

Ecological Bistability and Evolutionary Reversals under Asymmetrical Competition

Dercole, F., Ferriere, R. and Rinaldi, S.

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International Institute for
Applied Systems Analysis
Schlossplatz 1
A-2361 Laxenburg, Austria

Tel: +43 2236 807 342
Fax: +43 2236 71313
E-mail: publications@iiasa.ac.at
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Ecological Bistability and Evolutionary Reversals under Asymmetrical Competition

Fabio Dercole (dercole@elet.polimi.it)

Régis Ferrière (regis.ferriere@snv.jussieu.fr)

Sergio Rinaldi (rinaldi@elet.polimi.it)

Approved by

Ulf Dieckmann (dieckman@iiasa.ac.at)

Project Leader, Adaptive Dynamics Network

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Abstract

How does the process of life-history evolution interplay with population dynamics? Almost all models that have addressed this question assume that any combination of phenotypic traits uniquely determine the ecological population state. Here we show that if multiple ecological equilibria can exist, the evolution of a trait that relates to competitive performance can undergo adaptive reversals that drive cyclic alternation between population equilibria. The occurrence of evolutionary reversals requires neither environmentally-driven changes in selective forces, nor the co-evolution of interactions with other species. The mechanism inducing evolutionary reversals is two-fold. First, there exist phenotypes near which mutants can invade and yet fail to become fixed; although these mutants are eventually eliminated, their transitory growth causes the resident population to switch to an alternative ecological equilibrium. Second, asymmetrical competition causes the direction of selection to revert between high and low density. When ecological conditions for evolutionary reversals are not satisfied, the population evolves toward a steady state of either low or high abundance, depending on the degree of competitive asymmetry and environmental parameters. A sharp evolutionary transition between evolutionary stasis and evolutionary reversals and cycling can occur in response to a smooth change in ecological parameters, and this may have implications for our understanding of size-abundance patterns.

About the Authors

Fabio Dercole
CIRITA, Politecnico di Milano
Via Ponzio 34/5, 20133 Milano, Italy

Régis Ferrière
Mathematical Eco-Evolutionary Theory (MEET) Group
Laboratoire d'Ecologie, Ecole Normale Supérieure
46 rue d'Ulm, 75230 Paris cedex 05, France
and
Adaptive Dynamics Network
International Institute for Applied Systems Analysis
A-2361 Laxenburg, Austria

Sergio Rinaldi
CIRITA, Politecnico di Milano
Via Ponzio 34/5, 20133 Milano, Italy

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Fabio Dercole
Régis Ferrière
Sergio Rinaldi

The contrasting patterns of evolution in populations with chronically high or low densities have captured the shared interests of ecologists and geneticists for a long time (Travis, 1990). There has been a considerable amount of verbal and mathematical theory on the subject (reviewed lucidly by Mueller (1997)). In this context, the integrative notion of an eco-evolutionary feedback emphasizes that selective pressures exerted on individuals are shaped by population structure and abundance; in return, population dynamics are primarily determined by individual phenotypic traits that are genetically-based and molded by natural selection (Pimentel, 1968; Heino et al., 1998).

Density-dependent selection is the central theme underlying one arch of the eco-evolutionary feedback—from ecology to evolution. Over the last two decades, there has been intensive empirical investigation of the effect of population density on the nature, direction and strength of selection on life-history traits. Exemplary studies include those by Wilbur (1984) and Travis et al. (1985) on larval anurans, who showed that the role of predatory salamanders as a selective force for rapid growth of tadpoles varies depending on tadpole density: at very low densities this force is weak because growth rates are high and encounter rates with predators are low; greater numerical impact of predators occur only at higher tadpole densities; yet at extremely high densities all tadpoles grow so slowly, due to effective food limitation, that they can be driven extinct. The net result is that effective selection on growth rate will occur only within certain regions of the parameter space, depending upon the corresponding population density.

Although much empirical effort has been devoted to understand how crowding influences patterns of selection on life-history traits, the backward effect of selection on population dynamics—the other arch of the eco-evolutionary feedback—remains poorly understood, even theoretically (Metz et al., 1992; Rand et al., 1994; Heino et al., 1998). One important feature of density-dependent models of population dynamics is their propensity to generate complex dynamics, including periodic and chaotic oscillations. Much attention has been paid to the question of whether natural selection could drive individual traits from values leading to stable equilibria, to values corresponding to cycles or chaos (Gatto, 1993; Ferrière and Gatto, 1993, 1995; Doebeli and Koella, 1995; Ferrière and Fox, 1995; Ebenman et al., 1996); contrasting theoretical predictions are awaiting to be tested empirically. A crucial assumption in all models developed around this issue is that any combination of traits uniquely determines the population state (De Feo and Ferrière, 2000). However, ecological models can have alternative equilibria (see Scheffer et al., 2001, for a survey), associated with different equilibrium densities, that can be reached for the very same individual trait values. The question of how the eco-evolutionary feedback works in these cases is basically untouched and provides the motivation for this work.

We consider a very simple population model that can have a high and a low density equilibrium. At the former, there is selection for a trait that reduces population density, but at the latter there is selection for a trait that increases population density. Under some conditions that we identify by means of the adaptive dynamics approach (Metz et al., 1992; Geritz et al., 1997), these opposing patterns of selection result in periodic evolutionary reversals. Our analysis also predicts the influence of a set of environmental parameters on the outcome, and investigates the full interplay of population density and selective pressures that result from the eco-evolutionary feedback. A salient result of our study is that there are broad ecological conditions under which the direction of natural selection periodically reverts in conjunction with switches between ecological equilibria.

