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ESTIMATION OF THE CONSUMER DEMAND SYSTEM IN POSTWAR JAPAN

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PREFACE

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This paper is intended to present an analytical model of a consumer demand system and to give an example of its application to empirical data in postwar Japan. The model is called Powell's system, a type of linear expenditure system.

The linear expenditure system has been used by IIASA as a method of carrying out the analysis and prediction of the demand side in various national models concerned with the Food and Agriculture Program (FAP). It is hoped that this paper will be of some help in assessing the efficiency and usefulness of the linear expenditure system in the process of advancing the task at IIASA.

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FOREWORD

Understanding the nature and dimensions of the world food problem and the policies available to alleviate it has been the focal point of the IIASA Food and Agriculture Program since it began in 1977.

National food systems are highly interdependent, and yet the major policy options exist at the national level. Therefore, to explore these options, it is necessary both to develop policy models for national economies and to link them together by trade and capital transfers. For greater realism the models in this scheme are being kept descriptive, rather than normative. In the end it is proposed to link models to twenty countries, which together account for nearly 80 per cent of important agricultural attributes such as area, production, population, exports, imports and so on.

The linear expenditure system used by the Food and Agriculture Program for analysis and description of the demand side within the national models is examined in both a static and a dynamic version by Kozo Sasaki for the case of postwar Japan. This is a further step towards the development of a detailed agricultural model for Japan.

> Kirit Parikh Program Leader

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1. INTRODUCTION

The objectives of this study are to estimate the demand system for subgroups of commodities and to clarify the changes in consumer demand and their characteristics, using the time series of family budget data in postwar Japan.

As is commonly known, the condition of consumption improved remarkably from the deficient state to the present high level, as the Japanese economy rapidly recovered from the war-devastated state and reached the high standard of living of today. In the meantime, consumer demand has apparently undergone a marked change. Data used in the analysis are those of *All Households in Cities with Population of 50,000 or More.* The period covered is 27 years, from 1951 to 1977, and excludes the immediate postwar years. The analytical method adopted is the linear expenditure system developed by A.A. Powell (1966, 1968), which corresponds to a particular utility function and is effective in analyzing a number of commodities under the assumption of directly additive preferences. It is a variant of J.R.N. Stone's classical linear expenditure system (Stone 1954), which was simplified for estimation purposes.

First, a linear approximation by the static version of the linear expenditure system is made for appropriate segments of the entire period, since there have been remarkable changes in consumption patterns over the past three decades. Estimated parameters of the demand model yield estimates of income and price elasticities of demand, income flexibility or Frisch's money flexibility, subsistence consumption levels, etc. At the same time, changing patterns of those demand and utility parameters are examined. Second, taste variables are introduced into the demand system in order to make it a dynamic one. It is of some interest to see to what extent the estimated parameters are stable over time and across alternative specifications of demand model.

Nonlinearity of the demand system to be estimated necessarily arouses our interest in the convergence process of estimates. Various statistical tests are undertaken for the results obtained.

2. METHOD

2.1. Static Model of the Linear Expenditure System

Powell's system, which is directly applied to this analysis, enables us to derive a number of commodity expenditure functions from empirical data on such few variables as expenditures and prices. It is designed to reduce considerably the number of parameters to be estimated and to avoid the burdensome problem of multi-colinearity.

A brief description of Powell's system may be necessary for this discussion. Generally, a simple static model of the linear expenditure system is written as a set of linear expenditure functions in prices and income with fixed coefficients. In the case of marked changes in tastes, such a static model may be easily transformed into a dynamic one by introducing an additional term which allows for shifts of expenditure functions. With the three theoretical restrictions of additivity, homogeneity, and symmetry incorporated into the static model, the linear expenditure system of the Stone type is obtained.

The distinction of Powell's system is that the assumption of directly additive preferences is locally imposed upon this demand system at the sample means of all variables. The underlying assumption is characterized by the symmetry restriction. Apart from both additivity and homogeneity, symmetry is given as the condition that, at sample means, the substitution effect between any pair of different commodities is proportional to the two relevant income derivatives.¹

Thus the static model is transformed into the following expression:

$$\mathbf{v}_{it} = \mathbf{p}_{it} \overline{\mathbf{x}}_i + \lambda \mathbf{z}_{it} + \mathbf{b}_i \mathbf{u}_t + \boldsymbol{\varepsilon}_{it}, \qquad (i = 1, 2, \dots, N)$$
(1)

(t = 1, 2, ..., T)

where

$$z_{it} = b_i \sum_j b_j (p_{jt} / \overline{p}_j - p_{it} / \overline{p}_i), \qquad (i, j = 1, 2, ..., N)$$

$$u_t = m_t - \sum_j p_{jt} \overline{x}_j \qquad (3)$$

The v_{it} , p_{it} , and x_{it} indicate per capita expenditure on the <u>i</u>th commodity, the price of the <u>i</u>th commodity, and the quantity consumed per capita of the <u>i</u>th commodity during time t, respectively. The m_t denotes per capita income or total expenditure during time t. The \overline{p}_i , \overline{x}_i ($\overline{x}_i \equiv \overline{v}_i/\overline{p}_i$) and \overline{v}_i represent the sample means of p_i , x_i , and v_i . The λ is Houthakker's income flexibility;² that is, a proportionality factor which appears in the cross substitution of effects under the additive preference postulate. It is related to the marginal utility of income ω in the following manner:

$$\lambda = -\omega/\left(\partial\omega/\partial\mathbf{m}\right) \tag{4}$$

Moreover, b_i and ε_{it} are the marginal budget share of the <u>i</u>th commodity and the residual respectively. Both λ and b_i are behavioral parameters to be estimated, so that equation (1) proves to be nonlinear in unknown parameters. The estimating equation is written as

$$y_{it} = \lambda z_{it} + b_i u_t + \varepsilon_{it}$$
(5)

where

$$y_{it} \equiv v_{it} - p_{it}\overline{x}_{i}$$

The y_{it} is the difference between actual expenditure and the presumed expenditure for the purchase of sample mean quantity of the <u>i</u>th commodity during time t. The z_{it} is the variable associated with substitution effects.³ The u_t is the difference between the actual total expenditure and the total presumed expenditure for the purchase of sample mean quantities of all commodities during time t. According to this analytical model, changes in the quantity of each commodity consumed are represented by its variations around the sample mean, while changes in income during each time t are represented by changes in the remaining income after deduction of the total expenditure for all sample mean quantities from the current total expenditure. The average values of y_i , z_i , and u are all set equal to zero.

Income and price elasticities of demand, evaluated at sample means, are derived from equation (1) as

$$\overline{E}_i = b_i / \overline{w}_i \tag{6}$$

and

$$\overline{e}_{ij} = \begin{cases} \varphi \overline{E}_i - \overline{w}_i \overline{E}_i (1 + \varphi \overline{E}_i), \ (i = j), \\ -\overline{w}_j \overline{E}_i (1 + \varphi \overline{E}_j), \ (i \neq j) \end{cases}$$
(7)

 \overline{E}_i is the income elasticity of the <u>i</u>th commodity calculated at sample means, \overline{e}_{ij} is the price elasticity of the <u>i</u>th commodity calculated at sample means with respect to the jth price, \overline{w}_i is the sample mean average budget share or budget proportion of the <u>i</u>th commodity, and φ is Theil's income flexibility, that is, the

reciprocal of the income elasticity of the marginal utility of income.

