taken in the electric  
 234 state;  $T_0$  is the stray resistance torque of the motor, and the negative sign is taken in the electric state.

235 Combining Eq. (6) with Eq. (9), we can get the mechanical loss  $p_{ML}$ :

$$236 p_{ML} = \frac{2Kv_N}{D} T_L - mv_N \left( \frac{D}{2K} \frac{\pm T_e \mp T_L - T_0}{J} + g \right) \quad (10)$$

237 Therefore, energy flow analysis in the charging state of the GES system, excluding the mass module,  
 238 is completed. The analysis of this part in the discharging state is similar.

239 The power conversion inside the mass module is related to the system's operating state. The  
 240 following six operating states are discussed in terms of charge start, charge operation, charge brake,  
 241 discharge start, discharge operation, and discharge brake.

242 In the charged state, when the mass block rises at a steady speed, all of the mass block power  $P_m$   
 243 is converted to the mass block gravitational potential energy power  $P_p$ . The gravitational potential  
 244 energy power  $P_p$  can be expressed by Eq. (11):

$$245 P_p = mgv \quad (11)$$

246 Where  $m$  is the mass of the mass block;  $g$  is the acceleration of gravity, which is a constant of

247  $9.81 \text{ m/s}^2$ ;  $v$  is the instantaneous velocity of the mass module.

248 When in the starting state, the block starts to move from a standstill, so there is a kinetic energy  
249 power  $P_k$ , and the power of the mass module  $P_m$  will be converted into two parts: gravitational potential  
250 energy power  $P_p$  and kinetic energy power  $P_k$ . The kinetic power  $P_k$  and the power of the mass  
251 module  $P_m$  are expressed by equations (12) and (13):

$$252 \quad P_k = mav \quad (12)$$

$$253 \quad P_m = mv(a + g) \quad (13)$$

254 Where  $a$  is the instantaneous acceleration of the mass block.

255 When in the braking state, the block gradually changes from running to stationary, so the same  
256 kinetic power  $P_k$  exists. In contrast to the starting state, the kinetic power  $P_k$  is negative at this time,  
257 which is reflected in the energy perspective as a gradual reduction of the kinetic energy of the mass block.  
258 However, the flow direction of the kinetic power  $P_k$  in the braking state is related to the system structure  
259 and its control strategy. The possible flows include conversion to gravitational potential power  $P_p$   
260 (uncontrolled kinetic strategy), conversion to mass block power  $P_m$  for feeding back to the grid (motor  
261 feedback braking strategy) or conversion to mass-side loss power  $P_{ml}$  (electrical consumption braking  
262 or mechanical braking).

263 In the discharged state, when the mass block maintains a steady rate of descent while dragging the  
264 motor to generate electricity, all of the mass block's gravitational potential energy power  $P_p$  is converted  
265 to mass power  $P_m$  and generates motor-side mechanical power  $P_M$ . When in the starting state, similar  
266 to the charge starting state, mass power  $P_m$  is converted to kinetic energy power  $P_k$  with gravitational  
267 potential energy power  $P_p$ . When in the braking state,  $P_k$  may be converted to mass block power  $P_m$   
268 for return to the grid (motor feedback braking strategy) or converted to mass-side loss power  $P_{ml}$   
269 (electrical consumption brake or mechanical brake)

## 270 4 Power electronics control strategies

271 The control of power electronics is at the bottom, and the foundation of the control of HGES, so the  
272 control of HGES relies heavily on the control of power electronics. This section focuses on two systems  
273 involving power electronics: electrical drive and power-based energy storage systems. Based on the  
274 discussion in Section 2.3, this section will discuss the control strategy of power electronics in AC-DC-  
275 AC inverter (electrical drive system) and DC/DC converter (power-based energy storage system) based  
276 on the perspective of HGES control.

### 277 4.1. Motor-side inverter

278 The motor-side inverter refers to the inverter near the motor side of the AC-DC-AC inverter in the  
279 electrical drive system. The control object of the motor-side inverter is the motor, and its control can be  
280 divided into scalar control (SC) and vector control (VC). Vector control is the industry's most widely  
281 used control technology for high-power drive systems because of its better dynamic response, energy  
282 consumption characteristics, and control accuracy.

283 According to flux orientation, vector control can be divided into flux orientation control (FOC)  
284 based on rotor flux orientation and direct torque control (DTC) based on stator flux orientation.

285 The basic control model of FOC is shown in Fig. 6. The equivalent DC motor model is obtained by  
286 coordinate transformation, and then the torque is controlled by the flux chain component according to  
287 the control method of the DC motor. Finally, the resulting control quantities are converted to the



306 With the development of digital processors, the above two vector control techniques can be  
 307 implemented in engineering at a low cost, thus becoming the most widely used high-performance motor  
 308 control techniques. The comparison between FOC and DTC is shown in Table 1, both are based on the  
 309 dynamic model of the motor, and the torque and flux components of the three-phase stator current are  
 310 separated through coordinate transformation to achieve decoupled control, which enables the induction  
 311 motor to achieve dynamic performance comparable to the DC motor.

312 Stable and reliable control of the mass module during operation is the most basic requirement of the  
 313 gravity storage system, so it is desired to provide stable torque control over a wide range of speed  
 314 variations. From the speed regulation and torque control perspective, FOC is more suitable for gravity  
 315 storage requirements. On the other hand, DTC control requires fewer motor parameters and does not  
 316 require complex rotational coordinate transformation. Therefore, it still has better control robustness  
 317 when the motor parameters change, which improves the reliability of the electrical drive system in  
 318 unconventional conditions.

319 In summary, FOC is more suitable for achieving high-performance control under stable conditions,  
 320 while DTC may perform better in the face of fault conditions. We can consider switching different control  
 321 strategies in different situations to achieve the best-integrated control effect when hardware conditions  
 322 allow.

323 **Table.1 Comparison of the control characteristics of FOC and DTC [40, 41]**

	DTC	FOC
Flux control	Stator flux control	Rotor flux control
Torque control	Multi-position control, larger pulsation	Continuous control, less pulsation
Current control	Uncontrollable	Closed-loop control
Coordinate transformation	Static coordinate transformation	Rotating coordinate transformation
Speed range	Narrower	Wider
Required parameters	$R_s$	$R_s, R_r, L_s, L_r, L_m$
Control robustness	Good	Normal
PWM strategy	Hysteresis or SVPWM	Hysteresis or SVPWM

#### 324 4.2. Grid-side inverter

325 Grid-connected control is an essential requirement for energy storage systems, and the performance  
 326 of its grid connection directly affects the overall performance of the energy storage system. The main  
 327 body of grid-connected control is the grid-side inverter, i.e., the AC-DC-AC inverter near the grid side  
 328 in the electrical drive system. Generally speaking, the main content of grid-connected control is the  
 329 control of active and reactive currents, i.e., active power (or node phase angle) and reactive power (or  
 330 node voltage).

331 The instantaneous power in the stationary three-phase coordinate system is defined as:

$$332 P = |V_{abc}| |I_{abc}| \cos\varphi \quad (16)$$

$$333 Q = |V_{abc}| |I_{abc}| \sin\varphi \quad (17)$$

334 By transforming the above two equations by  $T_{3s/2s}$  and  $T_{2s/2r}$ , we can obtain the instantaneous  
 335 power expression based on the grid voltage orientation after rotating the coordinate system:

$$336 P = V_d I_d + V_q I_q \quad (18)$$

$$337 Q = V_q I_d - V_d I_q \quad (19)$$

338 When the grid voltage is stable, i.e.,  $V_d$  is constant, active and reactive power can be controlled by

339 controlling the dq-axis component of the inverter output current. The DC-side voltage of the AC-DC-AC  
 340 inverter is related to the power flow at both ends of the dc-side. Assuming that the dc power input at the  
 341 rectifier side is constant, the dc-side voltage will be controlled by the active power output at the inverter  
 342 side, so the dq-axis component of the inverter current will be controlled can also achieve the control of  
 343 the dc-side voltage, as shown in Fig. 8.