1 Biological background

We consider a single species whose population dynamics are determined by a set of fixed ecological parameters, and by life-history parameters that are functions of a phenotypic trait. This trait is assumed to be genetically determined and heritable, but it may vary among individuals due to mutations of small effects. Selection acts upon this variation, with changes in population dynamics as a potential by-product. We assume that for suitable environmental parameters there can be values of the trait for which the population possesses alternative stable equilibria.

Ecological bistability was first put forward by Holling (1973), Noy-Meir (1975), and May (1977). Subsequently, alternative low- and high- density states have been found in a host of ecological models. Although the first experimental examples that were proposed were criticized strongly (Connell and Sousa, 1983), more recent studies (reviewed in Scheffer et al. (2001)) support the view that multiple stable states can characterize natural systems.

Here we assume a simple phenomenological model to generate alternative stable equilibria, akin to the minimal models proposed by Scheffer et al. (2001). As explained below, one possible interpretation of this model is that the species under consideration is harvested by a generalist predator, which exploits a spectrum of other prey species. This assumption ensures that potential variations in selective pressures derive exclusively from intraspecific interactions.

We also assume that the phenotypic trait is related to competitive performance, and we call it, for this reason, ‘competitive ability’. Thus, variation in individual trait results in asymmetrical competition between phenotypes. Moreover, individuals that are at competitive advantage are none-the-less expected to suffer some physiological cost: this is why competitive ability is assumed to be costly to some components of reproductive success. A common case involving asymmetrical competition and physiological costs of higher energy demands occurs when competing individuals differ in size. Often, larger individuals enjoy a competitive advantage because of their superior ability at obtaining limited resources (Brooks and Dodson, 1965; Wilson, 1975; Persson, 1985; Calder III, 1996), but the opposite can also be true, like in the case of small zooplanktivorous fish outcompeting large ones for food (Persson et al., 1998). However, this dichotomy does not influence our findings, since the only assumption that counts in this theory is that a positive variation of the trait is accompanied by an advantage in competition (or growth) and by a counterbalancing disadvantage in growth (or competition).

The body size interpretation of competitive ability may be useful because the relationship between body size and population abundance arguably has attracted great attention. Yet the search for general patterns has not been conclusive (Lawton, 1989; Blackburn and Lawton, 1994; Rosenzweig, 1995). Data from extant populations show that low abundance, under some circumstances, is associated with large body size (Brown, 1995; Gaston and Kunin, 1997), but the pattern is far from general. For example, Navarette and Menge (1997) found no tendency for small species to occur at higher densities than larger species in the tropical intertidal communities of Panama,

in sharp contrast with the pattern in intertidal communities in temperate Chile (Marquet et al., 1990). Thus, although direct measures of competitive performance are difficult to obtain from real systems, there is hope that our theoretical predictions could be tested against the results of experimental studies (like those reported by Lenski and Bennett (1993) for bacteria) on the evolution of body size.

2 Mathematical analysis

2.1 The ecological model

We describe the ecological dynamics of the population of a single competition phenotype u by making use of the following simple model:

$$\dot{x} = G(x, u) x - H(x) \quad (1)$$

where x denotes population density. The function G measures the logistic component of population growth; it is given by: $G(x, u) = r(u) - ax$, where $r(u)$ is the per capita intrinsic growth rate which is assumed to decrease with competitive ability u to express the cost of enhanced competitive performance and ax measures the extra mortality caused by intraspecific competition. Competitive ability u scales between 0 and 1. This scaling is achieved by means of the transformation $u = \log(l/l_{\min}) / \log(l_{\max}/l_{\min})$, where l is the ‘real’ trait value, and l_{\min} and l_{\max} are minimum and maximum trait values, respectively (Schwinning and Fox, 1995).

Bistability is triggered by combining the negative density-dependence of logistic growth with the positive density-dependence of an additional demographic factor. Two important examples of such a factor are: the reduction of reproduction due to a shortage of mating encounters in sparse population; and the reduction of mortality due to the dilution of predation risk as density increases (Dennis (1989) and references therein; Stephens and Sutherland (1999)). Both examples can be accounted for by the same model, namely a discount term $H(x) = xc/(x+d)$ in equation (1) (hereafter H will be referred to as ‘discounting function’). This form of H reflects a negative exponential distribution of mating encounters (Dennis, 1989), or a Holling type-II functional response of the predator (May, 1977; Huberman, 1978; Brauer, 1979). The resulting population model leads, under suitable conditions on parameters, to the coexistence of two stable equilibria: the trivial equilibrium of extinction, and a positive equilibrium.

In this paper we investigate a more general scenario of ecological bistability involving the coexistence of two non-trivial stable equilibria. This is obtained simply by altering the discounting function H into $H(x) = xcx/(x^2 + d^2)$ which provides a simple way of accounting for spatial heterogeneity in predation risk or the chance of mating. With this choice of H , model (1) predicts the existence of a lower threshold on competitive ability, u_l , below which the population assumes a single stable equilibrium at high density; and an upper threshold, u_h , above which the population possesses a single stable equilibrium at low density (Appendix). For u values lying between u_l and u_h , there are two alternative stable equilibria, one corresponding to a state of high abundance (denoted by \bar{x}) and the other to a state of low abundance (\underline{x}), see Figure 1.

It is also worth noticing that if body size is a measure of competitive ability, and the discounting function H is predation rate, it would be more realistic to assume that H in (1) depends also upon u since prey body size usually influences the functional response of the predator. However, this would give rise to an analytically intractable problem even if the final result would be qualitatively the same. For this reason we have assumed that H is independent on u . In any case, model (1) applies when competitive ability does not influence predation or when body size has only a weak influence on the predator functional response.