The corresponding utility function is of the Stone-Geary type:

$$U = \sum_{i} b_{i} \log(x_{i} - \beta_{i}), \ b_{i} > 0, \ \sum_{i} b_{i} = 1, \ (x_{i} - \beta_{i}) > 0$$
(8)

where

 $\beta_i = \overline{x}_i - b_i \lambda / \overline{p}_i$

2.2. Dynamic Model: Introduction of the Taste Variable

A dynamic factor should be taken into account in constructing a demand system which covers a long period of time. As previously stated, the static model can be readily converted into a dynamic one by introducing a taste variable into the demand system. Thereby, equation (1) is transformed into

$$\mathbf{v}_{it} = \mathbf{p}_{it}\overline{\mathbf{x}}_i + \lambda \mathbf{z}_{it} + \mathbf{b}_i \mathbf{u}_t + \mathbf{c}_{ist} + \varepsilon_{it}$$
(9)

where s_t stands for the level of taste variable during time t, and c_i is its coefficient. The s_t is common to all of the N expenditure functions. Similarly, equation (2) is modified as

$$y_{it} = \lambda z_{it} + b_i u_t + c_i s_t + \varepsilon_{it}$$
(10)

Although time trend is often used as a proxy for the taste variable, it does not seem to serve as such an explanatory variable in this model, because of its high correlation with the income variable ut. Let us consider two alternative specifications for the proxy; that is, an annual increase in income and an annual rate of increase in income. They are written as follows:

$$\mathbf{s}_t = \mathbf{m}_t - \mathbf{m}_{t-1} \tag{11}$$

and

$$s_t = (m_t - m_{t-1}) / m_{t-1}, respectively$$
(12)

All values of the s_t for each specification can be adjusted in such a way that they sum to zero, and the average is also equal to zero. In this case, additivity is globally satisfied, but both homogeneity and symmetry are fulfilled only at sample means. Furthermore, β_i is rewritten as

$$\beta_{it} = \overline{x}_i - (b_i \lambda / \overline{p}_i) + (c_i s_t / p_{it})$$
(13)

3. ESTIMATION PROCEDURE

The estimating equation (5) in the static model is compactly expressed by Zellner's block diagonal specification:

y 1)	z_1	u	0				0]	ſλ	}	$\left[\varepsilon_{1} \right]$
У2		Z2	0	u	•				bı		ε2
{ ·	} =			•		•			4.	 +	٠ ،
			•	·	•	•	•	0		}	
y _N	ļ	ZN	0			-	0	u	b _N		ε _N

where y_i , z_i , u_i , and ε_i are (T×1) vectors. Equation (14) is also written as

$$y = X\gamma + \varepsilon \tag{14}$$

where

$$y = (y_1', \dots, y_N')'$$

$$\varepsilon = (\varepsilon_1', \dots, \varepsilon_N')'$$

$$\gamma = (\lambda, b_1, \dots, b_N)'$$

and X indicates the (NT×(N+1)) matrix on the right hand side of equation (14). For simplicity of estimation, systems least squares method is used.⁴ Least squares estimator of γ is obtained by minimizing the residual sum of squares over all equations and all observations:⁵

$$\widehat{\gamma} = (X'X)^{-1}X'y \tag{15}$$

This result is partly described as

$$\hat{\mathbf{X}} = \sum_{i} \mathbf{N}_{i} / \sum_{i} \mathbf{D}_{i}$$
(16)

where

$$N_{i} = \begin{vmatrix} \sum_{t} z_{it} y_{it} & \sum_{t} z_{it} u_{t} \\ \sum_{t} u_{t} y_{it} & \sum_{t} (u_{t})^{2} \end{vmatrix}$$
(17)

$$D_{i} = \begin{vmatrix} \sum_{t} (z_{it})^{2} & \sum_{t} z_{it} u_{t} \\ \sum_{t} u_{t} z_{it} & \sum_{t} (u_{t})^{2} \end{vmatrix}$$
(18)

The equation for estimating b_i results in

$$y_{it}' = b_i u_t + \varepsilon_{it}$$
 (i = 1,2,...,N) (19)
(t = 1,2,...,T).

where

 $y_{it}' \equiv y_{it} - \hat{\lambda} z_{it}$

The estimates of b_i 's are obtained by applying ordinary least squares to each equation in (19) separately. Since z_{it} is a function in unknown parameters as shown in equation (2), equation (5) or (14) is nonlinear in unknown parameters, and its estimation requires an iterative procedure.

Under the simple assumption of the error structure⁶, behavioral parameters λ and b_i are estimated by an iteration of linear regressions. If z_{it} is regarded as an exogenous variable for the present, unbiased estimates are obtained for λ and b_i , and their standard errors can be computed.⁷ Thus, it is possible to test the significance of estimated parameters.

Prior to the iterative estimation of Powell's system, starting values of the marginal budget shares b_i 's should be sought to treat z_{it} as an exogenous variable. For this purpose, it is convenient to get the estimates of b_i 's from Leser's system⁸ (Leser 1960 and 1961), which is along the lines of Powell's. Examination of the convergence of estimated parameter $\hat{\lambda}$ is sufficient to show the convergence of the whole system. It is decided that convergence has been reached when the relative deviation of $\hat{\lambda}$ between two consecutive iterations has dropped below 0.01 percent.⁹

On the other hand, the estimating equation (10) in the dynamic model is also transformed, and hence equations (17) - (19) have to be modified¹⁰ in

estimating a set of λ , b_i , and c_i .

4. DATA AND ESTIMATION

The above models are fitted to empirical data on household expenditures and prices to derive the consumer demand system on a per capita basis in the postwar period. The data sources are Annual Report on the Family Income and Expenditure Survey and Annual Report on the Consumer Price Index.

As regards the classification of commodities, total expenditure is first decomposed into 24 subgroups of commodities as listed in Table 1 with 11 subgroups of food commodities and 13 subgroups of nonfood commodities. Some of the 24 subgroups are further aggregated into fewer groups in specified periods where required. It is of our great concern to analyze as many commodity groups as possible under given assumptions.

As for the classification of food commodities, the following would be noteworthy: the subgroup of other cereals contains barley, wheat flour, bread, rice-cakes, etc.; meat includes beef, pork, chicken, ham, and sausages; milk and eggs subgroup also includes powdered milk, butter and cheese; processed food involves dried food (beans, mushrooms, laver, etc.), cooked and canned food, and condiments (sugar, fat and oil, etc.); fruits comprise oranges, apples, strawberries, grapes, etc.; and beverages is composed of alcoholic ("sake," beer, whiskey, wine) and nonalcoholic (tea, coffee, fruit juice, lactic drinks, etc.) beverages. In regard to the non-food commodities, subgroups of public transportation, communication and private transportation; education and stationery; and of recreation, reading, and other miscellaneous items are respectively aggregated at the start into a single group.

The major notations and data used in the analysis are as follows:¹¹

- $p_i = price of the <u>i</u>th subgroup, deflated by the General Consumer Price Index$ (i = 1.2 - 24) = 1070 prices = 1)
 - (i = 1, 2, ..., 24; 1970 prices = 1)
- $x_i =$ quantity yearly consumed per capita of the <u>i</u>th subgroup (expenditure in constant 1970 prices)
- m = yearly income per capita, deflated by the General Consumer Price Index (total expenditure in 1970 yen)

Price index is taken as an individual price for each subgroup of commodities. The base year is 1970, the prices of which are all set equal to unity.