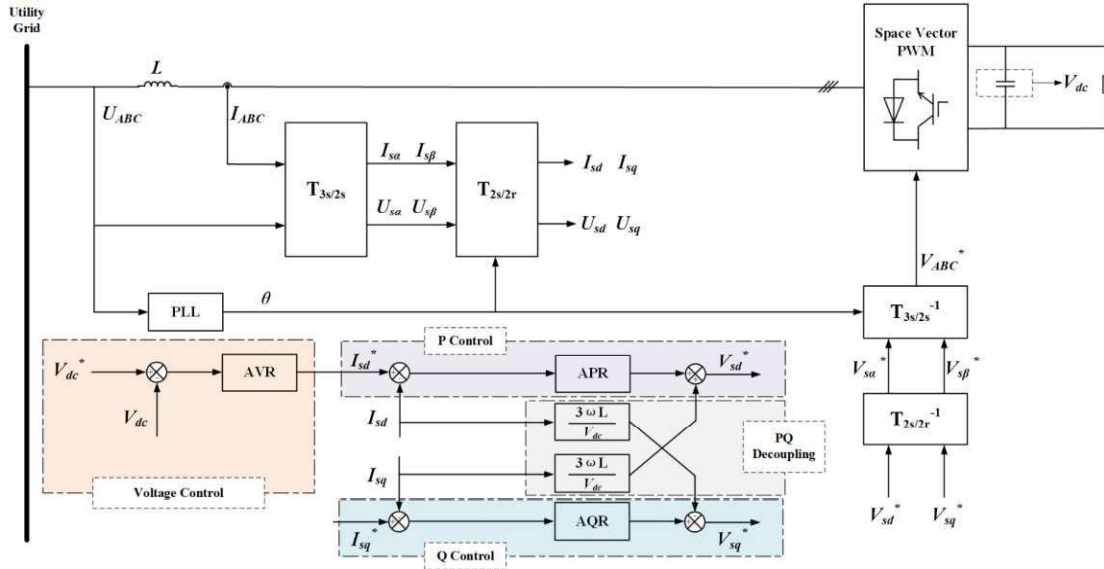


Fig. 8. Control System of Grid-connected Inverter

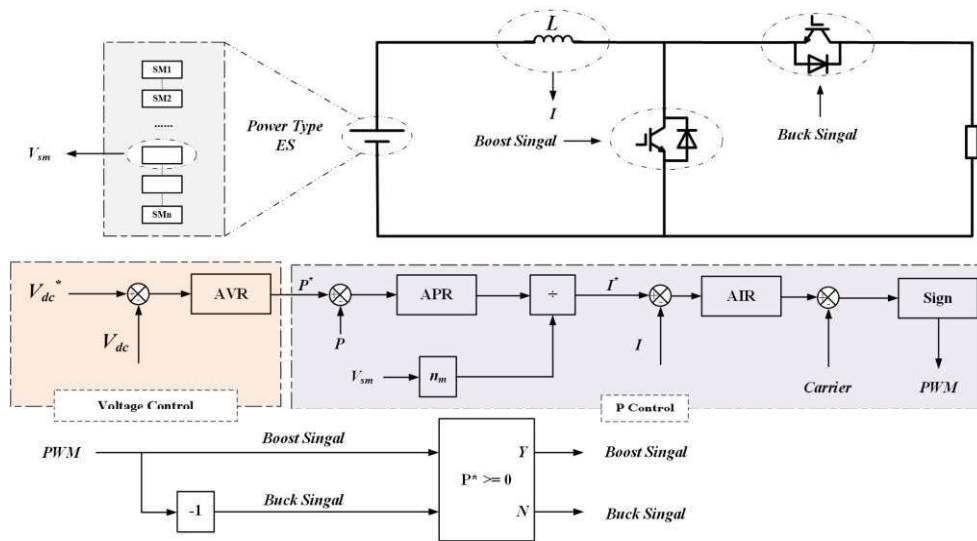
346 The control system samples the three-phase voltage and current on the grid side and obtains the  
 347 phase angle of the voltage through a phase-locked loop (PLL), then uses a coordinate transformation to  
 348 get the voltage and current vectors in a two-phase rotating coordinate system. The decoupling control  
 349 loop consists of voltage, active power loop, and reactive power loop, which can be switched to active  
 350 power control by removing the voltage control part when voltage control is not used. Since the current  
 351 component of the dq axis is coupled, which makes the decoupling control of PQ complicated, thus  
 352 feedforward control is introduced for decoupling. The output of the decoupled control loop through the  
 353 inverse coordinate transformation gets the three-phase voltage reference vector, which SVPWM  
 354 modulates to generate the three-phase switching signal to control the grid-connected inverter.

#### 4.3. DC/DC converter

356 The function of the DC/DC converter is to convert DC power from one voltage level to another  
 357 voltage level, playing a role similar to the DC transformer. For a hybrid GES system, even at the lowest  
 358 380 V distribution voltage level, if an AC-DC-AC converter is used as the electrical drive system, the  
 359 bus voltage on its DC side will be above 560 V. On the other hand, the supercapacitor, as a typical and  
 360 mature power-based energy storage device, the rated voltage of a single unit is only 2.7 V[42-44]. If  
 361 DC/DC converter is not used for voltage matching, a large number of devices will be connected in series,  
 362 which is undesirable in terms of economy and technology.

363 The control system of the DC/DC converter is shown in Fig. 9. The DC/DC converter suitable for  
 364 the energy storage system requires control of the energy flow in both directions, so a Boost/Buck  
 365 bidirectional converter is used. In order to provide sufficient voltage, the power-based energy storage  
 366 side still needs some devices connected in series. The control part is similar to the control of the grid-  
 367 side inverter, including voltage control and power control, and again, the voltage control part is not added

368 when power control is used.



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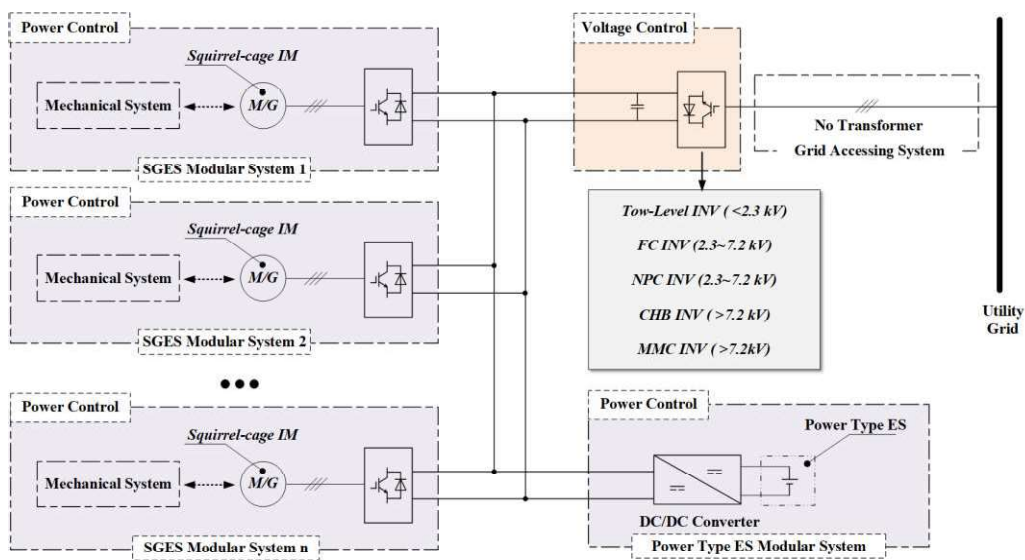
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Fig. 9. DC/DC converter control system

371 4.4. Discussion on control coordination

372 Based on the discussion in Section 2.3, in the distribution grid application scenario, a wound  
 373 asynchronous motor can be directly connected to the grid, where the gravity storage part does not involve  
 374 power electronics, and there is no control problem at the power electronics level. Power-based energy  
 375 storage devices are connected to the grid through DC/DC converters and inverters, which can be  
 376 designated for power control and DC bus voltage control, respectively.

377 In the transmission grid scenario, the AC-DC-AC inverter-based configuration has many advantages,  
 378 including significantly reducing the number of grid-side inverters through a shared DC bus strategy, as  
 379 shown in Fig. 10.



380

381

Fig. 10. Schematic diagram of HGES at the transmission grid level

382 When a common DC busbar strategy is used, additional devices for gravity and power-based energy  
 383 storage can be connected to the system with a minimum number of power electronics, improving the cost  
 384 and reliability of the system significantly. The DC-side bus will be expanded into a micro DC network,

385 facilitating the connection of other possible DC devices (such as PV arrays). On the other hand, with  
 386 DC-side structures becoming complex, connected power electronics will face control coordination  
 387 problems.