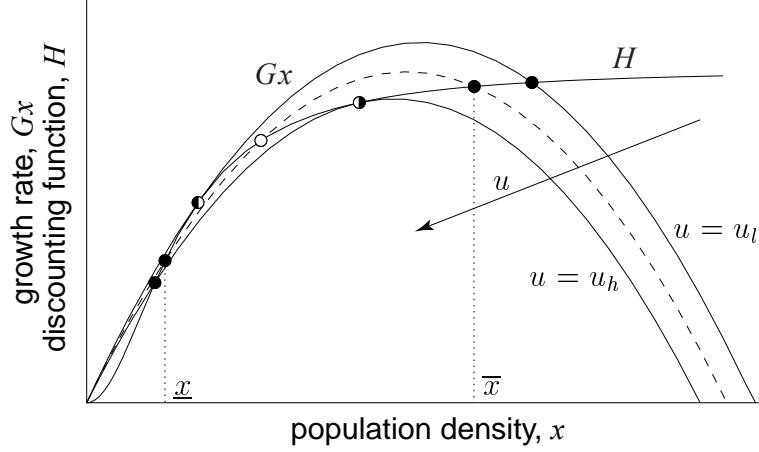


Figure 1: Multiple ecological equilibria. Population equilibria are given by the intersection of the population growth function Gx (which depends on phenotypic trait u) and the discounting function H . For u between the lower threshold u_l and the upper threshold u_h (see dashed line), the population has three ecological equilibria: two stable equilibria (filled circles), one at low population density \underline{x} and the other at high population density \bar{x} ; and one unstable equilibrium (open circle). For the two critical values of u , namely u_l and u_h , there is a collision of a stable equilibrium with an unstable equilibrium (see half-filled circles).

2.2 Analysis of mutant-resident model

Having this ecological model in place, we describe the evolutionary dynamics of the individual trait u that we regard as adaptive. Adaptive evolution is assumed to proceed by discrete steps involving small random mutations, and selection (Metz et al., 1992; Geritz et al., 1997). Mutations are assumed to be sufficiently rare so that two conditions are fulfilled: (i) at the time a mutant phenotype arises, the resident population of the wild type is at ecological equilibrium, and (ii) the wild type population is challenged by one mutant phenotype at a time. Once the mutant has entered the population, it may simply go extinct, or invade and go to fixation by replacing (or coexisting with) the resident type, thereby setting the new wild environment against which the next mutant will have to strive. These two conditions amount to separating out the ecological and evolutionary timescales; they allow us to describe the evolutionary dynamics of the adaptive trait u as a random walk, each step of which being taken according to the outcome of competition between a resident population and a mutant population (Champagnat et al., 2001).

The dynamics of interacting resident and mutant populations characterized by traits u and u' , respectively, are governed by the following system

$$\begin{aligned}\dot{x} &= g(x, x', u, u')x - h(x, x') \\ \dot{x}' &= g(x', x, u', u)x' - h(x', x)\end{aligned}\tag{2}$$

We assume that there is no discrimination between resident and mutant populations with regard to discounting (e. g. no discrimination by a predator), so that the function h is given by

$$h(x, x') = x \frac{c(x + x')}{(x + x')^2 + d^2}\tag{3}$$

By contrast, the per capita growth function g must incorporate the effect of asymmetrical competition between two phenotypes. This is achieved by setting

$$g(x, x', u, u') = r(u) - ax - b(u, u')x'\tag{4}$$

The competition coefficient b is taken to depend only on the difference between phenotypic values u' and u and is equal to a for $u' = u$. It should increase as the difference $u' - u$ increases, expressing a stronger deleterious effect on the u -population growth of larger u' -competitors. The slope of this function as $u' - u$ goes to zero provides a measure of the strength of the asymmetry, and is denoted by β in the following, i. e.

$$\beta = \left. \frac{db}{d(u' - u)} \right|_{u'=u}$$

All possible outcomes of resident-mutant competition can be classified by means of a detailed analysis of system (2-4) in the trait space (u, u') . In principle, this analysis could be carried out through extensive simulation of system (2-4) for various values of u and u' . However, in practice, the simulation approach is rather critical. This is why a much more effective method, called bifurcation analysis (Kuznetsov, 1998), has been used in this paper. The assumption that mutations have small effects makes it legitimate to restrict the analysis to the vicinity of the diagonal line $u = u'$, that is, to the region of the trait space where the mutant phenotype differs only slightly from the resident. The result is shown in Figure 2, which unravels seven regions corresponding to seven qualitatively different behaviors of the dynamical system (2-4). In region I, the resident population possesses only one stable equilibrium, namely the high-density equilibrium \bar{x} . Small mutations characterized by slightly larger phenotype invade and replace the resident type (side panel I). The evolutionary random walk takes on a small step toward larger phenotype, and this results in a slight decrease of the equilibrium population density (see Fig. 1). The same outcome is observed in all regions II-V (side panels II-V). In all of these regions, a mutant with a slightly larger phenotype can invade and eliminate the resident type. Thus, starting from any ancestral state of high abundance for which u is less than u_h , adaptive evolution proceeds through the gradual increase of the phenotype, causing the concurrent, slow decrease of population density.