At the first step of estimation, Leser's system¹² was fitted to the same data to obtain the starting values of b_i estimates. This system also has a common parameter to all equations, which is viewed as the average elasticity of substitution. Its value was confined to the range between 0 and 1 in the static model, as considered in Leser (1960, 1961). However, this restriction was relaxed in the dynamic model because, in a few cases, estimates of the common parameter centered about unity, and their empirical meaning seemed reasonable.

Starting with the estimation of the static model, an iterative procedure was undertaken by least squares to find the estimates of demand parameters for various segments of the whole period. Then, such a static approach ensured the linearity of expenditure functions over the specific subperiods at the particular levels of commodity breakdown. The estimates of static parameters converged so fast that many of the iterative estimations ended within ten rounds.

The dynamic model was fitted to longer time series of a similar data set, using a 21-commodity breakdown. The iteration took more rounds, but the speed of convergence was such that iteration terminated within 19 rounds in all cases undertaken.

Subperiod	L	1951	-1960				196	1-1970				196	3-1977	·· <u> </u>	
	Marginal Sha:	budget re	Correla coeffic	ation ient	Serial corr.	Marginal shar	budget re	Correla coeffic	ation sient	Serial corr.	Marginal b Shar	udget e	Correla coeffic	ation ient	Serial corr.
i	<u> </u>	t ratio	r _{y'.u}	R	coeff.	ĥ	t ratio	r _{v'.u}	R	coeff.	ĥi	t ratio	r _{v'. u}	R	coeff.
1 Rice	.0415	5.891	.901	.952	.274	0740	16.595	986	.943	.019	0518	14.475	970	.957	.562••
2 Other cereals	0403	10.058	- 963	.953	.310	.0064	4.192	.829	.834	.499	.0034	3.399	.686	.957	.073
3 Fish	.0109	3.953	.813	.837	.185	.0047•	2.092	.595•	.986	191	.0036+	1.727	.432•	.984	183
4 Meat	.0357	16.740	.986	.986	.316	.0461	18.641	.989	.990	.613					
5 Milk + eggs	.0447	22.506	.992	.991	.125	.0327	7.197	.931	.841	.592	.0526	2.283	.988	.983	.282
6 Vegetables	0028•	. 93 5	314•	.756	133	.0100	4.199	.829	.970	125	.0142	15. 6 36	.974	.991	293
7 Processed food	.0521	13.530	.979	.965	.349	.0181	10.211	.964	.944	.310	.0169	15.274	.973	.987	.034
8 Cakes	0336	10 849	088	020	002	.01 6 7	17.715	.987	.983	097	.0115	15. 3 05	.973	.978	.480
9 Fruits	.0330	10.040	.800	.920	F.003	.0301	12.385	.975	.969	.341	.0214	8.708	.729	.850	.467
10 Bevera ges	.0323	16.824	.986	.981	.405	.0467	51.334	.998	.998	529	.0376	21.049	.986	.975	.570**
11 F.a.f.h. ^a	.0479	15.532	.984	.983	.425	.0451	20.343	.990	.991	.585	.0495	44.984	.997	.997	.195
12 Rent	.0229	5.135	.876	.958	.527	.0352	8.636	.950	.968	.599	.0422	30.986	.993	.993	042
13 Repairs ^b	.0257	8.707	. 9 51	.949	.105	.0158	7.620	.937	.945	.078	0107	F 021	050	0.17	170
14 Water charges	.0049	8.322	.947	.966	.210	.0069	17.510	.987	.985	.337	.0127	5.961	.856	.947	.476
15 Furniture	.0822	8.318	.947	.948	.559	.0767	8.279	.946	.925	.710**	.0692	9.294	.932	.888	.799**
16 Fuel + light	.0345	15.828	.984	.990	041	.0436	19.379	.990	.937	.397	.0476	19.073	.983	.955	.444
17 Clothes	1384	11 680	072	025	167	.0769	16.999	.986	.979	.570	.0802	23.088	.988	.988	.207
18 Personal effects	.1304	11.000	.812	.930	157	.0174	7.826	.940	.914	.231	.0091	7.449	. 90 0	.746	.276
19 Medical care	. 032 5	18.431	.988	.979	.361	.0393	20.137	.990	.987	159	.0381	46.541	.997	.995	281
20 Toilet care	.0257	10.173	.963	.972	.581	.0234	18.168	.988	.986	.362	.0167	13.187	.965	.966	.309
21 Transportation $^{\mathbf{c}}$.0237	21.311	.991	.993	.222	.1090	27.203	.995	.994	688 ••	.1180	20.100	.984	.982	.188
22 Education	. 036 5	8.034	.943	.962	.594	.0125•	1.463	.459•	.775	.699••	0061	2.404	555	.859	.389
23 Tobacco	3105	25 834	004	004	264	.0080	9.575	.959	.939	.403	4105	00.040	001	001	~~
24 Recreation ^d	.5185	cJ.030	.004	. 884	.604	.3528	82.152	.999	.999	.354	.4135	33,346	.994	.894	.771**
λ	47.027	2.388	(\$\varphi = .	407)		82.652	6.062	(∅ = –	.410)		110.626	3.357	(.450)	

Table 1. Estimates of Demand Parameters \hat{b}_i , $\hat{\lambda}$ by Subperiod (Static Model)

^aF.a.f.h. indicates food away from home. ^bRepairs include maintenance. ^cTransportation also contains communication. ^dRecreation includes miscellaneous.

*insignificant at 5 percent (\hat{b}_i) **significant at 5 percent (serial correlation coefficient) $\hat{\varphi} = -\hat{\lambda}/m$

5. EMPIRICAL RESULTS OF THE STATIC MODEL

5.1. Estimates of Demand Parameters

Demand parameters estimated by the static model for three sample periods, which are relatively good from a statistical viewpoint, are summarized in Table 1. As demand relations have not been stable since the mid-1960s, sample periods partly overlap.

It seems relatively difficult to estimate demand relations in later subperiods owing to a change in consumers' béhavior. Consumers are considered to have lately become quite moderate in purchasing, facing simultaneously a steep rise in prices and considerable slowdown of economic growth. Per capita deflated income (or total expenditure) increased by 80 percent in 1951-60, 58 percent in 1961-70, and only 35 percent in 1968-77.

In the first subperiod (1951-60), other cereals belonged to an inferior good, while vegetables did not show an increase in consumption. Although inferior goods are ruled out from an additive utility function, a few of them do exist at the subgroup level of commodity classification. After parameters b_i and λ are estimated, a system of expenditure functions (1) is determined as well as demand elasticities (6) and (7). As a measure of goodness of fit, the multiple correlation coefficient was indirectly computed for each expenditure function, ¹³ in addition to the simple correlation coefficient in equation (19). The multiple correlation coefficients obtained in this way are generally high. There is no first order serial correlation in the error term. The fitted model shows a high fit in the total test, as most of the measures of fit¹⁴ indicate an accuracy of 80 percent or more.

In the second subperiod (1961-70), rice changed to an inferior good, while other cereals and vegetables turned to normal goods. Expenditures except for rice increased steadily. The multiple correlation coefficients are high as a whole, and the measures of fit are mostly at the level of 90 percent in the total test.

In the third subperiod (1963-77), during which the national economy grew substantially less than in previous subperiods and prices went on rising sharply, consumer demand was restrained to a considerable degree. The income coefficient for education is negative, as is that of rice. As for rice, both deflated expenditure and the expenditure in 1970 prices declined. In the case of education, the expenditure in 1970 prices showed a downward tendency due to the steep rise in its relative price in recent years, although the deflated expenditure increased. In this respect, it may not be appropriate to call it an inferior good indiscriminately. Serial correlation is not serious, but the Durbin-Watson test appears more severe.