388 The primary node types of AC-based power systems include PQ, PV, and V $\theta$  nodes. The PQ node  
 389 is a node where the amounts of active and reactive power exchanges are determined. The PV node has  
 390 some reactive power compensation capability to ensure its node voltage is stable. The V $\theta$  node is also  
 391 called a balancing node, which has a large capacity and can ensure the power balance of the whole grid,  
 392 and this node is both necessary and unique based on the consideration of control stability.

393 In analogy with the node characteristics of the AC grid and considering that there is no reactive  
 394 power in the DC grid, it is easy to find that the DC microgrid should include two types of nodes, P-node  
 395 and V node, corresponding to the power control and voltage control in the aforementioned power  
 396 electronic control strategy. From the control aspect, several P nodes can be under the DC grid to ensure  
 397 the stability of node exchange power through power control; V nodes should still exist and be unique for  
 398 ensuring the voltage stability of the whole DC grid. Considering the V node based on the power  
 399 perspective, the sufficient and necessary condition to maintain the DC voltage stability should be that the  
 400 node can complete the power balance of the whole network, so the V node must have sufficient capacity.

401 Considering that the grid-side inverter can exchange power between the entire DC microgrid and  
 402 the AC main grid, it is inevitable that it will have the largest equipment capacity in the whole DC  
 403 microgrid. So we can set the grid-side inverter as the V node, as shown in Fig. 10. Another advantage of  
 404 this control strategy is that since a larger capacity of the grid-side inverter is required, a modular  
 405 multilevel topology is more likely to be used to facilitate access to higher voltage transmission grids,  
 406 which will avoid the potential use of transformers (thus reducing investment and losses).

## 407 5 Compensation and configuration strategy of Power-based ES

408 For a GES system with a certain capacity, the HGES needs to be configured with the corresponding  
 409 capacity of power-based energy storage, which will affect the overall economy of the system. If the  
 410 configured capacity is too large, it will affect the economic performance of the hybrid system. While the  
 411 configured capacity is too small, the technical performance will deteriorate, so it is necessary to  
 412 determine the appropriate capacity configuration scheme for power-based energy storage. The capacity  
 413 configuration scheme of power-based energy storage is related to the compensation strategy for a given  
 414 demand, so various capacity configuration schemes in this chapter will be presented based on different  
 415 compensation strategies.

416 According to Eq. (9), when driving a constant torque load, the way to change the motor speed (i.e.,  
 417 the mass module movement state) is to change the electromagnetic torque of the motor. Simplifying the  
 418 actual GES as a first-order inertia loop, the response of its tractive force (torque) step command is an  
 419 exponential function, and let the horizontal segment  $F_h$ , rising segment  $F_{up}$  and falling segment  $F_{down}$   
 420 of its tractive force response curve be:

$$421 F_h = B_2 mg \quad (20)$$

$$422 F_{up} = B_m mg + (B_n - B_m) mg (1 - e^{-At}) \quad (21)$$

$$423 F_{down} = B_n mg + (B_m - B_n) mg e^{-At} \quad (22)$$

424 where time  $t \geq 0$ ,  $B_m$  is the initial coefficient of traction force,  $B_n$  is the final coefficient of  
 425 traction force, and  $A$  is related to the motor, transmission system, and mass block used, reflecting the  
 426 inertia of the entire gravity energy storage system. To simplify the analysis, we combine the above three

427 traction forces and considering the gravity of the mass module, the combined external force on the mass  
 428 module can be expressed uniformly as:

$$429 \quad F = (B_n - 1)mg + (B_m - B_n)mge^{-At} \quad (23)$$

430 To simplify the analysis, we assume that three steady-state traction forces exist in this example:  
 431  $B_1mg > B_2mg = mg > B_3mg$ . Therefore, the velocity response curve can be calculated by the  
 432 following equation:

$$433 \quad v = v_0 + \int_{t_0}^{t_0+\Delta t} \frac{\Delta F}{m} dt \quad (24)$$

434 Where,  $t_0$  is the initial moment of traction force change,  $\Delta t$  is the traction force change elapsed  
 435 time, taking  $t_0 = 0$ , the velocity and acceleration response curve can be obtained according to Eq. (23),  
 436 which is generated by the combined external force F:

$$437 \quad v = v_0 + (B_n - 1)g\Delta t + (B_m - B_n)\frac{g}{A}(1 - e^{-A\Delta t}) \quad (25)$$

$$438 \quad a = (B_n - 1)g + (B_m - B_n)ge^{-A\Delta t} \quad (26)$$

439 In particular, when the traction coefficient satisfies Eq. (27), Eq. (25) and Eq. (26) can be further  
 440 simplified to Eq. (28) and Eq. (29):

$$441 \quad \forall |B_m - B_n| = C \quad (27)$$

$$442 \quad v = v_0 + \frac{Cg}{A}(K_1A\Delta t + K_2(1 - e^{-A\Delta t})) \quad (28)$$

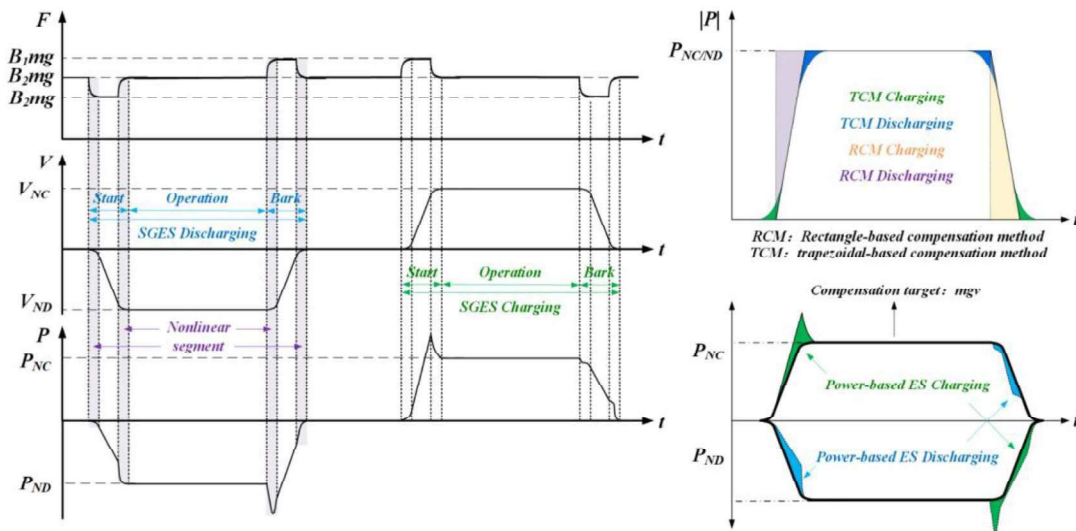
$$443 \quad a = Cg(K_1 + K_2e^{-A\Delta t}) \quad (29)$$

444 Where  $C$  is a constant,  $K_1 \in \{1,0,-1\}$ ,  $K_2 \in \{1,0,-1\}$  and  $K_1K_2 \neq 1$ .

445 So far, the tractive force and velocity curves of the mass block downward and upward can be plotted  
 446 schematically, and the exchange power schematic can be plotted according to Eq. (30):

$$447 \quad P = Fv \quad (30)$$

448 The tractive force curve, mass module velocity curve, and exchange power curve are shown on the  
 449 left side of Fig. 11. Due to the inherent inertial loop of the electromechanical system leads to the existence  
 450 of nonlinear segments of the curve, among them, the nonlinear situation of the power curve is the most  
 451 serious. The most unfavorable power nonlinear segment to the system's normal operation is the power  
 452 spike generated during the start-up phase of gravity storage charging and the discharge braking phase,  
 453 which will produce overcurrent and voltage instability at the machine if not suppressed.



454

455

Fig. 11. Power-based energy storage compensation method diagram

456 Explained from the analytical perspective, based on Eq. (30), it is clear that the nonlinearity is most  
 457 pronounced since the exchange power curve is the product of the tractive force curve and the velocity  
 458 curve.