A new phenomenon is observed in region VI, where the resident trait is still slightly less than u_h while the mutant trait is now slightly greater than u_h . In this case, the mutant first invades, but the resident ‘strikes back’ (side panel VI): after its initial increase, the mutant reaches a peak density, then it starts declining and eventually goes extinct. This unexpected dynamical pattern arises from the existence, for the resident population, of two alternative equilibria which differ in their vulnerability to invasion by the mutant. Initially the resident population stands on its high-density equilibrium, which appears to be invulnerable. As the mutant population grows, the resident population cannot sustain its high density any longer and starts to approach its low-density state. While doing so, it creates a competitive environment that becomes non-invulnerable by the mutant. Now the latter is doomed, and as it goes extinct the population is sent back to its original phenotypic state; but in the mean time the ecological state has changed: the resident population experienced a sudden transition from the state of high abundance to the state of low abundance.

The same picture holds for the dual case, starting from an ancestral state of low abundance and intermediate or large phenotype (u larger than u_l). Here the adaptive process drives the slow decrease of the trait and the concomitant slight increase of population density. When the phenotypic state comes close to the low threshold u_l , any invasion attempt by mutants smaller than u_l triggers the ecological switch of the resident population from \underline{x} to \bar{x} . Altogether this analysis shows that the evolutionary dynamics of the population remains monomorphic and never comes to a halt. The phenotypic state of the population oscillates between a minimum (u_l) and a maximum (u_h) trait value. The ecological state of the population switches between low and high densities every time the adaptive process reaches either of these threshold phenotypes.

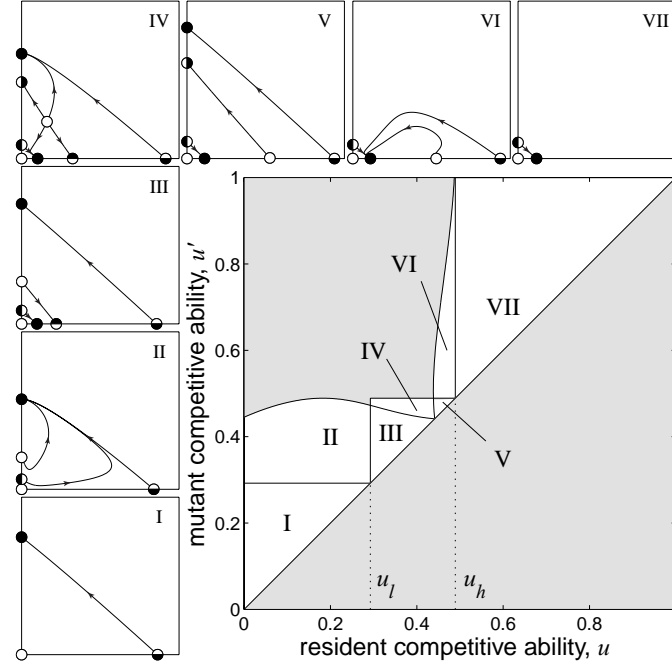


Figure 2: Bifurcation diagram of the resident-mutant model (2-4) in the resident-mutant trait space (u, u') . The bifurcation diagram (main panel) is symmetrical with respect to the diagonal line; only its upper part is shown. Mutant trait values must be close to resident trait values (under the assumption of small mutational effects), therefore the bifurcation analysis is restricted to the neighborhood of the diagonal. Seven regions (I-VII) correspond to qualitatively different behaviors for the resident-mutant system. A side panel that describes the population dynamics in the state space (x, x') is attached to each region. In these panels, filled circles indicate stable equilibria, open circles: unstable equilibria, half-filled circles: saddle points. Resident-mutant trait values in side panels: $(0.1, 0.2)$ in panel I, $(0.2, 0.4)$ in II, $(0.35, 0.4)$ in III, $(0.4, 0.48)$ in IV, $(0.46, 0.48)$ in V, $(0.46, 0.6)$ in VI, $(0.6, 0.7)$ in VII. Other parameters: $a = 0.1$, $\beta = 0.33$, $c = 1.0$, $d = 0.75$, $r_0 = 1.0$, $\gamma = 1.0$ (see Appendix for a full specification of the model).

2.3 Adaptive dynamics model

One can achieve similar conclusions by using an adaptive dynamics model which provides a deterministic approximation of the mutation-selection random walk process described above (Dieckmann and Law, 1996). The adaptive dynamics model reads:

$$\begin{aligned}\dot{x} &= G(x, u) x - H(x) \\ \dot{u} &= k x s(u, x)\end{aligned}\tag{5}$$

This model gives the rate of change \dot{u} of the adaptive trait u as a function of population density x and of the selection gradient denoted by $s(u, x)$, scaled by a constant rate of evolutionary innovation, k . The selection gradient is defined as the slope of the fitness landscape in the vicinity of the resident phenotype, and is therefore given by

$$s(u, x) = \frac{\partial}{\partial u'} g(x', x, u', u)|_{u'=u, x'=0}\tag{6}$$

The dynamics governed by system (5) involve a fast component, that of population dynamics governed by the first equation; and a slow component, that of adaptive dynamics described by the second equation. The analysis of such a slow-fast system can be performed through a method popularized in ecology by May (1977) (see also Rinaldi and Scheffer (2000) for a recent survey and Matsuda and Abrams (1994b) and Khibnik and Kondrashov (1997) for applications in the context of eco-evolutionary dynamics). The analysis requires two steps. First, the two stable equilibria $\bar{x}(u)$ and $\underline{x}(u)$ of the fast component are determined for each frozen value of the slow variable u . This yields the thin curves shown in the first row of Figure 3. Then the sign of \dot{u} at each point $(u, \bar{x}(u))$ and $(u, \underline{x}(u))$ is determined so as to predict the direction of phenotypic change. This amounts merely to finding the isocline $s(u, x) = 0$ in the space (u, x) . Figure 3 displays the three possible outcomes. In Figure 3A, starting from point 0, we observe a first, fast population transient ($0 \rightarrow 1$), followed by a slow evolutionary transient ($1 \rightarrow 2$), entraining a slow ecological change yet leaving the population with low abundance. At point 2, a fast transient of ecological change abruptly brings the population to high abundance ($2 \rightarrow 3$), and from point 3 a final slow evolutionary transient takes place, driving the population toward an eco-evolutionary equilibrium at point 4 where the phenotype is associated with high population density. At this point, selection may turn disruptive, causing evolutionary branching and the further evolution of polymorphism (Kisdi, 1999), but the investigation of this phenomenon lies outside the scope of the present article. Figure 3B shows a similar pattern whereby the evolutionary process drives the population toward a state of permanent low abundance and promotes large phenotypes.