5.2. Demand Elasticities

Price and income elasticities computed from estimated parameters and observed data are given by subperiod in Tables 2-4.

In the first subperiod (Table 2) income elasticity is particularly large for furniture, food away from home, milk and eggs, repairs, recreation, etc.; and their own price elasticities are also relatively high. The own price elasticity for furniture exceeds unity in absolute value. For this subgroup, the estimate of subsistence parameter β_i shows a negative sign. An inferior good has necessarily positive own price elasticity and is a net complement for all normal goods.

In the second subperiod (Table 3) income elasticity is quite large for transportation, furniture, medical care, beverages, and food away from home. It

Shares [w]]				•	;		I			I	ŀ											
	-	~	e	4	ۍ	8	~	8-9	0	=	12	13	14	12	16	17-18	18	20	21	22	23-24	ក្រវ
1 Rice	- 170	- 012	014	-00	- 002	- 012	018	- 010 -	8	000	8	8	100	100	012	022	5003-	900	003	-005	.020	328
2 Other cereals	.129	540	.050	013	900.	.044	990	.035	015	.00.	.014 .0	004	- 003	-005	.044	080	010	.027	110.	018	170.	-1.180
3 Fish	- 025	012	105	003	002	800	- 013	- 003 -	- 003	.000	.003	- 100	100	100.	600	016	002	- 900	002	004	• 10	233
4 Meat	154	071	058	08°;-	010	052	0 70	042	- 210	100.	- 910	500	.003	900	.053	095	012	032	013	023	085	1.408
5 Milk + eggs	-, 194	060'-	075	610'-	736	066	100	- 063	.022		.021	800	004	808	.067	120	015	- 041	016	029	107	1.778
8 Vegetubles	.008	0 0	.003	100'-	1 00	034	8	.002	100	.000	· 100.	000	. 000	000	.003	.005	-001	.002	1 00	100	<u>900</u>	077
7 Processed food	074	034	028	007	- 005	025	312	- 020 -	808	.001	- 800	- 200.	.002	.003	.025	046	-,006	015	008	011	041	.673
B-9 Cakes																						
+ fruits	084	039	032	900	005	620	043	- 337 -	- 010	- 100	600	- 200	.002	.003	.029	052	007	018	007	013	047	.770
10 Beverages	139	084	053	014	600'-	047	071	- 900	- 183.	- 100	- 910	- 100	.003	- 60	.048	066	110	029	- 01 1	021	077	1.266
11 F.a.t.h.	258	119	099	-:025	018	087	133	- 120'-	.029	.962	.028	- 900	900.	.010	.089	160	020	- 054	021	039	143	2.368
12 Rent	119	055	-,046	012	008	040	190'-	- 033	. 610.	- 100	.457	- 100	.003	800	16	074	600'-	025	010'-	018	066	1.090
13 Repairs	201	093	078	020	013	068	103	- 0550	- 023	- 100	.021 -	- 992.	.005	900	.069	125	016	042	017	030	111	1.840
14 Water charges	120	055	- 046	012	- 008	041	062	- 033	- 014 -	100	- 610.	500	.448	300.	8	074	800'-	025	010	018	066	1.004
15 Furniture	308	142	- 119	030	020	-104	158	.084	- 035 -	.002	.033	- 010	1- 200.	1.134	.106	190	024	065	025	046	170	2.812
16 Fuel + light	073	034	028	007	· 005	025	038	- 020 -	- 900	.00	- 900	- 200	.002	.003	.297	045	- 006	015	006	011	040	.667
17-18 Clothing + pe	Ł																					
sonal effects	-, 121	056	047	012	-,008	041	062	- 033	- 410	- 100	- 610.	- 100.	.003	80.	042	526	. 000-	025	010	018	067	1.108
19 Medical care	163	075	063	016	-,010	055	084	- 045	- 810	.001	.017 -	- 900	.004	9 0 0.	.056	101	620	034	013	025	080	1.401
20 Toilet care	084	90	032	- 008	-000	028	043	023	600	100	- 600.	- 003	.002	003	-029	052	007	- 331	007	013	047	.788
21 Transportation	-, 139	064	053	014	. 009	047	120'-	038	- 010	100	- 015 -	- 100	E00.	900	048	-,066	110'-	029	528	021	077	1.267
22 Education	128	059	049	013	-,008	043	066	- 035	- 014	100	- 10.	- 100.	.003	80	-044	-079	010	027	110'-	484	170	1.166
23-24 Tobacco																						
+ recreation	- 183	085	071	018	-,012	062	084	- 020 -	- 021	100	- 030	- 900	004	600.	063	113	014	038	015	028	784	1.675
W	.126	.034	466	.025	020	.036	.077	.044	026	.020	120	014	604	029	.052	.123	220	.033	610.	160.	181.	

Table 2 Demand Elasticities Estimated for Twenty-one Subgroups at the Sample Means of all Variables in 1951–1960 $[\overline{e}_{ij}, \overline{E}_{i}]$ and Sample Mean Average Budget

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 $\overline{\sigma}_{ij}$ = elasticity of subgroup i with respect to the j-th price calculated at sample means \overline{E}_i = income elasticity of subgroup i calculated at sample means \overline{w}_j = budget share of subgroup j calculated at sample means

,	, 1	2	2	3	4	5	6	7	6	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	Ē
1 Rice	.61	7 .0	17	.043	.020	.021	.032	.061	.018	.010	.014	.014	.019	.013	.002	.020	.031	.062	.032	.011	.025	009	.035	.007	.118	-1.231
2 Other cereals	03	510	32	013	006	007	010	019	005	003	004	004	008	004	001	008	010	019	010	003	008	.003	011	002	038	.382
3 Fish	01	100	02	056	002	002	003	006	002	001	001	001	002	001	.000	002	003	006	003	001	003	.001	004	001	012	.126
4 Meat	11	80	18	046	557	022	034	065	019	011	015	015	020	014	003	021	033	065	034	011	028	.010	038	007	122	1.305
5 Milk + eggs	09	?0)	15	038	018	- 458	028	053	015	009	012	012	017	011	002	017	027	- 054	028	009	022	.008	031	-,006	101	1.072
6 Vegetables	03	000)5	011	005	006	143	016	005	003	004	004	005	003	001	005	008	016	009	003	00?	.003	009	002	031	.327
7 Processed food	02	900)4	011	-,005	005	008	145	005	003	004	004	005	003	001	005	008	016	008	003	.006	.002	009	002	030	.316
8 Cakes	07	101	11	028	013	013	021	039	335	007	609	009	012	008	002	013	- 020	040	021	007	016	.006	023	004	074	.790
9 Fruits	13	202	21	051	-,024	025	039	073	021	611	016	017	023	- 015	003	023	037	073	038	013	029	.011	042	008	137	1.460
10 Beverages	13	902	22	054	025	028	041	077	022	013	648	017	024	016	003	025	039	- 077	040	013	~.031	S10.	044	009	144	1.537
11 F.a.f.h.	13	702	21	053	025	028	040	075	022	013	017	638	024	018	003	024	038	076	040	013	030	S10.	044	009	142	1.513
12 Rent	10	60	16	041	019	020	~.031	058	017	010	013	013	498	012	002	019	030	059	031	010	023	.009	034	007	110	1.168
13 Repairs	08	401	13	033	015	016	025	046	013	008	010	011	015	393	002	015	024	04?	024	008	019	.007	027	005	088	.933
14 Water charges	12	902	20	050	024	024	038	071	020	012	016	016	- 022	015	590	023	036	072	038	013	029	.011	041	008	~.134	1.430
15 Furniture	14	602	23	- 057	027	026	043	061	023	013	016	018	025	017	003	689	041	081	042	014	032	.012	047	009	152	1.618
16 Fuel + light	09	101	14	035	017	017	027	050	014	008	011	011	- 016	011	002	016	439	051	028	009	020	.008	029	006	095	1.009
17 Clothes	08	501	13	033	015	018	025	047	013	008	011	011	015	010	002	015	024	434	025	008	019	.007	027	~.005	088	.942
18 Personal effect	s04	700)7	018	009	009	014	026	007	004	006	008	008	005	001	008	013	028	227	005	010	.004	015	003	- 049	.521
19 Medical care	14	3 ~.02	2	056	026	027	042	079	023	013	018	018	025	018	003	025	040	079	041	662	- 032	.012	048	009	148	1.579
20 Toilet care	07	101	1	028	- 013	013	021	039	011	007	009	009	012	008	002	013	020	040	021	007	340	.006	023	004	074	.789
21 Transportation	20	604	11	- 103	048	050	078	148	042	024	033	033	046	031	008	047	075	147	077	-,028	059	1.184	085	017	276	.2.941
22 Education	03	300	26	013	006	006	010	018	005	003	004	004	006	004	001	006	009	018	010	003	007	.603	162	002	035	.368
23 Tobacco	06	101	13	032	015	015	024	045	013	007	010	010	014	009	002	014	023	045	024	008	018	.007	026	373	084	.897
24 Recreation	13	402	21	052	024	025	039	074	021	012	017	017	023	015	003	024	037	074	039	013	030	.011	043	008	745	1.479
Wi	.06	0.0	17_	.037	.035	.030	.030	.057	.021	.021	.030	.030	.030	.017	.005	.047	.043	.082	.033	.025	.030	.03?	.034	.009	.239	