459 From the energy perspective, based on the discussion in Section 2.4, the kinetic energy stored during  
 460 the operation of the mass module is released during the charging starting and discharging braking phases.  
 461 Due to the motor feedback braking strategy (including DTC and FOC), the kinetic energy is fed back to  
 462 the grid through the DB1 and CB2 paths in Fig. 5, and this energy is stacked on the gravitational potential  
 463 energy power resulting in a power spike. For the same reason, the exchange power inversion between  
 464 the charging braking and discharging starting phases can be explained.

465 Further, based on the power conversion triangle of the mass module in Fig. 5, with Eq. (11)-Eq. (13),  
 466 we can know that the exchange power is the superposition of gravitational potential energy power and  
 467 kinetic energy conversion power.

468 In a single run (rising or falling), gravitational potential energy power has a sign-preserving, more  
 469 moderate change, while kinetic energy power undergoes a positive and negative change that conforms to  
 470 the relatively drastic change.

471 Therefore, if we can remove the kinetic energy power, a more drastic change in the component, we  
 472 can obtain a more stable exchange power curve. Based on this idea, the compensation method obtained  
 473 is called the compensation method based on the gravitational potential energy power, as shown in Fig.  
 474 11 right below.

475 The capacity  $E_1$  of the power-based energy storage module to be configured for the gravitational  
 476 potential power-based compensation method can be obtained from Eq. (31):

$$477 \quad E_1 = \frac{1}{2} m v_m^2 \eta_M \quad (31)$$

478 Where  $v_m$  is the maximum speed of the mass module operation,  $\eta_M$  is the motor efficiency.

479 The compensation method based on gravitational potential power suppresses the power spikes and  
 480 sags brought by kinetic power and reduces the capacity of power transmission equipment. It also  
 481 facilitates the design of filters because the original irregular exchange power curve becomes regular and  
 482 symmetrical.

483 Considering that there are still nonlinear segments in the gravitational potential-based compensation  
 484 method, a linearized compensation method is further proposed on this basis, including the trapezoidal-  
 485 based compensation method (TCM) and the rectangle-based compensation method (RCM), as shown in  
 486 the upper right of Fig. 11.

487 The linearization-based compensation method makes the overall power external characteristics of  
 488 the HGES more regular and facilitates the dispatch at the microgrid scale. In particular, the rectangular-  
 489 based compensation method, based on the trapezoid-based compensation method, improves the full  
 490 power response time of the HGES from the original motor response time level to the power-based energy  
 491 storage device response time level, which significantly improves the response speed of the HGES.  
 492 Because the exchange power response curve of the rectangular-based compensation method is very close  
 493 to the rectangle when viewed on the original time scale. The method is thus entitled.

494 Based on Eqs. (12), (13), (28), and (29), the required configuration capacity  $E_2$  of the power-based  
 495 energy storage module based on the trapezoidal-based compensation method can be expressed as:

$$496 \quad E_2 = E_1 - (E_{start\ up} - \frac{v_{strat\ up}^2 |_{t=\Delta t}}{2a_{up}}) \eta_M \quad (32)$$

497 
$$v_{start\ up} = (B_1 - 1)g \left( t + \frac{e^{-At} - 1}{A} \right) \quad (33)$$

498 
$$E_{start\ up} = mg \int_0^{\Delta t} v_{start\ up} dt \quad (34)$$

499 
$$a_{up} = (B_1 - 1)g(1 - e^{-At}) \quad (35)$$

500 where  $v_{start\ up}$  is the speed of the mass module in the start-up phase;  $E_{start\ up}$  is the energy  
 501 absorbed by the mass module in the start-up phase; and  $a_{up}$  is the acceleration of the mass module in  
 502 the upward uniform acceleration phase.

503 The required configuration capacity  $E_3$  of the power-based energy storage module based on the  
 504 rectangular compensation method can be expressed as the difference between the triangular area in Fig.  
 505 11 and the area of the original irregular region:

506 
$$E_3 = \frac{v_m^2}{2a_{up}} \eta_M - E_1 \quad (36)$$

507 In summary, this chapter investigates the tractive force, velocity, and power of GES's mass modules.  
 508 The power compensation and capacity configuration strategies of three power-based energy storage are  
 509 given based on the external characteristics of its exchange power.

510 The compensation method based on gravitational potential power decouples the exchange power of  
 511 the mass module, separates the gravitational energy storage power from the kinetic energy power based  
 512 on the power triangle in Fig. 5, and eliminates the kinetic energy power component that fluctuates  
 513 significantly to improve the stability and symmetry of the power waveform.

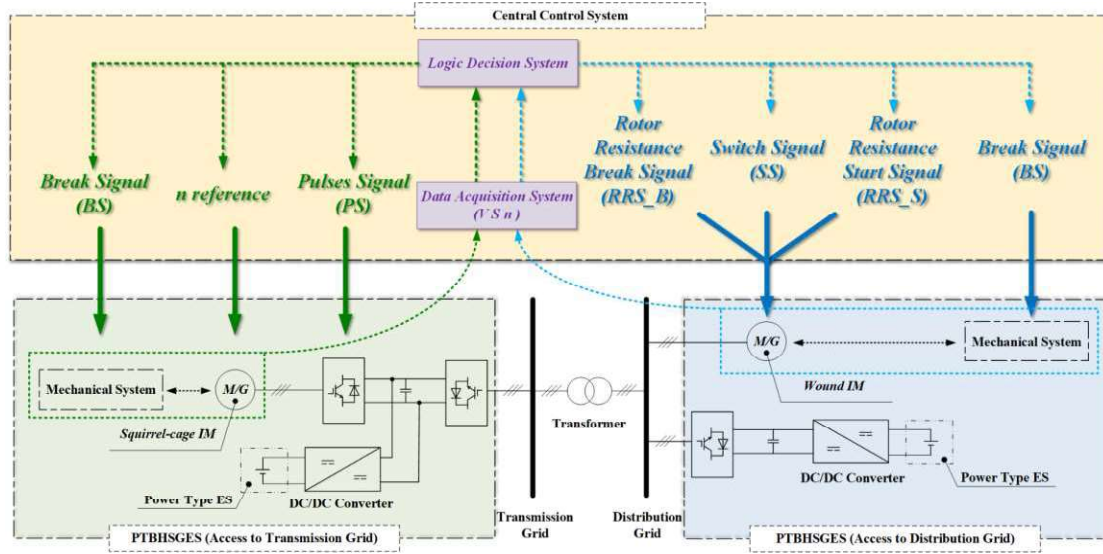
514 The trapezoid-based compensation method achieves the complete linearization of the external  
 515 characteristics of the power. On this basis, the rectangular-based compensation method is further induced  
 516 to improve the full power response time from the GES system to the power-based energy storage response  
 517 time so that the HGES has both the energy storage capacity of the energy-based energy storage and the  
 518 response speed of the power-based energy storage.

## 519 6 Coordinated control strategies at the hybrid energy storage system 520 level

521 For two typical application scenarios in transmission and distribution grid, two types of HGES and  
 522 their control signals are shown in Fig. 12. The distribution grid level HGES is shown in the blue part of  
 523 Fig. 12, and the transmission grid level hybrid gravity storage system is shown in the green part of Fig.  
 524 12.

525 The two types of HGES are similar in terms of the control process. First, the system state is sampled,  
 526 including at least three critical parameters: mass module operating speed  $V$ , mass module operating  
 527 position  $S$ , and motor speed  $n$ . The resulting signals are sent to the logic decision system for system  
 528 operating state identification to give the corresponding control signals.

529 The control strategies for the two types of HGES differ due to the system structure; thus, the final  
 530 output control signals are also varied. The control strategies are introduced according to the six basic  
 531 operating states of GES.



532

533

Fig. 12. Hybrid system-level control flow chart of HGES

534 6.1. Distribution grid-level HGES control strategy

535 The HGES applied to the distribution grid is shown in the blue part of Fig. 12. Based on the  
 536 discussion in Section 2.3, the motor is a wound asynchronous motor, and both the electrical drive system  
 537 and the grid access system use a direct access strategy. Power-based energy storage is controlled by a  
 538 DC/DC converter for power control, then connected to the distribution grid after the DC-side voltage  
 539 control by the inverter.