In contrast, the eco-evolutionary process never comes to a halt in the case shown in Figure 3C. Here, after a first, fast ecological transient ($0 \rightarrow 1$), and a slow evolutionary transient ($1 \rightarrow 5$), the system is trapped forever on a slow-fast limit cycle ($5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5$). One can see by comparing Figures 3A, B, and C that the necessary and sufficient condition for the existence of such periodic evolutionary reversals is that the selection isocline $s(u, x) = 0$ (boundary of grey regions in Fig. 3) separates the two stable branches of equilibria of the population. This is a general condition for the existence of slow-fast limit cycles, known as separation principle (Muratori and Rinaldi, 1991).

3 Biological implications

3.1 Predicting the occurrence of evolutionary reversals

The occurrence of evolutionary reversals and adaptively-driven population cycles depends on four ecological parameters: the intraspecific competition coefficient, a , the strength of intraspecific

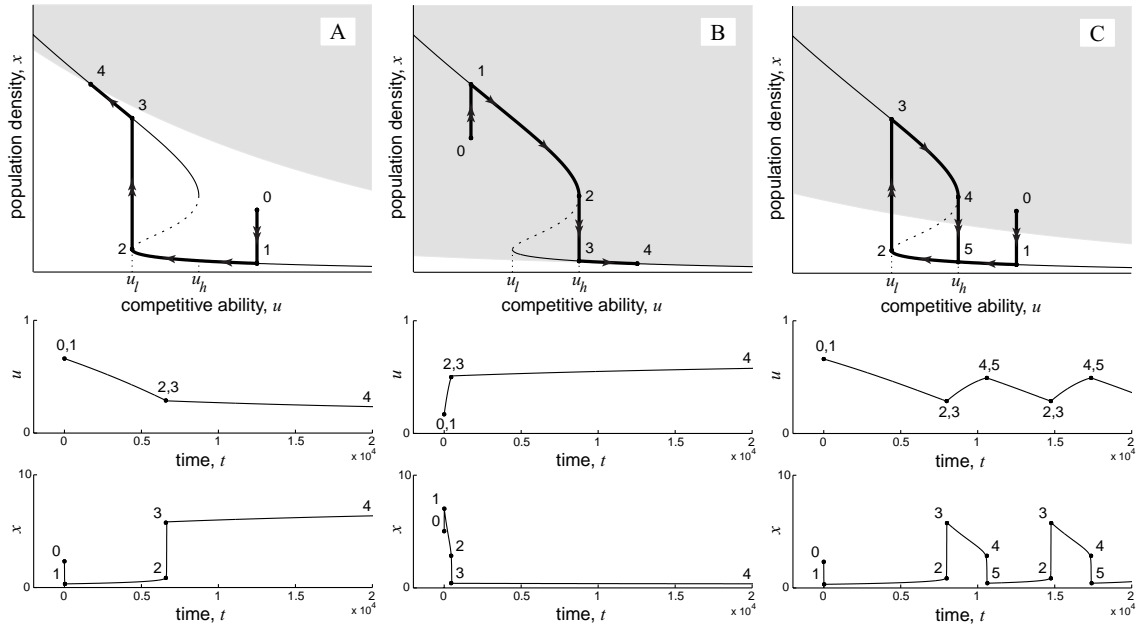


Figure 3: Eco-evolutionary dynamics in the space of trait u and population density x (first row) and corresponding time evolution of u and x (second and third rows). In the first row, thin curves indicate the set of equilibrium population density as a function of the trait value u (plain portions: stable equilibria, dotted portions: unstable equilibria); shaded region: positive selection gradient ($s(u, x) > 0$); thick curve: exemplary trajectory (single arrows: slow dynamics, double arrows: fast dynamics). **A**, Evolution toward small trait and permanent high abundance ($\beta = 0.12$). **B**, Evolution toward large trait and permanent low abundance ($\beta = 1.6$). **C**, Periodic evolutionary reversals and adaptively-driven population cycle ($\beta = 0.33$). Other parameter values as in Figure 2, and $k = 10^{-4}$.

competition asymmetry, β , and the discount parameters, c and d . Notice that in the case where discounting is due to predation, c and d measure the predation rate and the predator half-saturation constant, respectively. Evolutionary reversals can develop only when the population possesses two alternative ecological equilibria, which imposes the condition $a < c/8d^2$ (Appendix and Fig. 4A). Thus, ecological bistability requires that the competition coefficient be lower than a threshold set by the parameters of the discounting function; this constraint becomes weaker as the discounting pressure increases (larger c and/or smaller d).

In ecologically bistable populations, the occurrence of periodic evolutionary reversals is determined by the strength of competitive asymmetry, which has to lie within a range of intermediate values such that selective pressures on the adaptive trait revert at low and high abundance (Appendix). Figures 4A and B show that this range shrinks under harsher conditions expressed by a larger competition coefficient a , whereas for fixed a , it expands if discounting is enhanced (larger c and/or smaller d). Altogether, a consistent pattern is that evolutionary reversals are more likely to occur in species characterized by significant competitive asymmetry, and facing strong discounting pressure.