Table 3. Demand Elasticities Estimated for Twenty-four Subgroups at the Sample Means of all Variables in 1961–1970 $[\overline{e}_{ij}, \overline{E}_i]$ and Sample Mean Average Budget Shares $\{\overline{w}_i\}$

 \overline{e}_{ij} = elasticity of subgroup i with respect to the j-th price calculated at sample

 $\frac{means}{\overline{E}_i} = \text{income elasticity of subgroup i calculated at sample means}$ $\overline{w}_j = \text{budget share of subgroup j calculated at sample means}$

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j	1	2	3	4-5	6	7	6	9	10	11	12	13-14	15	16	17	18	19	20	21	22	23-24	Ē,
1 Rice	.633	.018	.044	.048	.027	.053	.018	.013	.016	.013	.015	.020	.020	.023	.054	.032	.011	.025	004	.04 i	.106	-1.226
2 Other cereals	014	10 }	008	008	005	009	003	002	003	002	003	004	004	004	010	006	002	004	.001	007	019	.218
3 Fish	006	001	046	004	002	004	001	001	001	001	001	- 002	002	- 002	004	002	001	002	.000	003	008	.095
4-5 Meat,																						
milk,etc.	055	012	030	409	019	038	012	009	011	009	011	014	014	016	037	022	007	017	.002	028	073	.838
6 Vegetables	032	007	018	019	233	021	007	- 005	006	005	006	008	008	010	022	013	004	010	.001	016	043	.492
7 Processed food	022	005	012	013	007	163	005	003	004	004	004	005	005	008	015	009	003	007	.001	011	029	.330
8 Cakes	- 038	008	021	023	013	025	272	006	008	006	007	010	009	011	026	015	005	012	.002	019	051	.584
9 Fruits	070	015	038	042	024	046	018	491	014	012	013	017	017	020	047	027	009	021	.003	035	093	1.066
10 Beverages	062	018	045	049	028	055	016	013	~.581	014	018	020	020	023	055	032	010	025	.004	042	109	1.253
11 F.a.f.h.	078	021	054	058	033	085	022	018	019	686	019	024	024	028	065	038	013	- 030	.004	049	129	1.488
12 Rent	087	019	048	052	030	058	019	014	017	015	618	022	022	.025	059	034	011	- 027	.004	044	116	1.334
13 Repairs																						
+ water	036	008	021	023	013	025	008	006	008	006	007	- 268	009	011	025	015	005	012	.002	019	450	.575
15 Furniture	096	021	- 053	057	033	064	021	015	019	016	018	024	682	027	064	038	013	029	.004	049	127	1.461
16 Fuel + light	078	017	- 043	047	027	052	017	012	016	013	015	019	019	556	052	031	010	024	.003	039	103	1.186
17 Clothing	086	014	- 036	039	023	044	015	010	013	011	013	016	018	019	495	026	~.009	020	.003	033	087	1.002
18 Personal effects	020	004	011	012	007	013	004	003	004	003	004	005	005	006	013	145	~.003	006	.001	010	026	.305
19 Medical care	097	021	053	058	033	064	022	015	019	018	019	024	024	028	065	038	~.678	030	.004	~.049	128	1.478
20 Toilet care	040	009	022	024	014	028	009	008	008	087	008	010	010	011	027	018	005	285	.002	020	053	.605
21 Transportation	154	034	- 065	092	053	102	034	- 025	031	028	030	038	038	044	103	061	020	047	-1.050	078	204	2.347
22 Education	.013	.003	.007	.008	.004	.009	.003	.002	.003	.002	.003	.003	.003	.004	.009	.005	S00.	.004	001	.097	.017	200
23-24 Tobacco																						
+ recreation	099	`022	055	059	034	066	022	016	019	017	019	025	- 025	- 028	067	039	013	030	.004	050	813	1.514
w _i	.042	.016	.038	.063	.029	.051	.020	.020	.030	.033	.032	.022	.047	.040	.080	.030	.026	.028	050	. 0 30	.273	

Table 4. Demand Elasticities Estimated for Twenty-one Subgroups at the Sample Means of all Variables in 1963–1977 $[\overline{e}_{ij}, \overline{E}_i]$ and Sample Mean Average Budget Shares $[\overline{w}_j]$

 \overline{e}_{ij} = elasticity of subgroup i with respect to the j-th price calculated at sample means

 $\overline{\widetilde{E}}_i$ = income elasticity of subgroup i calculated at sample means \overline{w}_i = budget share of subgroup j calculated at sample means

also increased for cakes, fruits, rent, water charges, fuel and light, etc. Demand for transportation is highly responsive to a change in its price.

In the third subperiod (Table 4) transportation, recreation, food away from home, medical care, and furniture are rather high in income elasticity, while income elasticities of rent, fuel and light, clothes, etc., increased in comparison with the second subperiod.

It is apparent that the demand for subgroups of food commodities has become less elastic with respect to both income and own prices over time. It is also notable that the housing demand as a whole has been substantially elastic during the entire period. More conspicuous is the fact that transportation has the largest income and own price elasticities, reflecting a strong demand for private cars in recent times.

5.3. Money Flexibilities

From all the estimated linear expenditure systems, some good results were chosen and their estimates of money flexibility ω^* were tabulated in Table 5. These estimates are liable to depend on the sample period, the level of commodity aggregation, and so on. However, they range from -2.0 to -2.5 without wide variations. Until comparatively recently, they tended to decline in absolute value. The corresponding $\hat{\lambda}$'s and $\hat{\varphi}$'s were all estimated as statistically significant values.