540 A significant starting torque is required when the system is in a charging starting state because the  
 541 motor needs to start with a mass module. In order to avoid stalling and to suppress the starting current, a  
 542 strategy of adding a starting resistor in series with the rotor (which is one of the reasons for not using a  
 543 squirrel-cage motor) is used, and the starting resistor is removed after sufficient speed is reached to bring  
 544 the motor into normal operation. We can obtain the value of the starting resistance is obtained through  
 545 the motor electromagnetic torque equation, and the motor electromagnetic torque after the rotor series  
 546 resistance can be expressed as:

547 
$$T = \frac{3pU_s^2 \frac{R_r + \Delta R_r}{S}}{2\pi f_s \left[ \left( R_s + \frac{R_r + \Delta R_r}{S} \right)^2 + (X_s + X_r)^2 \right]} \quad (37)$$

548 Where  $T$  is the electromagnetic torque;  $p$  is the number of motor pole pairs;  $U_s$  is the RMS value  
 549 of the stator-side phase voltage;  $R_r$  is the rotor resistance;  $\Delta R_r$  is the resistance in series with the rotor;  
 550  $f_s$  is the stator-side frequency;  $R_s$  is the stator-side resistance;  $X_s$  is the stator-side inductance;  $X_r$  is  
 551 the rotor-side inductance;  $S$  is the slip rate. To obtain the maximum starting torque, the required series  
 552 resistance  $\Delta R_r$  can be solved by bringing  $S = 1$  and  $T = T_m$  ( $T_m$  is the maximum electromagnetic  
 553 torque) into Eq. (37).

554 When the system is in charging operation, the power absorbed by the mass module will be steadily  
 555 converted to gravitational potential energy power, and the system components are in a steady state  
 556 without special control.

557 When the system is in a charging braking state, the motor rotor is strung into the braking resistor  
 558 for electrical braking to complete the deceleration (if a squirrel cage motor is used, it will face the  
 559 problem of braking difficulties). When the speed drops to zero (or low enough), the motor brakes and

560 the braking resistor is removed, and the system is removed from the grid and then leaves the grid. The  
 561 braking resistance is similar to the starting resistance and can be solved by bringing  $S = 1$  and  $T = T_L$   
 562 ( $T_L$  is the load torque) into Eq. (37) to find the required series resistance  $\Delta R_r$ .

563 When the system is in a discharged start condition, the same starting resistance is needed as for a  
 564 charged start, not because the starting torque is insufficient - it should be noted that the driving and drag  
 565 properties of the electromagnetic torque and the load torque have been exchanged - but to limit the  
 566 excessive start-up current. In particular, at this point, the mass module will be in a downward process,  
 567 and the motor will be counter-rotating. In order to keep the motor in a discharged state, it is necessary to  
 568 connect to a negative sequence three-phase power supply - by exchanging any two phases of the three-  
 569 phase grid-connected mechanical switch. After reaching enough speed to remove the starting resistance,  
 570 the system turns into normal operation.

571 When the system is in the discharging operation state, the gravitational potential power is steadily  
 572 released as the output power of the mass module, and all parts of the system are in a steady state without  
 573 special control.

574 When the system is in the discharging braking state, it is noted that the electromagnetic torque is  
 575 resistance in nature. If the rotor braking resistor is directly connected to the rotor, the electromagnetic  
 576 torque will be further reduced, leading to the out-of-control of the mass module (free fall), so the braking  
 577 resistor should be connected after the positive sequence three-phase power supply is reconnected. After  
 578 the mass module is stationary, the motor will be held, the braking resistor removed, and the system off-  
 579 grid. In particular, when the system encounters an unexpected fault and needs to stop in an emergency,  
 580 the control strategy of discharge braking can also be used.

581 In conclusion, the control strategy at the distribution grid level can be organized as Table 2 for the  
 582 logic decision system in Fig. 12. The SS indicates the network side mechanical switching signal, which  
 583 is 1 when connected to positive sequence three-phase power, 2 when connected to negative sequence  
 584 three-phase power, and -1 when off-grid; BS indicates the braking signal, which is -1 when not braking  
 585 (normal operation) and 1 when braking; the rotor series starting and braking resistor signals are RRS\_S  
 586 and RRS\_B respectively, which are 1 when connected and -1 when removed.

587 **Table.2 Control logic table for distribution grid-level HGES**

System Status	SS	BS	RRS_S	RRS_B
CS ( $ n  >  n_s $ )	1	-1	1→(-1)	-1
CO	1	-1	-1	-1
CB ( $V = 0$ )	-1	-1→(1)	-1	1→(-1)
DS ( $ n  >  n_s $ )	2	-1	1→(-1)	-1
DO	2	-1	-1	-1
DB ( $V = 0$ )	1→(-1)	-1→(1)	-1	1→(-1)

588 *6.2. Transmission grid-level HGES control strategy*

589 The HGES applied to the transmission grid is shown in the green part of Fig. 12. Based on the  
 590 discussion in Section 2.3, the motor is a squirrel-cage asynchronous motor and the electrical drive system  
 591 is an AC-DC-AC inverter, and the machine side inverter is controlled by the FOC because the FOC is a  
 592 direct control of the rotational speed, which is more convenient in the control system design. The  
 593 incoming system adopts the direct access strategy, and the power-base energy storage is controlled by  
 594 the DC/DC converter for power exchange and then connected to the DC side of the AC-DC-AC inverter.

595 When the system is in a charging starting state or charging operating state, the machine side inverter  
 596 is given a pulse signal, and the reference speed can be given directly at this time because the FOC control  
 597 strategy is used for squirrel cage motor control. The reference speed is given as the nominal speed to  
 598 ensure that the motor runs in optimal working condition.

599 When the system is in the discharge starting state or charging operating state, the machine side  
 600 inverter is given a pulse signal, and the reference speed is specified as the negative rated speed. Then the  
 601 motor reverses and operates in the discharging state.

602 When the system is in a charging braking state or discharging braking state, the reference speed  
 603 can be directly given to zero by FOC control, and the motor brakes when the actual speed drops to zero  
 604 and stops giving pulse signals. Since the inverter itself consists of switching devices, the system is  
 605 spontaneously off-grid when the inverter is turned off.

606 Overall, the control strategy at the distribution grid level can be organized as table 3 for the logic  
 607 decision system in Fig. 12. Where BS indicates the braking signal, -1 when there is no braking (normal  
 608 operation), and 1 when braking; PS indicates the machine side inverter pulse signal.

609 **Table.3 Control logic table for transmission grid-level HGES**

System Status	BS	PS	n reference
CS ( $ n  >  n_s $ )	-1	1	$n_N$
CO	-1	1	$n_N$
CB ( $V = 0$ )	-1→(1)	1→(-1)	0
DS ( $ n  >  n_s $ )	-1	1	$-n_N$
DO	-1	1	$-n_N$
DB ( $V = 0$ )	-1→(1)	1→(-1)	0

610 From the control point of view, the two different hybrid gravity storage systems which are applied  
 611 to the distribution and transmission grids, the hybrid gravity storage system at the transmission grid level  
 612 becomes complex to control at the equipment level but simpler at the system level due to the addition of  
 613 power electronics which makes the equipment more controllable.