When conditions for periodic evolutionary reversals are not satisfied, permanent low abundance and permanent high abundance represent alternative by-products of natural selection operating on competitive ability. Although there is a narrow range of parameters for which permanent high abundance evolves concomitantly with intermediate phenotypic value (Fig. 4C), there is a clear tendency for high abundance to evolve most often along with small trait value, whereas permanent low abundance can be associated with the evolution of large as well as intermediate trait value. This may help understand why the association of rarity and large body size in groups of closely related species remains difficult to establish empirically.

3.2 Effect of environmental change

The ecological parameters a , β , c , d may vary in response to environmental change. It turns out that even small and smooth changes in these parameters may have a dramatic impact on the eco-evolutionary dynamics of the population. Here we focus our discussion on the transition between eco-evolutionary cycles and permanent low abundance. A transition of this kind caused by a slight environmental deterioration should imply a dramatic rise of the extinction risk. Population cycling may suddenly lose evolutionary stability and be replaced with a state of permanent low abundance when selection at low density ceases to be directional (toward the critical, low trait value at which adaptive reversal occurs) and becomes stabilizing instead (transition seen from Fig. 3C to B). This can happen as a result of (i) a small increase in competitive asymmetry, β , which makes the direction of selection on any trait value change at some lower population density actually reached in the state of low abundance; (ii) slightly more competition (larger competition coefficient a), or slightly less discounting (small decrease of c , or small increase of d), which cause the whole range of equilibrium population density across the state of low abundance to rise, leading the selective pressure induced by competitive asymmetry to dominate and favor larger phenotype, hence permanent low density.

4 Discussion

How density can influence and be influenced by evolutionary processes has concerned biologists ever since Darwin suggested that abundant species were more likely than rare species to be the sources of evolutionary novelties. Nonetheless, despite considerable attention to the matter, evolutionary biologists still hold widely varying views on the consequences of population density on evolution (Orians, 1997), and on the role of evolution in determining population abundance and

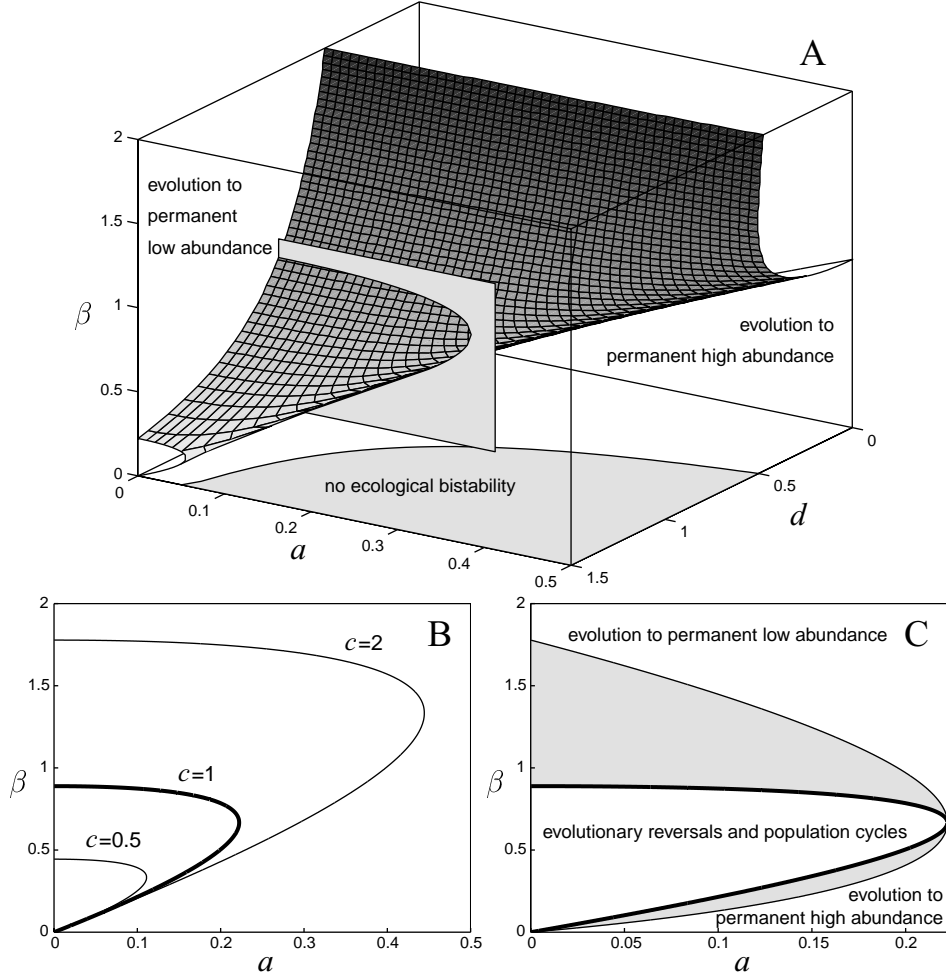


Figure 4: Eco-evolutionary dynamics depending on ecological parameters a (coefficient of intraspecific competition), β (strength of competitive asymmetry), and c and d (discounting parameters). **A**, Effect of a , d and β . The volume bounded by the displayed surface contains parameter combinations that lead to periodic evolutionary reversals. Permanent low abundance evolves above the surface. Permanent high abundance evolves below the surface. Ecological bistability occurs only for values of a and d lying outside the shaded region in the horizontal plane. Other parameter values: $c = 1.0$, $r_0 = 1.0$, $\gamma = 1.0$. **B**, Effect of discounting coefficient c on the region (inside curves) of a and β values for which periodic evolutionary reversals occur ($d = 0.75$). **C**, Effect of a and β on the transition between adaptively-driven population cycles and either permanent low abundance with large phenotypic trait, or permanent high abundance and small phenotypic trait. The shaded region indicates parameter combinations for which permanent low abundance and permanent high abundance evolve along with intermediate trait value. In **B** and **C**, the bold curve bounds the (a, β) region where periodic evolutionary reversals develop, and corresponds to the cross section indicated in **A**.