Subperiod	ي ۵+	Number of subgroups	Subgroups further aggregated
1951-60	-2.455	21	Cakes and fruits, clothes and personal effects, tobacco and recreation
1951-60	-2.533	22	Cakes and fruits, clothes and personal effects
1959-73	-2.401	23	Meat, milk, etc.
1959-73	-2.284	24	
1960-72	-2.547	24	
1961-70	-2.438	24	
1961-73	-2.295	23	Meat, milk, etc.
1961-73	-2.240	24	
1962-77	-1.957	21	Meat, milk, etc, repairs and water, tobacco and recreation
1963-77	-2.221	21	Meat, milk, etc, repairs and water, tobacco and recreation

Table 5. Estimated Money Flexibility by the Sample Period and by the Commodity Classification (Static Model)

 $\tilde{\omega}^* = 1/\hat{\varphi} = -\overline{m}/\hat{\lambda}$

Lastly, sample mean estimates of subsistence parameter β_i were calculated, but they are not mentioned here. The concept of subsistence consumption levels are not applicable to inferior goods in an additive utility function. It is discussed again with the economic implications of the dynamic model.

6. EMPIRICAL RESULTS OF THE DYNAMIC MODEL

6.1. Estimates of Demand Parameters

In estimation, equation (10) was used with alternative specifications of the proxy for changing tastes, as shown in equations (11) and (12). It was fitted to longer time series of per capita expenditure and price data. Several favorable results were obtained from various data sets, which are somewhat different in

terms of sample period, proxy for taste variable, and commodity aggregation. One of the good results can be seen in Table 6. It reveals recent trends in consumption patterns to some extent. The commodity classification is the same as in the third subperiod (1963-77) in Table 1.

	Margina	l budget	Coeffici	ient of	Correl	ation	Serial
Coefficient	sha	are	s _t var	iable	coeffi	cient	correlation
i		t ratio	ĉ	t ratio	R _{v',us}	R	coefficient
1 Rice	0540	22.003	0205*	.750	.983	.975	.575
2 Other cereals	.0032	4.322	0052•	.640	.752	.957	.322
3 Fish	0009	.657	.0159•	1.110	.309*	.990	.008
4-5 Meat, milk, etc.	.0672	20.618	.0278•	.766	. 98 1	.975	.804**
6 Vegetables	.0079	5.946	.0069•	.464	.822	.976	.508
7 Processed food	.0205	21.288	.0116•	1.081 -	.982	.987	.493
8 Cakes	.0151	19.858	.0085•	1.001	.979	.976	.515
9 Fruits	.0228	15.718	.0197•	1.218	.967	.958	.578
10 Beverages	.0411	29.288	.0249•	1.596	.990	.983	.522
11 F.a.f.h.	.0442	38.650	0089•	.695	.994	.995	.666**
12 Rent	.0371	26.152	0046•	.294	.988	.990	.376
13-14 Repairs]	
+ water	.0170	13.912	.0050•	.366	.959	.976	.414
15 Furniture	.0698	16.391	.0786•	1.658	.970	.947	.514
16 Fuel + light	.0469	32.171	0137•	.844	.992	.976	.393
17 Clothes	.0863	30.472	.0615•	1.951	.991	.988	.449
18 Personal effects	.0166	11.618	.0218•	1.371	.942	.946	.702**
19 Medical care	.0381	78.074	.0106•	1.957	.999	.998	.023
20 Toilet care	.0205	25.204	.0255	2.817	.987	.986	.654**
21 Transportation	.1063	23.728	0472•	.947	.985	.984	.332
22 Education	.0089	3.279	0120•	.396	.630	.886	.832**
23-24 Tobacco							
+ rec.	.3853	47.164	2061	2.267	.996	.996	.568
$\widehat{\lambda}$	96.471	3.277	(Ø = -	.4354)			

Table 6. Estimates of Demand Parameters \hat{b}_i , \hat{c}_i , $\hat{\lambda}_i$ in 1958–1977 (Dynamic Model)

Taste variable $s_t = m_t - m_{t-1}$

*insignificant at 5 percent $(\hat{b}_i, \hat{c}_i, R_{y',us})$

******significant at 5 percent (serial correlation coefficient)

Estimated marginal budget shares are all significant except for fish. All subgroups other than rice and fish are defined to be normal goods. Significance of the coefficients of the taste variable turns out to be low on the whole. It would imply that changes in the quantities demanded of many subgroups are substantially explained by income and price changes within the framework of economic theory. It is noteworthy, however, that the introduction of taste variable into the expenditure functions had a noticeable effect in stabilizing other relevant parameters in the regressions. The multiple correlation coefficients indirectly computed are very high; on the other hand, the serial correlation in the residuals is not a serious problem in this case. Measures of fit in the total test are mostly at the level of 90 percent. These two facts indicate a high predictive power of the model. Only a couple of values of this measure are rather low, i.e., for transportation in the early years of the period under consideration.