## 614 7 Simulation verification

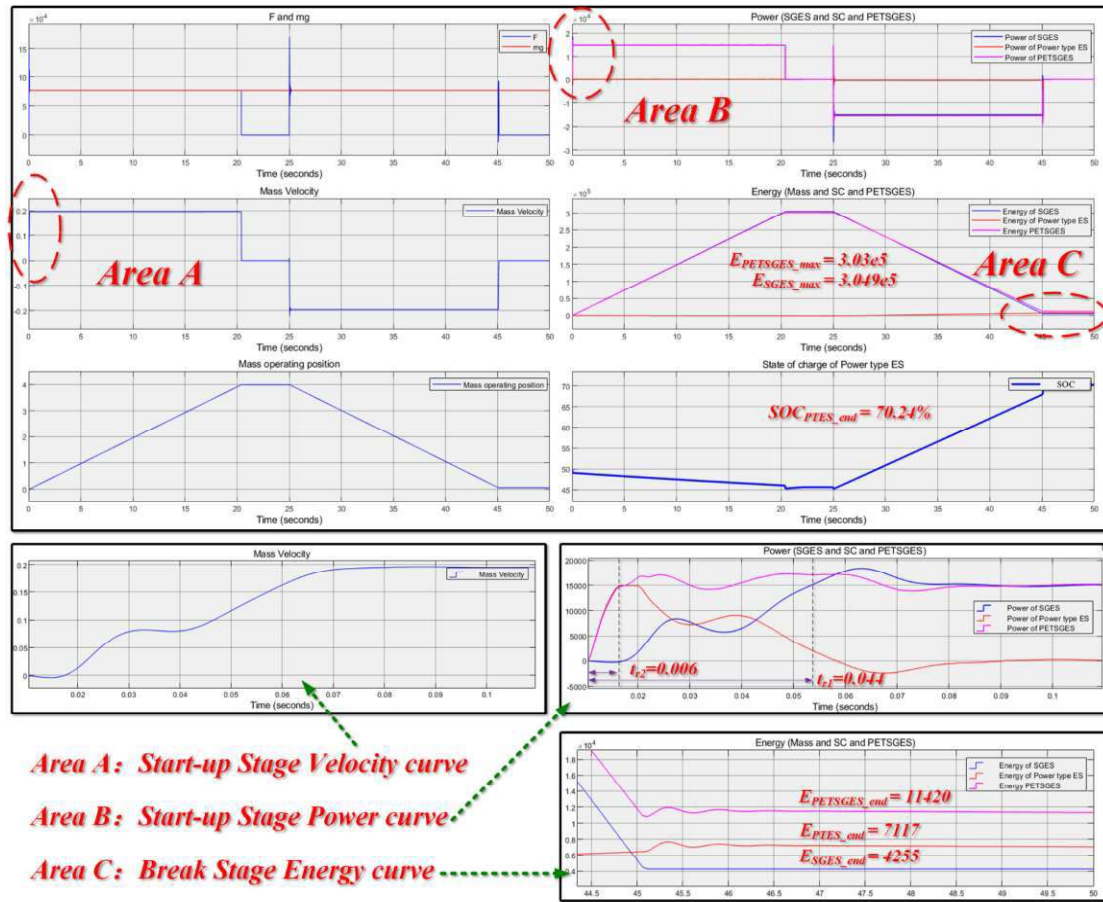
615 This chapter is based on MATLAB/Simulink to simulate and verify the proposed HGES, including  
 616 the feasibility of the system architecture of two HGES at the distribution grid level and transmission grid  
 617 level, the control strategy of power electronics, the control strategy of power-based energy storage and  
 618 the control strategy at the hybrid system level.

### 619 7.1. Distribution grid-level HGES

620 Based on the blue part in Fig. 12, a distribution grid-level HGES simulation model is established.  
 621 The model parameters are shown in Table 4, and the simulation results are shown in Fig. 13. In order to  
 622 present the entire process of HGES operation in a shorter time scale, the simulation time is set to 50  
 623 seconds (the operation time should be longer in reality), in which the first 25 seconds the system is  
 624 charged and the last 25 seconds the system is discharged. The rated speed of the mass module is 0.2  
 625 meters per second, and the total vertical height movement is set to 4 meters (which should be much more  
 626 prominent in reality). Due to the application for distribution grid level, a wound asynchronous motor  
 627 with a rated capacity of 15kW is used.

Table.4 Simulation parameter table for distribution grid-level HGES

Systems	Items	Parameters
Mechanical System	Mass	1.6 t
	Height of operation	4 m
	Rated operating velocity	0.2 m/s
Motor System	Rated capacity	15 kW
	Stator resistance	0.2147 $\Omega$
	Stator inductance	0.000991 H
	Rotor resistance	0.2205 $\Omega$
	Rotor inductance	0.000991 H
	Mutual inductance	0.06419 H
	Inertia	0.102 kg * m <sup>2</sup>
	Friction coefficient	0.009541 N * m * s
	Number of pole pairs	2
	Rated frequency	50 HZ
	Rated voltage	0.4 kV
	Starting resistance	3 $\Omega$
	Braking resistance	8.25 $\Omega$
Power-based ES (Supercapacitor)	System capacity	1 F
	Unit rated voltage	2.7 V
	Number of units	100
	System Rated Voltage	270 V
	Initial Voltage	191 V
Electric Drive system	DC/DC Inductor	0.01 H
	Voltage stabilizing capacitor	0.019 F
	Switching device on-resistance	0.001 $\Omega$
	Switching device blocking resistance	100000 $\Omega$
	PWM frequency	10 kHz



Area A: Start-up Stage Velocity curve  
Area B: Start-up Stage Power curve  
Area C: Break Stage Energy curve

629

630

Fig. 13. Simulation results of distribution grid-level HGES system states with typical operating conditions

631

The left column, from top to bottom, shows the mass module's traction force and gravity, the mass module's speed, the operating position of the mass module, and the speed curve of the start-up phase. The right column from top to bottom shows the exchanged power and stored energy of the mass module, power storage, and hybrid gravity storage system; the charge state of the power-based energy storage; the power curve of the start-up phase; and the energy gain/loss curve of the system after one operating cycle.

632

Due to using a 15 kW motor with small electromechanical inertia, reflected in the fast nonlinear transition process of the traction force curve in the figure, the velocity and position curve of the mass module can be considered linear on a time scale of seconds. Due to the access to the negative sequence three-phase power supply in the discharge state, large but quickly decaying tractive force fluctuations exist at the instant of discharging initiation ( $t=25$ ). Due to the slip rate, the motor cannot run precisely at the best operating point under the same load in both charging and discharging states. In order to ensure accurate output power, the power-based energy storage, in this case, also has a small compensating power in the stable operation stage.

633

The start-up stage power response curve (region B) shows that the full power response time of the hybrid gravity storage system is six milliseconds, while the original gravity storage system is 44 milliseconds. That is, the full power response speed of the hybrid energy storage system is seven times higher than the original gravity storage system under the current distribution grid simulation case.

634

Define the cycle efficiency of the energy storage system  $\eta_{sys}$  as follows:

635

$$\eta_{sys} = \eta_{in}\eta_{out} \quad (38)$$

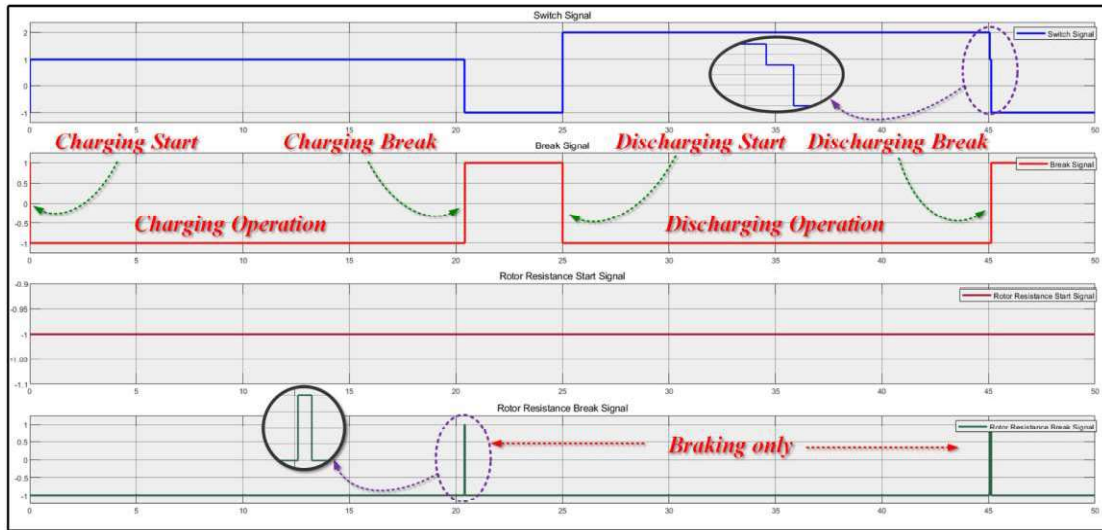
651 Where  $\eta_{in}$  is the energy storage system storage efficiency;  $\eta_{out}$  is the energy storage system  
 652 release efficiency. In particular, when the storage and release of the energy storage system have the same  
 653 process, the two process efficiencies can be considered equal, then the cycle efficiency  $\eta_{sys}$  of the  
 654 energy storage system can be written as:

$$655 \quad \eta_{sys} = \left( \frac{E_0 - E_{loss}}{E_0} \right)^2 \quad (39)$$

656 Where  $E_0$  is the original stored energy of the energy storage system;  $E_{loss}$  is the energy loss when  
 657 releasing energy to the outside. The power-based energy storage in this simulation case uses a  
 658 supercapacitor of size 1 F and rated voltage 270 V, and its stored energy can be expressed as:

$$659 \quad E_{SC} = \frac{1}{2} C U^2 \quad (40)$$

660 Where  $C$  is the capacitance value of the supercapacitor;  $U$  is the voltage of the supercapacitor.  
 661 Combining Eq. (39) and Eq. (40) with the simulation result, the efficiency of the GES system, in this  
 662 case, is 97.23%, and the efficiency of the power-based energy storage system is 96.45%. The efficiency  
 663 of HGES is the average of both weighted by the proportion of energy exchange, considering that the  
 664 energy exchange of the GES part is much larger than that of power-based energy storage, so the efficiency  
 665 of HGES should be close to 97%.