dynamics (Holt, 1997). This theoretical study investigates the interaction between population density and life-history evolution by focusing on an individual trait related to competitive performance that is potentially under different selection pressures depending on the population abundance. Our model allows for multiple ecological equilibria, which entails that the population may rest on a state of low abundance or on a state of high abundance under the very same conditions.

potentially under different selection pressures depending on In ecological systems that possess alternative equilibria, the equilibrium on which the population settles depends on ecological history, and recurrent jumps between equilibria have been traditionally explained by means of environmental or ecological factors (e. g., Southwood and Comins, 1976; Hanski, 1985; Crawley, 1992). In contrast, our analysis shows that the periodic alternation between low-density and high-density equilibria can develop on the evolutionary timescale as a result of a purely endogenous mechanism: periodic reversals of selection on a phenotypic trait.

The simple, deterministic model considered here produces perfectly regular evolutionary cycles in trait value and population density. Random variability, however, is inherent to all populations. In a stochastic environment, the regularity of such slow-fast cycles is likely to break down (Rinaldi and Scheffer, 2000), in lieu of which more irregular alternations of phases of low and high abundance should be expected. Documenting such fluctuations in population abundance requires exceptional data sets collected on a timescale seldom accessible to ecologists. Perhaps the best example of such data is provided by subfossil deposits of pelagic fish, which have been used to reconstruct several millenia of population dynamics, with time resolution as fine as a decade (Soutar and Isaacs, 1974; Baumgartner et al., 1992). In the Pacific sardine *Sardinops caerulea*, population data show that the species has persisted at very low density over more than 55% of the time, through phases of irregular durations, from 10-200 years. Alternations between low and high abundance occurred rapidly and more or less in unison across the whole species range. Interestingly, a competitor, and possibly predator species, the Northern anchovy *Engraulis mordax*, has been fluctuating more smoothly without reaching extreme population densities, suggesting that direct environmental factors may not be solely responsible for the dynamics of the sardine. Similar patterns have been documented in *Sardinops sagax* over the whole Holocene period, with bouts of very low abundance spanning up to 500 years (De Vries and Pearcy, 1982); and in *Sardinops melanistica* on the timescale of the last four centuries (Tsuboi, 1984; Kondô, 1987). Tens and even hundreds of consecutive generations at either high or very low abundance may have given ample time for contrasting selective pressures to operate on traits related to competitive performance, and cause the alternations of high and low abundance observed in the data. The combination of multiple ecological equilibria and adaptive reversals between them offers an alternative explanation, previously suggested in a verbal model by Cury (1988), to purely ecological models of such long-term fluctuations between high and low density in fish communities (Ferrière and Cazelles, 1999). It would be interesting to re-analyse the subfossil fish scale data to investigate the occurrence of concomitant changes in fish body size, which could be indicative of density fluctuations driven by evolutionary reversals.

4.1 Mechanism causing evolutionary reversals

The biological mechanism causing evolutionary reversals involves two ingredients. First, there must exist trait values in the phenotypic space near which mutant phenotypes can invade and yet fail to go to fixation, while their transitory presence cause the resident population to switch between two ecological states. This phenomenon brings new evidence that the ‘invasion-implies-fixation’ principle of adaptive dynamics theory can be violated even for arbitrarily small mutations, and does require the uniqueness of the ecological attractor to hold true (Geritz et al., 1997). So far the few examples known to contradict the invasion-implies-fixation principle had been constructed by resorting to mutations of unlikely large effect (Doebeli (1998); Diekmann et al. (1999); De Feo

and Ferrière (2000); Mylius and Diekmann (2001); see also Case (1995) and Abrams and Shen (1989) in the context of species invasion in communities).

The second key ingredient for evolutionary reversals is that selective pressures operate in opposite directions on the same phenotypes depending on whether the population density is high or low. Why this contrasting effect of selection arises in our model is easily understood: at high population density, a mutant is engaged in many competitive contests; thus, it has much to gain by investing more into competitive efficiency (through an increased trait value) at the expense of reducing its reproductive rate (provided that the trade-off between competition and reproduction is not too steep). In contrast, at low density encounters are few, there is little to be gained from improved competitive ability; thus, one can expect advantageous mutants to be characterized by a larger intrinsic reproductive rate, achieved with smaller phenotype.

Khibnik and Kondrashov (1997) also showed that cyclic evolution involving sharp transitions between multiple ecological attractors can occur in Red Queen dynamics of multispecies coevolution. Our study demonstrates that the coevolutionary Red Queen scenario is not necessary to explain the reversal of selective pressures between different ecological attractors and the endless variations in adaptive traits; purely intraspecific interactions are sufficient.