2 .018 087 .000	3 .040 007	4-5 .034	6	7	8	9	10	11	12	13-14	15	16	17	18	19	20	21	22	23-24	Е,
.018 087 .000	.040 007	.034	.027	0.15																
067 .000	007	.004		047	014	010	012	013	015	015	017	022	045	025	009	.020	001	.028	.100	-1.044
.000	007	- 006	- 005	- 009	. 003	- 002	. 002	- 002	- 003	- 003	- 003	- 001	- 008	- 005	- 002	- 004	000	- 005	- 018	192
.000	011	000	00.0	000	005	000	0002	002	003	003	000	000	.000	.000	000	000	- 000	001	.002	022
	.011	.001	.001	.001	.000	.000	.000	.000	.000	.000	.000	.000	.001	.001	.000	.000				
018	042	600	- 028	. 040	015		012	014	014	014	018	. 023	- 047	. 026	- 009	- 021	001	- 029	- 103	1.080
010	042	300	020	049	015	011	013	014	010	010	010	065	- 012	- 000	- 002	- 005	.000	- 007	. 028	270
004	010	009	124	012	-,004	003	003	003	004	004	÷.000	000	012	000	002	005	.000	001		
		~~~			005						000	000	014	000	~~~	007	000	- 010	- 036	377
006	014	012	010	181	005	004	004	005	008	008	006	000	010	009	003	007	.000	010	. 072	248
011	029	025	019	034	336	007	009	010	011	011	- 012	016	032	018	006	014	.000	020	072	1 150
018	045	038	030	052	016	516	014	015	017	017	019	025	050	027	.010	022	.001	031	111	1.100
021	053	048	038	063	~.019	014	620	018	020	020	023	030	060	033	012	027	.001	037	133	1.307
021	053	045	036	082	019	013	016	617	020	020	023	029	060	033	012	027	.001	037	132	1.370
016	046	040	031	- 055	016	012	014	016	542	018	020	026	052	029	010	023	.012	032	115	1.205
012	030	028	020	035	011	008	009	010	011	- 349	013	017	034	- 018	007	015	.001	021	074	.776
023	057	049	- 038	067	020	015	017	019	022	022	672	032	065	035	013	029	. <b>0</b> 01	-,040	142	1.486
017	043	037	029	051	015	011	013	014	016	016	019	513	049	027	010	022	.001	030	107	1.123
016	041	035	028	048	015	010	012	014	016	016	018	- 023	510	025	009	021	.001	029	102	1.065
008	021	018	014	024	007	005	008	007	008	008	009	011	023	247	005	010	.001	014	051	.538
023	058	050	039	068	021	015	018	019	022	- 022	025	032	066	036	671	029	.005	041	145	1.511
011	- 028	024	019	033	010	007	009	009	011	011	012	016	032	017	008	331	. <b>0</b> 01	- 020	070	.728
.036	090	077	061	- 106	032	023	028	030	034	034	039	- 050	102	056	020	045	-1.020	063	- 225	2.347
004	011	010	008	013	004	003	- 003	004	004	004	005	006	013	007	003	006	.000	134	028	.290
022	056	048	038	066	020	014	017	019	021	021	024	031	064	035	013	028	.015	- 039	779	1.463
.017	.038	.062	.029	0.54	.020	.020	030	.032	.031	022	.047	.042	.081	.031	.025	.028	.045	.031	.263	
	016 004 004 011 018 021 016 012 016 012 017 016 023 017 016 023 011 036 004 022 004	016042 004010 006014 011029 018045 021053 021053 018048 012030 023057 017043 016041 023058 011028 011028 036090 004011 022056 017038	018        042        508          004        010        009          006        014        012          011        029        025          018        045        038          021        053        046          021        053        046          021        053        046          021        053        046          012        030        026          023        057        049          017        043        037          018        041        035          008        021        018          023        058        050          011        028        024          036        090        077          004        011        010          022        056        048           .017         .038         .062	016        042        508        028          004        010        009        124          006        014        012        010          011        029        025        019          018        045        038        036          021        053        046        038          021        053        045        036          011        023        045        038          021        053        046        031          012        030        028        020          012        030        028        020          023        057        049        038          017        043        037        029          016        041        035        028          008        021        018        014          023        058        050        039          011        028        024        019          036        090        077        061          004	016        042        506        028        049          004        010        009        124        012          006        014        012        010        181          011        029        025        019        034          018        045        038        030        052          021        053        046        036        063          021        053        045        036        062          016        048        040        031        055          012        030        028        020        035          023        057        049        038        067          017        043        037        029        051          016        041        035        028        048          008        021        018        014        024          023        058        050        039        068          011        028        024        019        033          036	016        042        508        028        049        015          004        010        009        124        012        004          006        014        012        010        181        005          011        029        025        019        034        336          018        045        038        030        052        019          021        053        046        036        063        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Table 7. Demand Elasticities Estimated for Twenty-one Subgroups at the Sample Means of all Variables in 1958–1977  $[\overline{e}_i,\overline{E}_i]$  and Sample Mean Average Budget Shares  $[\overline{w}_j]$ 

 $\overline{e}_{ij}$  = elasticity of subgroup i with respect to the j-th price calculated at sample

 $\frac{means}{\overline{E}_i} = \text{bidstelly of subgroup i calculated at sample means}$  $\overline{\overline{W}_j} = \text{bidget share of subgroup j calculated at sample means}$ 

. 13 .

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#### 6.2. Demand Elasticities

Elasticities of demand with respect to deflated income and prices are given in Table 7, evaluated at the sample means in the past 20 years. At first sight, Table 7 closely resembles Table 4 in the static model. There are only slight differences in income elasticities between the two tables. Education is now apparently a normal good. As regards the food category, beverages, food away from home, fruits, and meat are elastic with respect to income. In the nonfood category, transportation, medical care, furniture and recreation have very high income elasticities.

Own price elasticities in Table 7 are similar to those in Table 4. This implies that the money flexibility estimated by the dynamic model in 1958-77 is close to that of the static model in 1963-77. Estimated money flexibilities vary rather widely in the dynamic model, depending mainly on the length of sample period in this analysis. Nevertheless, most of those estimates fell in the interval between -1 and -4.

## 6.3. Cost of Living Index and Subsistence Cost

There are three exceptional subgroups in estimating the cost of living index and the subsistence cost. They are rice, fish, and transportation. The first two subgroups have negative marginal budget shares, and the last one has a negative subsistence parameter. In disregard of their peculiarities, an attempt is made to estimate the cost of living index and the subsistence cost. In fact, these three subgroups possess only small shares of the total budget. The calculation of the cost of living index follows the formula (see Hoa 1969a, 1969b, and Theil 1980).

$$C_{ot} = (1+\varphi) \left( \sum_{i} p_{it} \beta_{it} / \sum_{i} p_{io} \beta_{it} \right) - \varphi \prod_{i} (p_{it} / p_{io})^{b_{i}}$$
(20)

where  $p_{it}$  and  $p_{io}$  denote the <u>i</u>th price in the comparison and base periods respectively. The  $\hat{\beta}_{it}$  can be obtained by equation (13) after the estimates  $\hat{b}_i$ ,  $\hat{c}_i$ , and  $\hat{\lambda}$  have been determined.

If the values of the cost of living index were all equal to 100, the General Consumer Price Index and the 'true' cost of living index would be the same. Though the values of the index in Table 8 are very close to 100, many of them do not attain this level. It would follow from the fact that the General Consumer Price Index in the Laspeyres form tends to have an upward bias as a deflator.

Year	Cost of living index	Subsistence cost	Year	Cost of living index	Subsistence cost
1958	100.0	122,120	1968	98.8	124,148
1 <b>9</b> 59	100.4	122,251	1969	99.1	125,288
1960	100.3	122,080	1970	99.1	125,832