666  
 667 **Fig. 14.** Simulation results of distribution grid-level HGES system control signals with typical operating conditions

668 The control signal of the HGES at the distribution grid level is shown in Fig. 14, and the simulation  
 669 results are consistent with those in Table 2. Since the motor capacity used is small (15kW) for small-  
 670 scale distribution grid applications, there is no need to add a series starting resistor to assist in starting,  
 671 and the rotor starting resistor control signal is kept at -1 (i.e., no starting resistor is used). Due to the low  
 672 rotational inertia of the motor, the rotor braking resistor completes the motor's braking soon after it is  
 673 connected and then cut off.

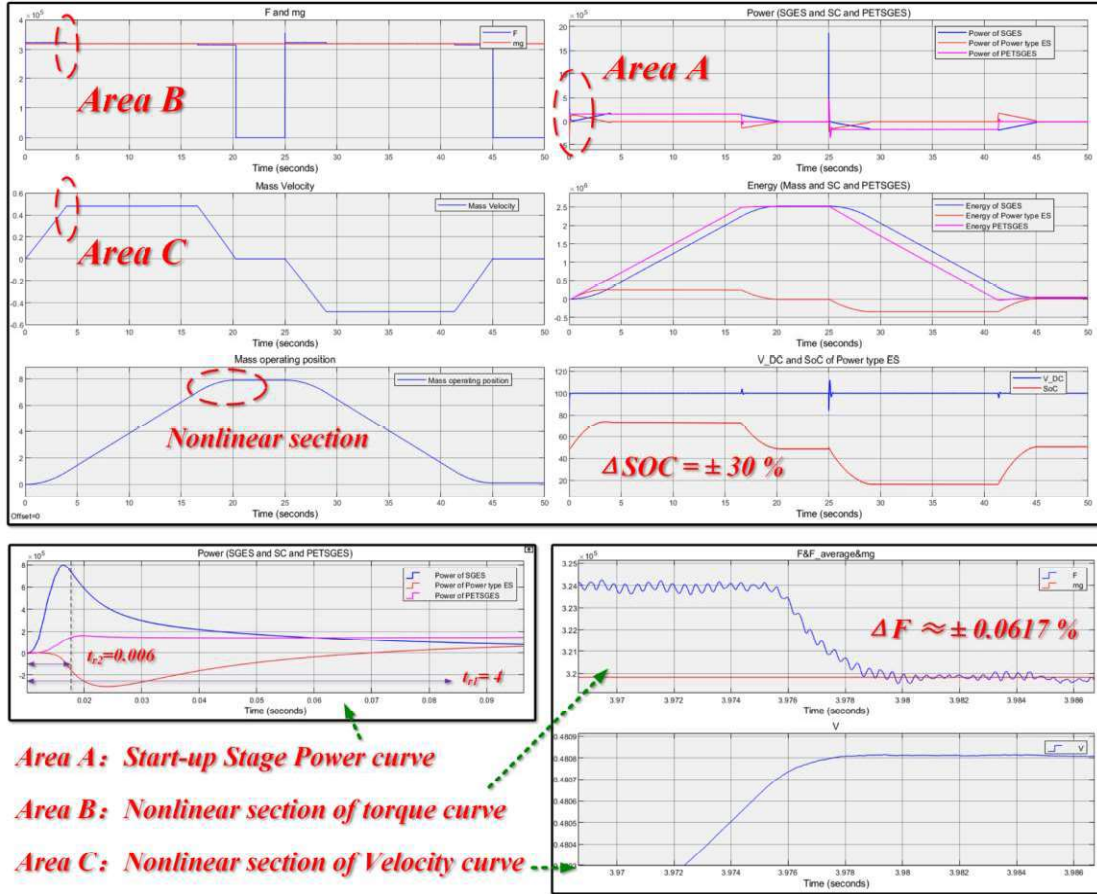
674 *7.2. Transmission grid-level HGES*

675 The simulation model of the transmission grid-level HGES is established based on the green part in  
 676 Fig. 12, the model parameters are shown in Table 5, and the simulation results are shown in Fig. 14.  
 677 Similarly, the simulation time is set to 50 seconds, in which the first 25 seconds the system is charged  
 678 and the next 25 seconds the system is discharged. Considering that an enormous height difference is more

679 likely to be used for GES at the transmission grid level, the rated speed of the mass module is 0.5 meters  
 680 per second, and the total vertical height displacement is set to 8 m (limited by the simulation duration,  
 681 which should be much more prominent in reality). Due to facing the transmission grid level application,  
 682 a squirrel-cage asynchronous motor with a rated capacity of 160 kW is used.

683 **Table.5 Simulation parameter table for transmission grid-level HGES**

Systems	Items	Parameters
Mechanical System	Mass	16.3 <i>t</i>
	Height of operation	8 <i>m</i>
	Rated operating velocity	0.5 <i>m/s</i>
Motor System	Rated capacity	160 <i>kW</i>
	Stator resistance	0.01379 $\Omega$
	Stator inductance	0.000152 <i>H</i>
	Rotor resistance	0.007728 $\Omega$
	Rotor inductance	0.000152 <i>H</i>
	Mutual inductance	0.00769 <i>H</i>
	Inertia	2.9 <i>kg * m<sup>2</sup></i>
	Friction coefficient	0.05658 <i>N * m * s</i>
	Number of pole pairs	2
	Rated frequency	50 <i>Hz</i>
Power-based ES (Supercapacitor)	Rated voltage	0.4 <i>kV</i>
	System capacity	30 <i>F</i>
	Unit rated voltage	2.7 <i>V</i>
	Number of units	600
	System Rated Voltage	1620 <i>V</i>
Electric Drive system	Initial Voltage	1145 <i>V</i>
	DC/DC Inductor	0.01 <i>H</i>
	Voltage stabilizing capacitor	0.019 <i>F</i>
	Switching device on-resistance	1e-3 $\Omega$
	Switching device blocking resistance	1e5 $\Omega$
	PWM frequency	10 <i>kHz</i>



684

685

Fig. 15. Simulation results of transmission grid-level HGES system states with typical operating conditions

686

The layout of Fig. 15 is essentially similar to that of Fig. 13, with the image in the second column of the third row additionally containing the percentages of the DC side voltage of the AC-DC-AC inverter. Comparing the images in the left column related to the operation of the mass module, we can see that the gravity storage for larger scale applications has a more pronounced nonlinear segment of the curve due to the use of a larger capacity motor (160kW vs. 15kW) with a heavier weight (32 tons vs. 7 tons), in line with the theoretical expectations of the fourth chapter section. It should be noted that the amplified torque curve also has small, fast fluctuations in addition to the nonlinear segment. Due to the current hysteresis control strategy, this high-frequency fluctuation is tiny and will be filtered out after going through the other inertial loops of the system.