Matsuda and Abrams (1994a) also considered the evolution of body size under asymmetrical competition, but the uniqueness of ecological equilibrium at any trait value prevented the mechanism causing adaptive reversals to operate in their model. As a consequence, they could observe only the directional evolution of large body size and low population density, a process that could lead to population self-extinction. In contrast, if the conditions for adaptive reversals are met in our model, the evolution toward large phenotype terminates at a trait value where population density drops fast and dramatically whereas selective pressures revert and ‘rescue’ the population from extinction by promoting smaller phenotype and slowly increasing population density as a by-product. Taxon cycles driven by asymmetrical interspecific competition were proposed to explain the long-term maintenance of diversity in communities subject to colonization and coevolutionary-driven extinction (Rummel and Roughgarden, 1983, 1985; Taper and Case, 1992). Likewise, adaptive cycles driven by asymmetrical intraspecific competition can explain the long-term persistence of a single population subject to genetic variability (providing the mutants needed to beget switches between ecological equilibria) and selective reversals.

4.2 Concluding remarks

Any ecological scenario that makes the number of ecological attractors dependent upon an adaptive trait sets the stage for switches between population attractors driven by the evolutionary dynamics of the trait. This has been clearly recognized and exploited by Matsuda and Abrams (1994b) for showing that the evolution of anti-predator ability may result in self-extinction of a prey population. Here we have used the same principle to demonstrate that the occurrence of adaptive reversals and consequent population cycling is a likely property of ecological systems that possess alternative equilibria. We stress that this property is not bound to the assumption that multiple steady states are caused by a special ecological mechanism. A discounting function of the form of Holling type III response was chosen here to make the analysis mathematically tractable. Qualitatively similar results would be obtained with a Holling type II-like discounting function; the low-abundance stable equilibrium would simply be replaced with the zero equilibrium, thus making the ‘evolutionary suicide’ of the population almost unavoidable. Interestingly, some compelling evidence for evolutionary reversals of social traits has been gathered recently (Velicer et al., 1998; Hibbett et al., 2000). Sociality can induce an Allee effect that may be responsible for a discounting factor of the type considered here (Courchamp et al., 1999). Thus, adaptive switches between multiple ecological equilibria may point to a purely endogenous mechanism responsible for the repeated evolutionary rise and fall of social behavior.

Our study delineates two ways in which selection may depend on density. In the first and classical case, each value of a trait uniquely determines the population density. If the density varies monotonically (e. g. decreases) with the trait value, the direction of adaptation may change with density as a mere consequence of directional selection toward an intermediate phenotype: at lower trait value, hence higher density, selection would favor an increase of the trait; at higher trait value, hence lower density, selection would promote the decrease of the trait. In contrast, when multiple equilibria are feasible, the direction and strength of selection may differ at the same trait value depending upon the state (e. g. high versus low density) on which the population is actually resting. Real systems possessing multiple equilibria should therefore be useful to set up laboratory experiments in which the effect of density on selection is strictly isolated.

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5 Appendix

5.1 Condition for ecological bistability

The ecological model is given by eq. (1) with $r(u) = r_0 \exp(-\gamma u)$, where r_0 and γ are constant parameters. In the (u, a) parameter plane, the transition from one stable positive equilibrium to three positive equilibria (two stable, one unstable) corresponds to a so-called fold bifurcation, and two fold bifurcation curves determine two values of u (u_l and u_h) for each value of a within an appropriate range. These two curves meet at a single point (called cusp) which identifies the a value beyond which no bistability can occur. By writing the standard conditions for fold bifurcations (e. g., Kuznetsov, 1998)), we find

$$u_l = -\frac{1}{\gamma} \ln \left[\frac{x_l}{r_0} \left(\frac{c}{x_l^2 + d^2} + a \right) \right] \quad u_h = -\frac{1}{\gamma} \ln \left[\frac{x_h}{r_0} \left(\frac{c}{x_h^2 + d^2} + a \right) \right]$$

where

$$x_l = \left[\frac{c - 2ad^2 - \sqrt{c(c - 8ad^2)}}{2a} \right]^{1/2} \quad x_h = \left[\frac{c - 2ad^2 + \sqrt{c(c - 8ad^2)}}{2a} \right]^{1/2}$$

The cusp point is given by

$$u = -\frac{1}{\gamma} \ln \left[\frac{8dr_0}{3\sqrt{3}c} \right] \quad a = \frac{c}{8d^2}$$

5.2 Condition for adaptively-driven population cycles

The selection gradient is $s(u, x) = -r_0\gamma \exp(-\gamma u) + \beta x$. Hence the selection null-isocline in the (u, x) space is:

$$x = \frac{r_0\gamma}{\beta} \exp(-\gamma u)$$

Adaptively-driven population cycles occur if and only if the selection null-isocline separates the upper branch of high population equilibria, and the lower branch of low population equilibria. Elementary algebra yields the following necessary conditions:

$$\begin{aligned} \frac{r_0\gamma}{\beta} \exp(-\gamma u_l) &> x_l & \frac{r_0\gamma}{\beta} \exp(-\gamma u_h) &< x_h \\ \frac{r_0\gamma}{\beta} \exp(-\gamma u_l) &< \frac{d^2 r(u_l)}{ax_l^2} & \frac{r_0\gamma}{\beta} \exp(-\gamma u_h) &> \frac{d^2 r(u_h)}{ax_h^2} \end{aligned}$$

and systematic numerical computations confirm that these conditions are also sufficient. The surface and curves displayed in Figure 4 are computed from these conditions.

5.3 Numerical analysis

We used the following asymmetric competition function:

$$b(u, u') = 2a \left\{ 1 - [1 + \exp(\delta(u' - u))]^{-1} \right\}$$

The strength of competitive asymmetry is measured by $\beta = a\delta/2$. Notice that for all u , $b(u, u) = a$. Numerical bifurcation analysis were carried out by making use of the software LOCBIF (Khibnik et al., 1993).