1961	100.0	122,15 <b>9</b>	1971	99.5	126,261
1962	99.5	122,187	1972	99.5	126,586
1963	99.1	122,520	1973	99.3	128,037
1 <b>96</b> 4	99.2	122,826	1974	99.3	128,031
1 <b>96</b> 5	98.3	123,014	1975	99.5	129,726
1966	98.6	122,689	1976	100.0	131,402
1967	98.7	123,437	1977	100.2	131,455

Table 8. Estimates of Cost of Living Index and Subsistence Cost by Year

Cost of living index in 1958 = 100.0 Subsistence cost =  $\Sigma_i p_{it} \hat{\beta}_{it}$  Estimated subsistence cost, as shown in Table 8, changes quite slowly over time. It results from the weak influence of the taste variable.

## 7. CONCLUDING REMARKS

It was intended in this paper to systematically analyze the consumer demand at subgroup levels on the basis of family budget data in 1951-77. All the commodities were classified into 21 to 24 subgroups in estimating the linear expenditure system. Powell's system was applied to the annual data in various segments of the whole period, estimating both static and dynamic parameters of the expenditure system.

The static model yielded well-defined demand relations and their characteristics in various subperiods, particularly in the three subperiods 1951-60, 1961-70, and 1963-77. Such a static approximation was attempted to preserve the linearity of expenditure functions and to take account of the possible changes in preferences during the whole period. Evidently from the empirical results, price and income elasticities of demand have changed over time, and the values of money flexibility show a little variation in dependence on sample period, commodity classification and so on.

In the dynamic model, many of the estimated parameters for the taste variable were not statistically significant, but some important demand and utility parameters were obtained. Estimates of money flexibility were fairly changeable according to the income level, specification of the taste variable and so on. They were more or less different from those of the static model. Price elasticities in the dynamic model are also at variance with the static results. The striking features of the results are that the measures of fit of the model were very high in interpolation test, and that the estimated parameters were rather stable as a whole.

Consumer demand estimation in more recent years will be discussed on another occasion.

#### NOTES

1. Let the cross substitution term in the Slutsky equation be  $K_{ij}$ . Then the symmetry condition is

 $K_{ij} = \lambda(\partial x_i / \partial m) (\partial x_j / \partial m), (i \neq j), (\lambda: \text{ constant})$ 

2. The  $\lambda$  is related to Theil's income flexibility  $\varphi$  and to Frisch's money flexibility  $\check{\omega}$  as follows:

 $(\lambda / m) = -\varphi = -(1 / \tilde{\omega}), (m: income)$ 

Frisch's money flexibility  $\tilde{\omega}$  is equivalent to the income elasticity of the marginal utility of income. Since the supernumerary ratio is defined as (see Goldberger 1970):

 $-\varphi = (m - \sum_{i} p_i \beta_i) / m$ 

 $\boldsymbol{\lambda}$  is interpreted as the supernumerary income in the linear expenditure system.

3. Denote the substitution term by  $K_{ij}$ . Then  $z_{it}$  is of the form:

 $z_{it} = (p_{it} / \lambda) \sum_{j} K_{ij} (p_{jt} / \overline{p}_{j})$ 

- 4. The maximum likelihood method entails a greater burden of computation as compared with the least squares method. As regards the convergence of demand parameters in nonlinear regressions, the maximum likelihood method appears to involve some difficulty. Lluch and Powell (1975) and Lluch and Williams (1975) reported the results that maximum likelihood estimates did not converge in some cases, but that convergence was achieved in those cases by the least squares method in the estimation of the linear expenditure system and of the extended linear expenditure system, respectively.
- 5. Assume that X and y are the matrix and vector whose elements consist of sample data on exogenous variables. Furthermore, if we assume in regard to the error structure that there is no serial correlation either within or across equations, and that there is no contemporaneous correlation across equations but a common error variance for all equations, maximum likelihood method reduces to least squares method (see Goldgberger and Gamaletsos 1970, Lluch and Williams 1975). The error structure in this case is of the form

$$E(\varepsilon_{it}) = 0$$
  
$$E(\varepsilon_{it}\varepsilon_{jt}') = \begin{cases} \sigma^2 \ (i = j \text{ and } t = t'), \\ 0 \text{ otherwise} \end{cases}$$

However, this error specification is practically implausible, as was pointed out by Goldberger and Gamaletsos (1970).

6. The simple assumption is that there is no serial correlation either within or across equations and that there is no contemporaneous correlation across equations but a constant error variance for each equation. The error specification in this case is of the form

$$E(\varepsilon_{it}) = 0$$
  

$$E(\varepsilon_{it}\varepsilon_{jt}') = \begin{cases} \sigma_{i}^{2} \ (i = j \text{ and } t = t'), \\ 0 \text{ otherwise} \end{cases}$$

7. The variances of the estimators  $\widehat{b}_i$  and  $\lambda$  under least squares postulates are mentioned below:

$$\sigma_{b_i}^2 = \sigma_i^2 / \sum_t u_t^2, (i = 1, 2, ..., N)$$
  
$$\sigma_{\lambda}^2 = (\sum_i D_i \cdot \sigma_i^2) \cdot \sum_t u_t^2 / (\sum_i D_i)^2$$

 $\sigma_i^2$  indicates the error variance in the estimating equation for the  $\underline{i}^{th}$  commodity, and its unbiased estimator ordinarily takes the expression

$$\hat{\sigma}_i^2 = \sum e_{it}^2 / (T-2)$$

with  $e_{it}$  being the residual and (T-2) the degree of freedom.

- 8. For the theoretical features of Leser's system, see Sasaki and Saegusa 1974.
- 9. The criterion of convergence is written as below, denoting the estimate  $\hat{\lambda}$  in round r by  $\hat{\lambda}_r$ (r = 1,2,...):

$$|(\widehat{\lambda}_{r-1}) - \widehat{\lambda}_r) / \widehat{\lambda}_r| < 10^{-4}$$

10.

$$N_{i} = \begin{vmatrix} \sum_{t} z_{it} y_{it} & \sum_{t} z_{it} u_{t} & \sum_{t} z_{it} s_{t} \\ \sum_{t} u_{t} y_{it} & \sum_{t} (u_{t})^{2} & \sum_{t} u_{t} s_{t} \\ \sum_{t} s_{t} y_{it} & \sum_{t} s_{t} u_{t} & \sum_{t} (s_{t})^{2} \end{vmatrix}$$
$$D_{i} = \begin{vmatrix} \sum_{t} (z_{it})^{2} & \sum_{t} z_{it} u_{t} & \sum_{t} z_{it} s_{t} \\ \sum_{t} u_{t} z_{it} & \sum_{t} (u_{t})^{2} & \sum_{t} u_{t} s_{t} \end{vmatrix}$$

$$D_{i} = \begin{bmatrix} \sum_{t} u_{t} z_{it} & \sum_{t} (u_{t})^{2} & \sum_{t} u_{t} s_{t} \\ \sum_{t} s_{t} z_{it} & \sum_{t} s_{t} u_{t} & \sum_{t} (s_{t})^{2} \end{bmatrix}$$

$$y_{it}' = b_i u_t + c_i s_t + \varepsilon_{it}$$

The variances of estimators  $\widehat{b_i},\, \widehat{c_i} \text{ and } \widehat{\lambda}$  are

$$\sigma_{b_i}^2 = \sigma_i^2 \cdot r_{11}$$
$$\sigma_{\widehat{c}_i}^2 = \sigma_i^2 \cdot r_{22}$$

$$\sigma_{\lambda}^{2} = \sum_{i} \sigma_{i}^{2} D_{i} \{ (\sum_{t} u_{t}^{2}) (\sum_{t} s_{t})^{2} - (\sum_{t} u_{t} s_{t})^{2} \} / (\sum_{i} D_{i})^{2}$$

 $\sigma_i^2$  is the error variance of the <u>i</u>th equation, and its unbiased estimator is  $\partial_i^2 = \sum e_i^2 / (T - 3)$ , (e_i: residual)

 $r_{ii}$  (i = 1,2) indicates a diagonal element in the inverse matrix:

$$\begin{bmatrix} \sum_{t} u_{t}^{2} & \sum_{t} u_{t} s_{t} \\ \sum_{t} s_{t} u_{t} & \sum_{t} s_{t}^{2} \end{bmatrix}^{-1} \equiv \begin{bmatrix} r_{11} & r_{21} \\ r_{12} & r_{22} \end{bmatrix}$$

In this paper, the sample size is not reduced by taking differences in annual income for the specification of the taste variable.

- 11. For details on data, see Sasaki (1981).
- 12. The static model of Leser's system is expressed as

$$\mathbf{v}_{i} = \mathbf{p}_{i}\overline{\mathbf{x}}_{i} + \overline{\alpha}(\overline{\mathbf{w}}_{i} \sum_{j} \mathbf{p}_{j}\overline{\mathbf{x}}_{j} - \mathbf{p}_{i}\overline{\mathbf{x}}_{i}) + \mathbf{b}_{i}(\mathbf{m} - \sum_{j} \mathbf{p}_{j}\overline{\mathbf{x}}_{j})$$

It does not require an iterative estimation. The taste variable  $\mathbf{s}_t$  is added to the above equation to extend it to a dynamic model in this analysis.

- 13. The multiple correlation coefficient R was computed as the simple correlation coefficient between actual and estimated expenditures for each subgroup.
- 14. The measure of fit in the total test is the ratio of calculated expenditure  $\hat{v}_{it}$  to actual expenditure  $v_{it}$ . This is equivalent to taking the ratio of calculated quantity consumed per capita  $\hat{x}_{it}$  to its actual value  $x_{it}$ .

Measure of fit =  $(\hat{v}_{it} / v_{it}) = (\hat{x}_{it} / x_{it})$ 

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