695

Moreover, in this case, the rectangular-based compensation method and its power-based energy storage capacity configuration strategy are based on Eqs. (36) and (40) with a 20% capacity margin (taking into account power pulses from motor start-up or for fast power fluctuation smoothing, emergency inertia support, etc.) are validated, and the capacity configuration is derived from Eq. (41):

699

$$C = 2 \frac{t_{ramp} P_N - m V_N^2}{U_N^2 (1 - 2\gamma)} \quad (41)$$

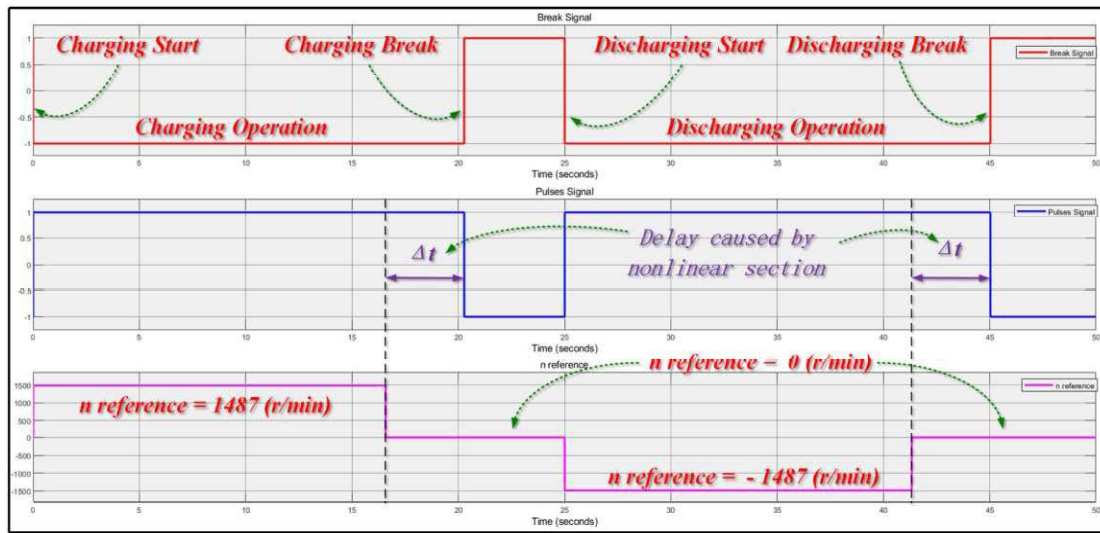
700

where  $t_{ramp}$  is the climb time of the motor speed (or mass module speed);  $P_N$  is the rated power of the compensated GES system;  $m$  is the mass of the mass module;  $V_N$  is the rated operating speed of the mass module;  $U_N$  is the rated voltage of the supercapacitor;  $\gamma$  is the stability margin expressed as a percentage. According to the designed capacity configuration, the SOC fluctuation of the actual power-based energy storage is limited to 30%, leaving a stability margin of 20%.

704

705 Due to the large capacity of the motor (160 kW), the rotating inertia is more considerable, and to  
 706 avoid excessive temperature rise due to overcurrent during the start-up stage. In this case, the motor start-  
 707 up time is set to 4 seconds, i.e., the full power response time of the gravimetric energy storage part is 4  
 708 seconds. Since the response time of power-based energy storage is in the millisecond range, the full  
 709 power response time of the hybrid energy storage system after combining power-based energy storage is  
 710 shortened to 6 milliseconds (similar to the application at the distribution grid level), which is a significant  
 711 performance improvement with a response speed of about 670 times compared to the original GES  
 712 system.

713 Similarly, the efficiency of the simulated gravity storage part under the transmission grid level case  
 714 is 98.63%, which is an improvement compared to 97.32% at the distribution grid level, as motor  
 715 efficiency generally rises with increasing capacity. Since the motor runs at the optimal operating point  
 716 based on FOC control, the output is the required rated power, so the power-based energy storage device  
 717 does not need to be compensated for stable operation. As a result, the energy exchange of the gravity  
 718 storage part becomes the absolute main body of the hybrid gravity storage system, so the efficiency of  
 719 the hybrid gravity storage system should also be close to 98%.



720  
 721 **Fig. 16.** Simulation results of transmission grid-level HGES system control signals with typical operating conditions

722 The control signal of the HGES at the transmission grid level is shown in Fig. 16, and the simulation  
 723 results are consistent with those in Table 3. Due to the larger motor capacity (160kW) used for larger-  
 724 scale transmission grid applications with higher rotational inertia, there is a more pronounced nonlinear  
 725 segment, and this transient process leads to a delay between the pulse signal and the speed reference  
 726 command.

727 *7.3. Discussion*

728 In both simulation cases, the HGES's efficiency is approximately equal to the GES's efficiency due  
 729 to the system's overall volume of energy exchange. The simulation results show that the cycle efficiency  
 730 of the GES is about 97%, which should be close to the square of the motor efficiency used - this is  
 731 obviously higher than the real situation - because this simulation case does not consider the energy loss  
 732 in the mechanical part of the GES. In fact, according to the HGES energy flow model shown in Fig. 5,  
 733 the losses of the GES system are mainly from the motor and mechanical losses, considering that the  
 734 power electronics are often very efficient. Therefore, the cycle efficiency obtained from this simulation

735 should be considered as the theoretical limit of the HGES cycle efficiency rather than the actual value.

736 The reason for not considering the mechanical system losses is that the GES system studied in this  
737 paper is an abstraction of various GES technologies (as shown in Fig. 2) and is the study of its most  
738 essential model. In contrast, the mechanical systems used in different GES technologies vary and cannot  
739 be generalized, so they are not considered in this study. The advantage of doing so is to ensure the  
740 generality of this study, which makes this study suitable for any GES technologies. If the actual efficiency  
741 of GES technologies is needed, only the efficiency of the corresponding mechanical system needs to be  
742 considered further.

743 From the energy perspective, another interesting phenomenon can be found in the study of HGES -  
744 under the rectangle-based compensation strategy, the energy of the hybrid energy storage system is time-  
745 shifted compared to the original GES system after the compensation of power-based energy storage. In  
746 fact, this is the very nature of energy storage systems - to decouple energy in space-time coordinates so  
747 that energy can be used in any time and space, thus achieving great flexibility.

748 Taking the hybrid gravity storage system as an example, we can find that the addition of power-  
749 based energy storage makes the energy of the hybrid system move on the time scale, while part of the  
750 transferred energy is transferred over space with power-based energy storage (in this case, supercapacitor)  
751 as the carrier. The power-based energy storage, as the energy storage in the storage system, optimizes the  
752 energy flow within the hybrid storage system, as the hybrid gravity storage system acts in the utility grid  
753 at a more macro-scale.

## 754 8 Conclusion

755 GES technology is a promising new large-scale energy storage technology, similar to pumped hydro  
756 storage, a typical energy-based energy storage technology. Combined with power-based energy storage  
757 technology, this paper proposes a hybrid GES technology based on the slow response of GES technology  
758 and the problem of significant output power fluctuation when loading and offloading heavy objects.

759 In this paper, we first analyze all possible structures of HGES and propose two appropriate HGES  
760 structures for distribution and transmission grid application scenarios. After obtaining a reasonable  
761 system structure, we analyze the control strategies of different structure schemes in detail according to  
762 three levels: device, single energy storage system, and hybrid energy storage system, including the power  
763 electronic control strategy at the bottom level, the control strategy of power-based energy storage, the  
764 control strategy of GES, and the overall control strategy of the hybrid system. In particular, three  
765 complementary capacity configuration schemes are also given for power-based energy storage in addition  
766 to the three basic control strategies. Finally, the simulated verification of the proposed hybrid energy  
767 storage system and its control strategy is completed based on MATLAB/Simulink platform.

768 The case simulation results of this study can be summarized as follows.

- 769 • The operation of the proposed HGES meets the theoretical expectations and verifies the  
770 feasibility of the proposed system structure approach, control strategy, and power-based  
771 energy storage configuration scheme.
- 772 • The power-based energy storage in the hybrid gravity storage system can well suppress the  
773 inherent power fluctuation problem of GES under the rectangular-based compensation strategy.
- 774 • The response speed of the HGES is improved by 1 to 2 orders of magnitude compared to the  
775 single GES system.
- 776 • The HGES can achieve more significant performance improvements in large-scale application

777 scenarios oriented to the transmission grid level.  
778 • The efficiency of the HGES will reach more than 95% without considering the mechanical  
779 system losses, and even considering the mechanical system losses, the HGES efficiency still  
780 promises to exceed 80% with a high-efficiency mechanical system.  
781 The proposed hybrid GES combines the large storage capacity of energy-based energy storage (MW  
782 level and above) with the high response speed of power-based energy storage (ms level). It is an ideal  
783 energy storage system without obvious performance drawbacks and will be expected to provide critical  
784 technical support for developing renewable energy power systems.

## 785 Data availability

786 The data that support the plots within this paper and other findings of this study are available from the  
787 corresponding author upon reasonable request.

## 788 Code availability

789 The code is available from the corresponding author upon reasonable request.

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879 The authors declare no competing interests.

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